



# Elementary Statistics Tables

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### Preface

Having published my Statistics tables in 1978, the obvious question is: why another book of Statistics tables so soon afterwards? The answer derives from reactions to the first book from a sample of some 500 lecturers and teachers covering a wide range both of educational establishments and of departments within those establishments. Approximately half found Statistics tables suitable for their needs; however the other half indicated that their courses covered rather less topics than included in the Tables, and therefore that a less comprehensive collection would be adequate. Further, some North American advisers suggested that more 'on the spot' descriptions, directions and illustrative examples would make such a book far more attractive and useful. Elementary statistics tables has been produced with these comments very much in mind.

The coverage of topics is probably still wider than in most introductory Statistics courses. But useful techniques are often omitted from such courses because of the lack of good tables or charts in the textbook being used, and it is one of the aims of this book to enable instructors to broaden the range of statistical methods included in their syllabuses. Even if some of the methods are completely omitted from the course textbook, instructors and students will find that these pages contain brief but adequate explanations and illustrations.

In deciding the topics to be included, I was guided to an extent by draft proposals for the Technician Education Council (TEC) awards, and Elementary statistics tables essentially covers the areas included in this scheme for which tables and/or charts are necessary. The standard distributions are of course included, i.e. binomial, Poisson, normal, t, x2 and F. Both individual and cumulative probabilities are given for binomial and Poisson distributions, the cumulative Poisson probabilities being derived from a newly designed chart on which the curves are virtually straight: this should enhance ease of reading and accuracy. A selection of useful nonparametric techniques is included, and advocates of these excellent and easy-to-apply methods will notice the inclusion of considerably improved tables for the Kruskal-Wallis and Friedman tests, and a new table for a Kolmogorov-Smirnov general test for normality. The book also contains random-number tables, including random numbers from normal and exponential distributions (useful for simple simulation experiments), binomial coefficients, control chart constants, various tables and

charts concerned with correlation and rank correlation, and charts giving confidence intervals for a binomial p. The book ends with four pages of familiar mathematical tables and a table of useful constants, and a glossary of symbols used in the book will be found inside the back cover.

Considerable care and thought has been given to the design and layout of the tables. Special care has been taken to simplify a matter which many students find confusing: which table entries to use for one-sided and two-sided tests and for confidence intervals. Several tables, such as the percentage points for the normal, t,  $\chi^2$  and F distributions, may be used for several purposes. Throughout this book, α, and α, are used to denote significance levels for onesided (or 'one-tailed') and two-sided tests, respectively, and y indicates confidence levels for confidence intervals, (Where occasion demands, we even go so far as to use and at to denote significance levels for right-hand and left-hand one-sided tests.) If a table can be used for all three purposes, all three cases are clearly indicated, with 5% and 1% critical values and 95% and 99% confidence levels being highlighted.

My thanks are due to many people who have contributed in various ways to the production of this book. I am especially grateful to Peter Worthington and Arthur Morley for their help and guidance throughout its development: Peter deserves special mention for his large contribution to the new tables for the Kruskal-Wallis and Friedman tests. Thanks also to Graham Littler and John Silk who very usefully reviewed some early proposals, and to Trevor Easingwood for discussions concerning the TEC proposals. At the time of writing, the proof-reading stage has not yet arrived; but thanks in advance to Tonie-Carol Brown who will be helping me with that unenviable task. Finally, I must express my gratitude to the staff of the Cripps Computing Centre at Nottingham University: all of the tables and charts have been newly computed for this publication, and the service which they have provided has been excellent.

Naturally, total responsibility for any errors is mine alone. It would be nice to think that there are none, but I would greatly appreciate anybody who sees anything that they know or suspect to be incorrect communicating the facts immediately to me.

> HENRY NEAVE October 1979

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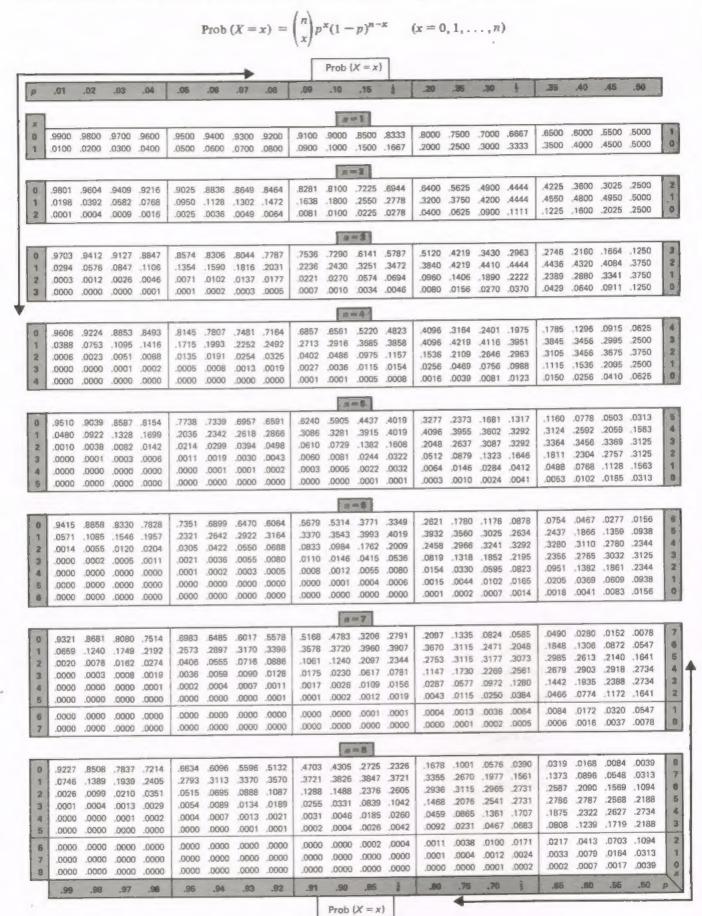
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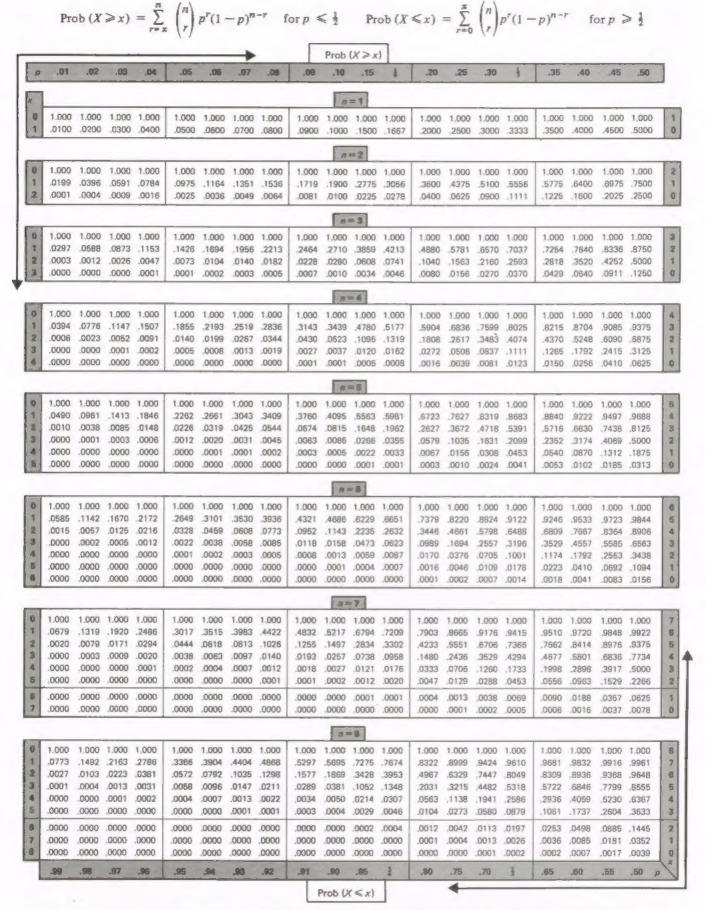
## The binomial distribution: individual probabilities



If the probability is p that a certain event (often called a 'success') occurs in a trial of an experiment, the binomial distribution is concerned with the total number X of successes obtained in n independent trials of the experiment. Pages 4, 6, 8 and 10 give Prob (X = x) for all possible

x and n up to 20, and 39 values of p. For values of  $p \le \frac{1}{2}$  (along the top horizontal) refer to the x-values in the left-hand column; for values of  $p \ge \frac{1}{2}$  (along the bottom horizontal) refer to the x-values in the right-hand column.

### The binomial distribution: cumulative probabilities



Pages 5, 7, 9 and 11 give cumulative probabilities for the same range of binomial distributions as covered on pages 4, 6, 8 and 10. For values of  $p \le \frac{1}{2}$  (along the top horizontal) refer to the x values in the left-hand column, the table entries giving Prob  $(X \ge x)$ ; for values of  $p \ge \frac{1}{2}$  (along the bottom horizontal) refer to the x-values in the

right-hand column, the table entries giving Prob  $(X \le x)$  for these cases. Note that cumulative probabilities of the opposite type to those given may be calculated by Prob  $(X \le x) = 1 - \operatorname{Prob}(X \ge x + 1)$  and Prob  $(X \ge x) = 1 - \operatorname{Prob}(X \le x - 1)$ .

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		,0000	.0000	.0000	.0000	_0000	.0000	0000	.0000	.0000	.0006	.0011	1	.0115				1009	1489	
8 .	.0000	,0000	.0000	.0000			0000	,0000		.0000				.0024			1000	.0420	0762	
_		.0000	0000	0000			.0000	.0000			0000			.0004				.0125	.0277	
10	.0000	,0000	.0000	.0000	,0000	0000	.0000	.0000		.0000	0000		-	,0000			-			
		.0000				.0000				.0000				0000.			7.9	.0000	.0010	
12 .	,0000	,0000	.0000	.0000	,0000	.0000	.0000	.0000	.0000	,0000	UUUU	.0000	.0000	,UUUU	.0000	Ventucian	30000	.0000	,0001	10001
										n =	13		1				1			
0 .	8775	,7690	.6730	.5882	.5133	4474	3893			2542				.0238					.0004	
1 .	.1152	,2040	.2706	3186		3712		3824		.3672				1029	0540		The second second	0113		
		.0250		0797		,1422				.2448				2059				1107		0349
		.0019		.0122		.0333				.0997				2517			2000	.1845	.1350	
		.0001		.0013		.0053				.0277			100000	.1258				2214		
5 .	,0000	0000	.0000	.0001	-	.0006		_					-	_			-			
		.0000		.0000	.0000		.0001			.0008			,0230	0559		.1378		.1958	.1775	
_		.0000		0000	.0000		.0000			1000			.0058	.0186	.0442		10000	.0656		
_		.0000		.0000		.0000				0000		.0000	.0001					0243		
	0000	,0000		.0000	.0000			,0000,		0000		.0000	.0000	1000.				.0065		.0349
		.0000						.0000		0000	_	.0000	_0000	_	,0001		-	.0012		.0095
_		.0000		.0000	.0000			.0000	1	0000		.0000	.0000	.0000				.0001		
_		.0000	.0000		,0000			.0000	0000			0000	.0000	.0000		.0000	.0000	.0000	.0000	1000,
	.0000		.97	.96	.95	.94	.93	.92	.91	.90	,86	1	.80	.75			_	_	$\overline{}$	.50

EXAMPLES: If ten dice are thrown, what is the probability of obtaining exactly two sixes? With n = 10 and  $p = \frac{1}{6}$ , Prob (X = 2) is found from the table to be 0.2907.

If a treatment has a 90% success-rate, what is the probability that all of twelve treated patients recover? With n = 12 and p = 0.9, the table gives Prob(X = 12) = 0.2824.

							+	-			(X ≥ x	-									1
ρ	.01	.02	.03	.04	.05	.06	.07	.00	.09	.10	.15	#	.20	.25	.30	1	,35	.40	.45	.50	
K										10 3	= 9										
0	1.000	1,000	1,000	1,000	1.000	1,000	1.000	1,000	1,000	1,000	1,000	1,000	1,000	1.000	1,000	1,000	1,000	1,000	1.000	1.000	Ш
1	.0865	.1663	2398	.3075	.3698	4270	4796	5278	.5721	.6126	.7684	8062	8658	,9249	.9596	,9740	.9793	.9899	9954	9980	ш
2	.0034	.0131	.0282	.0478	200	.0978	.1271	.1583	10000		,4005	4573	.5638	.6997	.8040	.8569	.8789	9295	9615	9805	ш
3	.0001	.0000	0020	.0045	.0084	0138	.0209	.0298	0405	.0530	.1409	.1783	2618	3993	.5372	6228	3911	7682 5174	8505 6386	9102	Ш
5	.0000	.0000	.0000	.0000	.0006	.0001	.0023	.0037	.0057	.0083	.0339	.0480	0856	.0489	.0988	.1448	1717	2666	3786	5000	н
													-						-		-
6 7	.0000	0000	.0000	.0000	0000	0000	.0000	.0000	.0000	.0001	.0006	.0011	.0031	.0100	.0253		.0536	0994	1658	2539	п
8	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	0000	.0003	,0013	.0004	,0083	.0112	.0038	0498	0898	В
9	.0000	0000	.0000		.0000	.0000	.0000	0000	.0000	.0000	.0000	0000	.0000	.0000	.0000		.0001	.0003	.0008	0020	
			locac	Judo	10000		10000	10000	10000		10000	10000	10000	10200	10000	10001	1000	10000	10000		1
										n =	_										
0	1.000	1.000	1.000		1.000	1,000	1.000		1.000		1.000		1,000	1.000	1,000		1.000	1.000	1,000		3
2	.0956	.1829	.2626	.3352		.4614	.5160	5656	.6106	6513	.8031	.8385	.8926	.9437	.9718	.9827 enen	.9865	9940	9975	9893	В
3	.0001	.0009	.0345	.0582		0188	.1517	.1879	.2254	2639	1798	5155	.6242	.7560	.8507		7384	.8327	9004	9453	н
4	.0000	.0000	1000	.0004	0.000	.0020	.0036	.0058	.0088	.0128	.0500	D697	.1209	2241	3504	.4407	4862	6177	.7340	.8281	
5	.0000	.0000	.0000	.0000	,0001	0002	.0003	.0006	.0010	.0016	.0099	.0155	.0328	.0781	.1503	.2131	2485	.3669		.6230	
6	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0014	.0024	.0064	.0197	.0473	.0766	.0949	.1662	2616	3770	
7	0000	0000	0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0009	.0035	.0106		.0260	.0548	1020		ш
В	0000	,0000	0000	0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	,0001	.0004		.0034	.0048	0123	0274		н
9	.0000	.0000	.0000	0000	,0000	.0000	.0000	0000	.0000	.0000	,0000	,0000	,0000	0000	.0001		,0005	0017	,0045		н
0	.0000	.0000	.0000	.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	,0000	.0000	.0000	.0000	0000	.0000	.0001	.0003	.0010	
										77 ==	11										
3	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000		1.000	1.000	1.000	1.000	1.000	1.000	1,000	1.000	1,000	1
1			2847	3618		4937	5499	6004	.6456	.6862	8327	.8654	9141	9578	9802	9884	.9912	9964	9986	9995	1
2		.0195	0413	0692		1382	.1772		2601	3026	5078	5693	.6779	.8029		9249	.9394	.9698		9941	
3	.0002	.0012	.0037	.0083	.0152	.0248	.0370	.0519	.0695	.0896	.2212	.2732	.3826	.5448	.6873	.7659	.7999	.8811	.9348	9673	
3	.0000	,0000	.0002	.0007	.0016	.0030	.0053	.0085	.0129	.0185	.0694	.0956	.1611	2867	4304	.5274	.5744	,7037	8089	8867	100
5	.0000	,0000	.0000	.0000	.0001	.0003	.0005	.0010	.0017	.0028	.0159	.0245	.0504	.1146	2103	2890	.3317	.4672	6029	7256	
1	.0000	.0000	0000	.0000	.0000	.0000	.0000	.0001	.0002	.0003	.0027	.0046	.0117	.0343	.0782	.1221	.1487	.2465	3669	5000	100
3	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0003	.0006	.0020	.0076	.0216	.0386	.0501	.0994	1738	2744	100
3	.0000	.0000	.0000	.0000	.0000	.0000	_0000	.0000	.0000	.0000	.0000	.0001	.0002	.0012	.0043		.0122	,0293	0610		
9	,0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000		,0000	.0000	.0000	,0001	,0006		,0020	.0059		.0327	
)	.0000	,0000	0000	.0000	,0000	.0000	.0000	.0000	.0000	.0000	,0000	.0000	.0000	,0000		.0001	.0002	.0007	.0022	.0059	
y	.0000	,0000	.0000	,0000	,0000	,0000	,0000	.0000	,0000	,0000	.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	.0002	0000	
										77 =	12			_							100
0	1,000	1,000	1.000	1.000	1.000	1,000	1,000	1,000	1.000	1,000	1,000	1,000	1,000	1,000	1,000	1.000	1,000	1.000	1.000	1.000	1
1		.2153	3082	.3873	1000	5241	.5814	6323	100	.7176	8578	8878		.9683	9862	,9923	.9943	9978		,9998	1
5		0231				1595				.3410				.8416				.9804			1
3	.0002		0048		- 3	.0316	.0468		10000	1109		3226		6093				9166		.9807	
4	.0000	.00001	.0003	.0001	42.64	.0043	.0009		.0027	.0256	0922	.0364		.3512			4167	.7747	.6956		
-							-		-						-						
8	.0000		.0000	.0000		.0000	.0001		.0003	.0005	-0046	.0079	.0194		.1178		2127		4731		
7 8	.0000	.0000	,0000	.0000	,0000	0000	.0000	.0000	.0000	.0000	.0007	.0013	.0039	.0143	.0386			.1582			
9	.0000	.0000	.0000	,0000	.0000	-0000	.0000	.0000	.0000	,0000	.0000	.0000		,0004	0017			,0153			1
0	.0000	.0000	.0000	.0000		.0000		.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0002				.0079		
	0000		.0000			.0000	.0000		,0000		.0000				.0000		.0001		.0011	7.16.5	
		.0000		****		.0000	.0000		.0000		.0000				.0000			.0000			
	1 000	1.000	1.000	1.000	1.000	1.000	1 000	1.000	1.000		1 000	1 000	1 000	1.000	1 000	1.000	1 000	1 000	1 220	1 000	-
3		1.000		7.74	10000	1.000		2000	27/20/20/2	1.000				1.000				1.000			17
2		2310	.0564	0932	1000	.5526	6107 2298	7 7 7 7 7	100.00	.7458		10000		.9762 .8733	9903	2000	9963		.9996		1
	.0003		.0062			.0392	0578			.1339		3719			.7975			.9421			10
		.0001	.0005	.0014	7.00	.0060	.0103		200007	.0342		.1581			.5794			.8314			-
3	.0000	.0000		.0001		.0007	.0013		.0041	.0065		.0512			3457			.6470			1
,	.0000	0000	.0000	.0000	.0000	.0001	1000	.0003	.0005	.0009	.0075	.0127	.0300	.0802	.1654	.2413	-2841	.4256	.5732	.7095	
,		.0000	.0000	.0000		.0000	.0000		.0001			.0024		.0243	.0624		.1295		3563		1
3				.0000		.0000	.0000		.0000	.0000		.0003			.0182			.0977			1
9	.0000	.0000	.0000	.0000	.0000	.0000	,0000	,0000	.0000	,0000	.0000	.0000	.0002	.0010	.0040	8800,	.0126	.0321	.0698	.1334	
0	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	,0007	.0016	.0025	,0078	.0203	.0461	_ ;
	_0000	.0000	.0000	.0000	.0000	.0000	.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	,0001	.0002	0003	,0013	.0041	.0112	
2	0000	.0000	.0000	.0000	.0000	.0000	,0000		,0000	.0000		.0000		.0000	,0000		.0000	.0001		.0017	
	.0000	,0000	,0000	,0000	,0000	0000	.0000	.0000	.0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	_0000	.0000	.0000	.0001	
	-	00	,97	,98	.96	.94	.93	.92	.91	.90	.85	- 1	,80	.75	.70	-	.65	.60	.55	.50	10
	.99	.96	4 SP P	4.00	A GRANT	And the second	-	1000	-47.4	Printer.	District of the last		-				100	1 alberto	7.00.00		300

EXAMPLES: If ten dice are thrown, what is the probability of obtaining at most two sixes? Now, Prob  $(X \le 2) = 1 - \text{Prob}(X \ge 3)$ . With n = 10 and  $p = \frac{1}{6}$ , the table gives  $\text{Prob}(X \ge 3)$  as 0.2248, so  $\text{Prob}(X \le 2) = 1 - 0.2248 = 1$ 

0.7752. If a treatment has a 90% success-rate, what is the probability that no more than ten patients recover out of twelve who are treated? With n=12 and p=0.9, the table gives Prob  $(X \le 10)=0.3410$ .

3887 7 1229 30000 3000 3000 3000 3000 3000 3000	.7386 .2261 .0323 .0029 .0002 .0000 .0000 .0000	.6528 .6528 .6070 .0000	.5421 .3388 .0988 .0178 .0022 .0002 .0000 .0000	.4877 .3593 .1229 .0259 .0037 .0004 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.3758 .1559 .0398 .0070 .0009 .0000 .0000 .0000 .0000 .0000	.0000 .0000 .0000 .0000 .0000 .0000	.3788 .2141 .0745 .0178 .0031 .0004 .0000 .0000 .0000 .0000 .0000 .0000	.2670 .3698 .2377 .0940 .0256 .0061 .0000 .0000 .0000 .0000 .0000 .0000	.2288 .3559 .2570 .1142 .0349 .0078 .0002 .0000 .0000 .0000 .0000 .0000 .0000	.2912 .2056 .0998 .0352 .0093 .0019 .0000 .0000 .0000	,0779 ,2181 ,2835 ,2268 ,1247 ,0499 ,0150 ,0004 ,0006 ,0001 ,0000 ,0000	.0440 .1539 .2501 .2501 .1720 .0860 .0322 .0092 .0003 .0000	.2402 .2202 .1468 .0734 .0280 .0082 .0018 .0003	.0407 .1134 .1943 .2290 .1963 .1262 .0618 .0232	.0779 .1559 .2143 .2143 .1607 .0918 .0402 .0134 .0033	.0024 .0181 .0634 .1366 .2022 .2178 .1759 .1082 .0510 .0183 .0049	.0073 .0317 .0845 .1549 .2066 .2066 .1574 .0918 .0408	.0027 .0141 .0462 .1040 .1701 .2088 .1952 .1398 .0762 .0312	.0056
2229 3081 3000 3000 3000 3000 3000 3000 3000	.2153 .0286 .0023 .0001 .0000	.2827 .0568 .0070 .0000	.3294 .0892 .0149 .0017 .0001 .0000	.3593 .1229 .0259 .0037 .0004 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.3758 .1559 .0398 .0070 .0009 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.3815 .1867 .0562 .0118 .0002 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .3387 .3801 .2003	.3788 .2141 .0745 .0178 .0031 .0004 .0000 .0000 .0000 .0000 .0000 .0000	.3898 .2377 .0940 .0256 .0061 .0008 .0001 .0000 .0000 .0000	.2288 .3559 .2570 .1142 .0349 .0078 .0002 .0000 .0000 .0000 .0000 .0000 .0000	.1028 .2539 .2912 .2056 .0998 .0352 .0093 .0019 .0000 .0000 .0000	.2181 .2835 .2268 .1247 .0499 .0150 .0034 .0006 .0001 .0000	.1538 .2501 .2501 .1720 .0860 .0322 .0092 .0020 .0003	.0832 .1802 .2402 .2202 .1468 .0734 .0280 .0082 .0018 .0003	.0407 .1134 .1943 .2290 .1963 .1262 .0618 .0232 .0066 .0014	.0240 .0779 .1559 .2143 .2143 .1607 .0918 .0402 .0134 .0033	.0181 .0634 .1366 .2022 .2178 .1759 .1082 .0510 .0183 .0049	.0073 .0317 .0845 .1549 .2066 .1574 .0918 .0408	.0027 .0141 .0462 .1040 .1701 .2088 .1952 .1398 .0762 .0312	.0009 .0058 .0222 .0611 .1222 .1833 .2095 .1833 .1222 .0611
2229 3081 3000 3000 3000 3000 3000 3000 3000	.2153 .0286 .0023 .0001 .0000	.2827 .0568 .0070 .0000	.3294 .0892 .0149 .0017 .0001 .0000	.3593 .1229 .0259 .0037 .0004 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.3758 .1559 .0398 .0070 .0009 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.3815 .1867 .0562 .0118 .0002 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .3387 .3801 .2003	.3788 .2141 .0745 .0178 .0031 .0004 .0000 .0000 .0000 .0000 .0000 .0000	.3898 .2377 .0940 .0256 .0061 .0008 .0001 .0000 .0000 .0000	.3559 .2570 .1142 .0349 .0078 .0013 .0002 .0000 .0000 .0000 .0000 .0000	.2539 .2912 .2056 .0998 .0352 .0093 .0019 .0000 .0000 .0000	.2181 .2835 .2268 .1247 .0499 .0150 .0034 .0006 .0001 .0000	.1538 .2501 .2501 .1720 .0860 .0322 .0092 .0020 .0003	.0832 .1802 .2402 .2202 .1468 .0734 .0280 .0082 .0018 .0003	.0407 .1134 .1943 .2290 .1963 .1262 .0618 .0232 .0066 .0014	.0240 .0779 .1559 .2143 .2143 .1607 .0918 .0402 .0134 .0033	.0181 .0634 .1366 .2022 .2178 .1759 .1082 .0510 .0183 .0049	.0073 .0317 .0845 .1549 .2066 .1574 .0918 .0408	.0027 .0141 .0462 .1040 .1701 .2088 .1952 .1398 .0762 .0312	.0009 .0058 .0222 .0611 .1222 .1833 .2095 .1833 .1222 .0611
0081 0000 0000 0000 0000 0000 0000 0000	.0286 .0023 .0001 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0568 .0070 .0000	.0892 .0149 .0017 .0001 .0000	.1229 .0259 .0037 .0004 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.1559 .0398 .0070 .0009 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.1867 .0562 .0118 .0018 .0002 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.2141 .0745 .0178 .0031 .0004 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.2377 ,0940 ,0258 ,0061 .0008 .0001 .0000 ,0000 ,0000 .0000	.2570 .1142 .0349 .0078 .0013 .0002 .0000 .0000 .0000 .0000 .0000 .0000	.2912 .2056 .0998 .0352 .0093 .0019 .0000 .0000 .0000	.2835 .2268 .1247 .0499 .0150 .0034 .0006 .0001 .0000	.2501 .2501 .1720 .0860 .0322 .0092 .0020 .0003 .0000	.1802 .2402 .2202 .1468 .0734 .0280 .0082 .0018 .0003	.1134 .1943 .2290 .1983 .1262 .0618 .0232 .0066 .0014	.0779 .1559 .2143 .2143 .1607 .0918 .0402 .0134 .0033	.0634 .1366 .2022 .2178 .1759 .1082 .0510 .0183 .0049	.0317 .0845 .1549 .2066 .1574 .0918 .0408 .0138	.0141 .0462 .1040 .1701 .2088 .1952 .1398 .0762	.0056 .0222 .0611 .1222 .1833 .2095 .1833 .1222 .0611
0003 0000 0000 0000 0000 0000 0000 000	.0023 .0001 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0070 .0006 .0000	.0149 .0017 .0001 .0000	.0258 .0037 .0004 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0398 .0070 .0009 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0562 .0118 .0018 .0002 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0745 .0178 .0031 .0004 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0940 .0256 .0061 .0008 .0001 .0000 .0000 .0000 .0000	.0142 .0349 .0078 .0013 .0002 .0000 .0000 .0000 .0000 .0000	.2056 .0998 .0352 .0093 .0019 .0003 .0000 .0000	.2268 .1247 .0499 .0150 .0034 .0006 .0001 .0000 .0000	.2501 .1720 .0860 .0322 .0092 .0020 .0003 .0000	.2402 .2202 .1468 .0734 .0280 .0082 .0018 .0003	.1943 .2290 .1963 .1262 .0618 .0232 .0066 .0014	.1559 .2143 .2143 .1607 .0918 .0402 .0134 .0033	.1366 .2022 .2178 .1759 .1082 .0510 .0183 .0049	.0845 .1549 .2066 .2066 .1574 .0918 .0408 .0138	.0462 .1040 .1701 .2088 .1952 .1398 .0762 .0312	.0222 .0611 .1222 .1833 .2095 .1833 .1222 .0611
0000 0000 0000 0000 0000 0000 0000 0000 0000	.0001 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0006 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0017 .0001 .0000	.0037 .0004 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0070 .0009 .0001 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .3963 .3785 .1691	.0116 .0018 .0002 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0178 .0031 .0004 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0256 .0061 .0008 .0001 .0000 .0000 .0000 .0000	.0349 .0078 .0013 .0002 .0000 .0000 .0000 .0000 .0000	.0998 .0352 .0093 .0019 .0003 .0000 .0000 .0000	.1247 .0499 .0150 .0034 .0006 .0001 .0000 .0000	.1720 .0860 .0322 .0092 .0020 .0003 .0000	.2202 .1468 .0734 .0280 .0082 .0018 .0003	.2290 .1963 .1262 .0618 .0232 .0066 .0014	.2143 .2143 .1607 .0918 .0402 .0134 .0033	.2022 .2178 .1759 .1082 .0510 .0163 .0049	.1549 .2066 .2066 .1574 .0918 .0408 .0138	.1040 .1701 .2088 .1952 .1398 .0762 .0312	.0611 .1222 .1833 .2095 .1833 .1222 .0611
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0000 0000 0000 0000 0000 0000 0000 0000 0000	.0000 .0000 .0000 .0000 .0000 .0000 .0000 .7386 .2261 .0323 .0029 .0000 .0000 .0000	.0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .3388 .0178 .0022 .0002 .0000 .0000	.0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0000 .0000 .0000 .0000 .0000 .0000 .0000 .3963 .3785 .1691	.0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0000 .0000 .0000 .0000 .0000 .0000 .0000	.0001 .0000 .0000 .0000 .0000 .0000	,0002 ,0000 ,0000 ,0000 ,0000 ,0000	.0019 .0003 .0000 .0000 .0000 .0000	.0034 .0006 .0001 .0000 .0000	.0092 .0020 .0003 .0000	,0280 ,0082 ,0018 ,0003	.0618 .0232 .0066 .0014	.0918 .0402 .0134 .0033	.1082 .0510 .0163 .0049	.1574 .0918 .0408 .0138	.1952 .1398 .0762 .0312	.2095 .1833 .1222 .0611
0000 0000 0000 0000 0000 0000 0000 0000 0000	.0000 .0000 .0000 .0000 .0000 .0000 .0000 .7386 .2261 .0323 .0029 .0000 .0000 .0000	.0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .3388 .0178 .0022 .0002 .0000 .0000	.0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0000 .0000 .0000 .0000 .0000 .0000 .0000 .3963 .3785 .1691	.0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000	.0000 .0000 .0000 .0000 .0000 .0000 .0000	.0001 .0000 .0000 .0000 .0000 .0000	,0002 ,0000 ,0000 ,0000 ,0000 ,0000	.0019 .0003 .0000 .0000 .0000 .0000	.0034 .0006 .0001 .0000 .0000	.0092 .0020 .0003 .0000	,0280 ,0082 ,0018 ,0003	.0618 .0232 .0066 .0014	.0918 .0402 .0134 .0033	.1082 .0510 .0163 .0049	.1574 .0918 .0408 .0138	.1952 .1398 .0762 .0312	.2095 .1833 .1222 .0611
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0004 0000 0000 0000 0000	.0029 .0002 .0000 .0000 .0000 .0000	.0086 .0008 .0001 .0000 .0000 .0000	.0178 .0022 .0002 .0000 .0000	.0307 .0049 .0006	.0468			.3605		,2312		.1319			.0171	.0128	.0047		.0005
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0000	.0000	.0000	.0000	.0000	,0000	.0000	,0001	.0001	.0003		.0053	.0138	.0393	.0811	-	.1319	.1771		.1984
0000				.0000	,0000	.0000	,0000	.0000	,0000	.0005	.0011	.0035	.0131	.0348	.0574	.0710	,1181	.1647	.1984
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1005	.0034	.0102	.0211	.0369	.0541		.0970	.1198		-2285	2423				.1066	.0888	.0468		
0000	.0002	.0010	.0029	.0061	.0112	.0183	.0274	.0385		.1311	.1575	.2001	.2252	2040	.1732	.1563	,1014	,0572	,0278
0000	.0000	.0001	,0003	8000.	.0017	,0033	.0057	.0091	.0137	.0565	.0756	.1201	.1802	.2099	.2078	.2008	.1623	.1123	.0887
0000	.0000	.0000	.0000	.0001	.0002	.0005	.0009	.0017	.0028	.0180	.0277	.0550	.1101	.1849	.1905	_1982	,1983	.1684	,1222
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429	.2461					.3726			.3150				.0426						
	.0402				.1935	.2244		2677		2673		.1914	.1136	.0581	.0345				.0010
447		.0120		1000	.0618	.0644		.1324		.2359		10000	.1893						,0052
447 1117 0006		.0013			.0138	.0222		.0458		.1457				1868			1370		.0182
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 .0000         .0000         .0000         .0001         .0003         .0007         .0013         .0023         .0039         .0236           0         .0000         .0000         .0000         .0000         .0001         .0002         .0000         .0007         .0065           0         .000	0 .000	0 .0000 .0001 .0004 .0010 .0023 .0044 .0075 .0118 .0175 .0688 .0893 .1361 0 .0000 .0000 .0000 .0000 .0001 .0003 .0007 .0013 .0023 .0039 .0236 .0357 .0680 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0002 .0004 .0007 .0065 .0112 .0267 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0014 .0028 .0084 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0004 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0004 0 .0000	0 .000	0 .0000 .0001 .0004 .0010 .0023 .0044 .0075 .0118 .0175 .0688 .0893 ,1361 .1914 .2081 0 .0000 .0000 .0000 .0000 .0001 .0003 .0007 .0013 .0023 .0039 .0236 .0357 .0680 .1276 .1784 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0002 .0004 .0007 .0065 .0112 .0287 .0688 .1201 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0014 .0028 .0844 .0279 .0644 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0014 .0028 .0021 .0093 .0276 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0004 .0025 .0095 0 .000	0 .0000 .0001 .0004 .0010 .0023 .0044 .0075 .0118 .0175 .0688 .0893 ,1361 .1914 .2081 .1963 0 .0000 .0000 .0000 .0000 .0001 .0003 .0007 .0013 .0023 .0039 .0236 .0357 .0680 .1276 .1784 .1963 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0002 .0004 .0007 .0065 .0112 .0287 .0688 .1201 .1542 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0014 .0028 .0084 .0279 .0644 .0964 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0014 .0028 .0084 .0279 .0644 .0964 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0004 .0021 .0093 .0276 .0482 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0004 .0025 .0095 .0193	0 .0000 .0001 .0004 .0010 .0023 .0044 .0075 .0118 .0175 .0688 .0893 .1361 .1914 .2081 .1963 .1849 0 .0000 .0000 .0000 .0000 .0001 .0003 .0007 .0013 .0023 .0039 .0236 .0357 .0880 .1276 .1784 .1963 .1991 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0002 .0004 .0007 .0065 .0112 .0267 .0868 .1201 .1542 .1685 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0014 .0028 .0084 .0279 .0644 .0964 .1134 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0004 .0025 .0095 .0183 .0263 0 .0000	0 .0000 .0001 .0004 .0010 .0023 .0044 .0075 .0118 .0175 .0688 .0893 .1361 .1914 .2081 .1963 .1849 .1379 0 .0000 .0000 .0000 .0000 .0001 .0003 .0007 .0013 .0023 .0039 .0236 .0357 .0880 .1276 .1784 .1963 .1991 .1839 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0014 .0028 .0112 .0267 .0668 .1201 .1542 .1685 .1927 0 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0000 .0001 .0014 .0028 .0084 .0279 .0644 .0964 .1134 .1808 0 .0000 .0	0 .0000 .0001 .0004 .0010 .0023 .0044 .0075 .0118 .0175 .0688 .0893 .1361 .1914 .2081 .1963 .1849 .1379 .0875 0 .0000 .0000 .0000 .0000 .0001 .0003 .0007 .0013 .0023 .0039 .0236 .0357 .0880 .1276 .1784 .1963 .1991 .1839 .1432 0 .0000

0	.01	.02	.03	.04	O.C.	DE	0.7	00	-00	10	45		- Open	40	94	-	.35	40	AE	100
p	.01	.UZ	.03	.(14)	.06	.06	07	.08	.09	.10	.15	3	.20	.25	.30		.35	.40	A6	.50
¥									_	n =	= 14									
0	1 000	1.000	1.000	1.000		1 000	1 000		1 000	1.000	1.000	1 000	1.000	1.000	1 000	1.000	1 000	1.000	1.000	1 000
2	1313	2464	3472 0645	4353 1059	1530	5795	6380	.6888	7330	7712	.8972	9221	9560	9872	9932	9966	9976 9795	9992	9998	9999
3	0003	0025	.0077	0167	.0301	2037	2564	.0958	3632 1255	1584	3521	7040 4205	8021 5519	8990 7189	9525 8392	9726 8947	9161	9602	9830	9935
4	0000	.0001	,0006	.0019	.0042	.0000	.0136	.0214	.0315	.0441	.1465	1937	3018	4787	6448	7388	7795	8757	9368	9713
5	0000	-0000	.0000	.0002	.0004	.0010	.0020	.0035	.0059	.0092	.0467	0690	1298	2585	4158	5245	5773	7207	8328	9102
6	0000	.0000	.0000	,0000	.0000	,0001	.0002	.0004	.0008	.0016	.0115	0191	0439	1117	2195	3102	3595	5141	6627	7880
7	0000	0000	.0000	.0000	0000	.0000	.0000	,0000	.0001	.0002	,0022	0041	0116	0383	0933	1495	1836	3075	4539	6047
8	0000	0000	0000	0000	0000	0000	.0000	.0000	.0000	.0000	.0003	0007	0024	0103	0315	0576	0753	1501	2586	3953
9	00000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	0001	0004	0022	0083	0174	0243	0583	1189	2120
10	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0003	0017	0040	0060	0175	0426	0898
11	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0002	0007	0011	0039	0114	0287
12	0000	0000	0000	.0000	.0000	0000	.0000	0000	.0000	.0000	.0000	0000	0000	00000	0000	1000	0001	0006	0022	0065
14	0000	0000	0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	0009
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0	1 000	1 000	1.000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000
1	1399	2614	3667	4579	5367	6047	663.3	7137	7570	7941	9126	9351	9648	9866	9953	9977	9984	9995	9999	1 000
3	0004	.0353	.0730	.1101	.1710	.2262	2832	3403	.3965	.4510	.6814	,7404	.8329	.9198	9847	9806	9858	9948	9983	9995
4	0000	00002	.0008	.0203	0362	.0571	0829	1130	1469	.1841	3958	.4678	.8020	7639 5387	.7031	9206 7908	9383	9729	9893 9576	9963 9824
5	0000	0000	.0001	.0002	.0006	.0014	.0028	.0050	.0082	0127	.0617	.0898	1642	3135	4845	5959	.6481	.7827	8796	9408
8.	0000	.0000	0000	.0000	.0001	.0001	0003	.0007	.0013	.0022	0168	0274	.0611	1484	.2784	3815	4357	596B	7392	.8491
7	0000	0000	0000	0000	.0000	.0000	0000	0007	.0002	.0003	.0036	0066	.0181	.0566	1311	2030	2452	3902	5478	6964
0	0000	0000	0000	0000	.0000	0000	.0000	0000	.0000	0000	0006	0013	.0042	.0173	0500	0887	1132	2131	3465	5000
9	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0002	0008	0042	0152	0308	0422	0950	1818	3036
10	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0008	0037	0085	0124	0338	0769	1509
11	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0007	0018	0028	0093	0255	0592
2	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0003	0003	0005	0019	0063	0176
3 4	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	00000	0001	0003	0011	0037
15	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0005
						0000	V	0000	5555		-	0000	0000		2000	0000	0000	0000	0000	
				1						7 =	16									
0	1 000	1 000	1 000	7 000	1 000	1 000	1 000	1 000	1 000	1 000		1 000	1 000	1 000	1 000	1 000		1 000		1 000
2	0109	2762	3857	1327	1892	6284 2489	6869 3098	7366 3201	7789 4289	8147	9257	7728	9719	9900	9967	9985	9990	9997	9999	1 000
3	0005	0037	0113	0242	0429	06.3	0969	1311	1604	4853	7161 4386	5132	8593 6482	9365	9739	9863 9406	9902 9549	9967	9990	9997
4	0000	0002	0011	BMG2	00.70	0132	0221	0342	0496	0684	2101	2709	4019	5950	7541	8341	8661	9349	8719	9894
5	0000	0000	0001	0003	0009	0019	0038	0068	0111	01.70	0791	134	2018	3698	5501	6609	7108	6334	9147	9618
6	0000	0000	.0000	0000	1000	0002	0005	0010	0019	0033	0235	0378	0817	1897	3402	4531	5100	6712	8024	8949
7	0000	0000	0000	0000	0000	0000	0001	0001	0003	0005	0056	0101	0267	0796	1753	2626	3119	4728	6340	7728
8	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0001	0011	0021	0070	0271	0744	1265	1694	2839	4371	5982
9	0000	0000	0000	0000	0000	0000	0000	1000	0000	0000	0002	0004	0015	0075	0257	0500	0871	1423	2559	4018
0	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0002	0016	0071	0159	0229	0583	1241	2272
1	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0003	0016	0040	0062	0191	0486	1051
3	0000	0000	0000.	0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0003	0008	0013	0049	0148	0384
4	0000	0000	.0000	0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0002	0009	0035	0106
16	0000	0000	0000	0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0003
6	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000
											42									
	1.000	1.000	1000	4.000		4 544		1.65			17									
1	1 000	1 000		1,000	1.000		7.000		1 000		1 000 n ten	1-000	1 000	1 000	1 000	1 000	1 000		1 000	
2		0446	4042	1465	5818	6507	7088	7577 3995	1088	8332 5 82	7375	9549	9775	9925 9499	9977	9990	9993	9998	9994	9999
3	0006	0044	0134	.0286	0503	0782	1 18	1503	1927	2382	4802	5565	6904	8363	9226	9668	9673	9877	9959	9988
4	0000	0003	0014	.0040	0088	0164	0273		0603	0826	2444	3113	4511	6470	7981	8696	8972	9536	9816	9936
5	0000	0000	0001	0004	0012	0026	0051	0089	0145	0221	0987	1396	2418	4261	613	7186	7652	B740	9404	9755
6	0000	0000	0000	0000	0001	0003	000?	0015	0027	0047	0319	0504	1057	2347	4032	5223	5803	7361	8529	9283
7	0000	0000	0000	0000	0000	0000	0001	0002	0004	8000	0083	0147	0377	1071	2248	3261	3812	5522	7098	B338
8	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0017	0035	.0109	0402	1046	1719	2128	3595	5257	6855
9	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0003	0007	.0026	0124	0403	D755	0994	1989	3374	5000
٥	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	.0005	0031	0127	0273	0383	0919	1834	3145
1	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	.0001	0006	0032	0080	0120	034B	0826	1662
2	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	.0000	0001	0007	0019	0030	0106	0301	0717
3	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0003	0006	0025	.0086	0245
4	0000	.0000	0000	0000	0000	0000	00000	00000	0000	0000,	0000	0000	.0000	0000	0000	0000	0001	0005	0019	0064
5	0000	0000	0000	0000	0000	0000	0000	0000	.0000	.0000	0000	0000	.0000	0000	0000	0000	0000	0001	0003	0012
and I	0000	0000	0000	0000	0000	0000	0000	0000	.0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0001
7	0000	0000	0000	TOTAL STREET	0000	0000	0000	0000	.0000	.0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000

Prob (X ≤ x)

p	.01	.02	.83	.04	.05	08	.07	.08	.00	10	15	- E	20	.26	.30	4	35	.40	.46	.50
_	-01	104		~~				.00				•								
A										0 =	_						2021	0001	0000	0000
0	B345	6951	5780	4796	3972	3283	2708	2229	1831	3002	1704	1352	0180 0811	0056	0126	0007	0004	0001	0000	0000
1 2	0130	2554	3217	3597	3763 1683	3772	3669 2348	34B9 2579	.3260	2835	2556	2299	1723	0958	0458	0253	0190	0069	0022	0006
3	0007	0048	0140	0283	0473	0697	0942	1196	1446	1680	2406	2452	2297	1704	1046	D690	0547	0246	0095	0031
4	0000	0004	00 6	0044	0093	0167	0266	0390	.0536	0.700	1592	1839	2153	2130	1681	1294	1104	0614	0291	0117
5	0000	0000	1,000	.0005	0014	0030	0056	0095	0148	0218	0.28.3	1030	1507	1988	2017	1812	1664	1146	0666	0327
6	0000	0000	0000	0000	0002	0004	0009	0018	0032	0057	0301	0446	0816	1436	1873	1963	1941	1655	1181	0708
7	0000	0000	0000	.0000	0000	0000	0001	0003	0005	0010	0091	0153	0350	0820	1376	1682	1792	1892	1657	1214
8	0000	0000	0000	0000	0000	0000	0000	0000	0001	0002	0022	0042	0120	0376	0811	1147	1327	1734	1864	1669
9	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0004	0000	0033	0134	0386	0643	0.794	1284	1694	1855
10	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0002	900B	D042	()149	028-	0385	0771	1248	1669
11	GOOD	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0010	0046	0 05	0.51	0374	0742	1214
32	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0003	0012	0031	0047	0145	0354	0708
13	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0002	0003	0012	0045	0134	0327
14	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0002	001	0039	0117
15	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000		D000							
16	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0006
17	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000
	10000	UUAU	·UUUU	·UUUU	0000	9000	0000	5000	0000	DOUG	0000	0000	0000	0000	5050	0000	VIII	Dobu	0000	
										n =	19						,			
0	8262	6212	5806	4604	3774	3086	2510	205	1666	34,1	0456	0313	0 44	0042	0011	0005	0003	0001	0000	0000
1	1588	2642	3294	3645	3274	3743	3602	3389	3131	2852	1529	1189	0685	0268	D003	0043	0029	ODOB	0002	0000
2	.0144	0485	0917	1367	287	2150	2440	2652	2787	2852	2428	2141	1540	0803	0358	0193	0 3B	0046	00 3	0003
3	8000	0056	0181	0323	0533	0778	104	130	1562	1796	2428	2426	2192	1517	0869	0546	0422	0175	0062	0018
4 5	0000	0005	0020	0054	01-2 001B	0199	0313	0456	0648	0298	1214	1941	1636	2023	1491	1639	1468	0933	0203	0222
										_										
6	0000	0000	0000	0001	0002	.0008	0012	0024	0042	0069	0374	0544	0955	1514	1916	1912	844	1451	0949	0518
7	0000	0000	0000	0000	0000	0001	0002	.0004	9000	0002	0122	0061	0443	0974	1525 0981	1332	1489	1797	1771	1442
9	0000	0000	0000	0000	0000	.0000	0000	1000	0000	0000	0007	0015	0051	0198	0514	0814	0980	464	1771	1762
10	0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	000	0003	0013	0066	0220	0407	0528	0976	1449	1762
11	0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0003	0018	0077	0166	0233	0532	0970	1442
12	0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0004	0022	0065	0083	0237	0529	0961
13	0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0001	0005	0015	0024	00R5	0233	0519
14	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0090	0000	0000	0000	0001	0003	0006	0024	0082	0222
15	0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0001	0005	0022	0074
18	0000	.0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	1000	0005	0018
17	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0003
18	0000	.0000	0000	0000	.0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000
18	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	000Q	0000	0000
										W-	20									
0	.8179	-6678	5438	4420	3585	2901	2342	1887	1516	1216	0389	0261	0 15	0032	0008	0003	0002	0000	0000	0000
1	1652	2725	3364	3683	3774	3703	3526	3282	3000	2702	1368	1043	O# 76	02 1	8300	0030	0020	0005	000	0000
2	.0169	.0528	.0968	1458	1887	2246	2521	2711	2818	2852	2293	1982	1369	0669	0278	0143	0.00	0031	8000	0002
3	.0010	.0065	.0183	0364	0596	0860	1139	1414	1627	1901	2428	2379	2054	1907	2304	0429	0321	0.23	0040	0046
4 5	0000	0006	.0024	0065 0009	0133	0233	0364	0523 Q145	0703	0898	1821	2022 1294	1746	1897	1789	45.7	272	0350 6746	0139	0148
														-						
6	0000	0000	0000	0001	0003	.0008	0017	0032	00\$5	0089	0460	064	1091	1686	1643	1800	1844	1244	1221	0370
3	0000	0000	0000	0000	0000	0001	0002	0005	0002	0020	0046	0084	0222	0609	1 44	460	1614	1797	1623	1201
9	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0011	0022	0074	02 1	0654	Dotto.	1 58	1597	177	1602
10	.0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0002	0005	0020	0099	030F	054+	5686	21	1593	1762
11	0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0001	0005	0030	0120	024	0.336	0,0	1185	1602
12	0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0001	ODOR	0039	0092	7 3h	0.155	0727	120
13	0000	0000	0000	0000	0,000	0000	0000	0000	0000	0000	0000	0000	0000	0002	(ID40	)(===	11 34 5	0146	0366	0739
14	0000	0000	0000	0000	0000		0000	0000	0000	0000	0000	0000	0000	0000	0007	000	5007	0049	0150	0370
15	0000	0000	0000	0000	0000	.0000	0000	000G	0000	0000	0000	0000	0000	0000	0000	001	5003	00 3	D049	Q148 D046
16	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	9000	900: 9000	7(X)() 7(X)()	0003	0002	0046
18	0000	0000	0000	0000	0000		0000	0000	0000	0000	0000	0000	0000	0000	DGHM	2005	0000	0000	0000	0005
19	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	3000	9000	0000	0000	0000	0000
20	0000	0000	0000	0000	0000	.0000	0000	0000	0000	7000	0000	COUL	0000	Wav	19/9/91	mis/cycl	9000	0000	0000	0000
-	-	.98	.97	.96	.96	.94	.83	.92	.91	.90	.85		.80	75	70	1	.65	60	.55	.60

The four charts on pages 12 and 13 are for use in binomial sampling experiments, both to find confidence intervals for p and to produce critical regions for the sample fraction f=X/n (see bottom of page 4 for notation) when testing a null hypothesis  $H_0$ .  $p=p_0$  The charts produce (a) confidence intervals having  $\gamma=90\%, 95\%, 98\%$  and 99% confidence levels, (b) one-sided critical regions (for alternative hypotheses  $H_1$  of the form  $p < p_0$  or  $p > p_0$ ) for tests with significance levels  $\alpha_1 = 5\%, 2\frac{1}{2}\%, 1\%$  and  $\frac{1}{2}\%$ , and (c) two-sided critical regions (for  $H_1$  of the form  $p \neq p_0$ )

for tests with significance levels  $\alpha_2 = 10\%$ , 5%, 2% and 1%. For confidence intervals, locate the sample fraction f on the horizontal axis, trace up to the two curves labelled with the appropriate sample size n, and read off the confidence limits on the vertical axis. For critical regions, locate the hypothesised value of p,  $p_0$ , on the vertical axis, trace across to the two curves labelled with the sample size n and read off critical values  $f_1$  and/or  $f_2$  on the horizontal axis. If  $f_1 < f_2$  the one-sided critical region for  $H_1: p < p_0$  is  $f \le f_1$ , or if  $H_1$  is  $p > p_0$  it is  $f \ge f_2$ . A two-sided critical

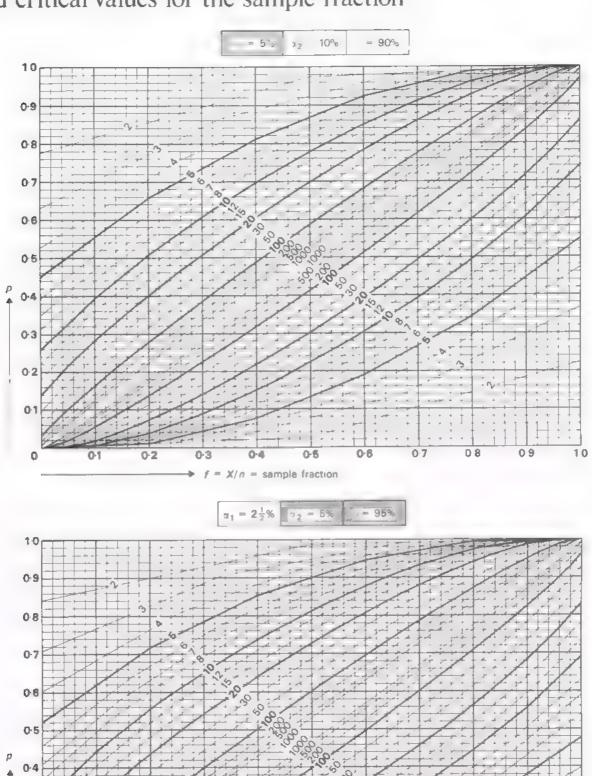
p	.01	.02	.03	.01	.05	.08	.07	.08	.09	10	16	4	.20	.25	.30	1	.35	.40	.45	.60	1
		- quint			100	- VIII	701	1000	1 .00			- 6		qual-	126			,40	.40	,00	4
A										49.7	- 10						1			_	-
0	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1.000		1 000	1.000	1 000	1.000	1 000	1.000	1.000	1.000	1 000	1 000	107
2	1655 0138	.3049	1003	1607	2265	.5717	7292 3622	.7771	8169	.8499	9464	9624	9820	9944	9984	9993	9996	9999	1 000	1 000	1
3	0007	.0052	Q157	.0333	.0581	.0896	1275	4281 1702	.4909	5497 .2662	.7759 5203	8272 5973	9009	.8605	9858	9932	9764	.9987 ,9918	9997	9999	1
4	.0000	.0004	0018	0050	.0109	.0201	0333	.0508	.0723	.0982	2798	3521	4990	6943	8354	.8983	9217	.9672	9880	9962	
5	0000	.0000	.0002	.0006	0015	.0034	,0067	.D176	D186	.0282	1206	1682	2836	.4813	6673	7689	8114	9058	9589	9846	1
6	0000	.0000	.0000	.0001	.0002	.0005	.0010	.0021	.0038	.0064	.0419	0653	1 129	2825	4656	58 ° B	6450	79-2	8923	9519	1
2	0000	.0000	.0000	0000	.0000	0000	.0001	.0003	.0006	.0012	.0118	.0206	.0513	1390	2*83	3915	4509	6257	7742	881	1
8	0000	,0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0027	,0053	,0163	0569	1407	2233	2717	4366	6085	7597	1
9	0000	0000	.0000	0000	0000	.0000	.0000	.0000	.0000	.0000	.0005	.0011	.0043	0193	0596	1076	1391	5935	4222	5921	Ш
10	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	0000	.0000	.0001	.0002	.0009	0054	0210	0433	0597	1347	2527	4073	Ш
11	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0002	0012	0061	0144	0212	0578	1280	2403	ш
12	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0002	0014	0039	0062	0203	0537	189	
4	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	E000	0009	0074	0048	0183	048	
15	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0002	0049	0154	
15	0000	0000	0000	0000	0000	0000	0000		-				-								-
7	0000	0000	0000	00000	1000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0007 0007	
8	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	
					1					_	_										_
										n =	10										
0	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1 000	1.000	1 000	1 000	1 000	1 000	35
3	1738	3188	4394	5396	6226	6914	7481	7949	8334	8649	9544	9687	9856	9958	9989	9995	9997	9999	1 000	1 000	1
2	.0153	0546	1 00	175	2453	3171	3879	4560	5202	5797	8015	8498	g171	9690	9996	9953	9969	9992	9998	1 000	\$
3	0009	0061	0183	0384	0665	1021	14 39	1908	2415	2946	5587	6351	7631	9887	9538	9760	9830	9945	9995	9996	16
4	0000	0005	0022	0061	0132	0243	0398	0602	0853	1 50	3159	3930	5449	1369	8668	9213	9409	9770	9923	9978	1
6	0000	0000	.0002	0007	0020	0044	0085	0147	0235	0352	1444	989	3267	5346	71.78	8121	B500	9304	9720	9904	1.
	0000	0000	.0000	0001	0002	0006	0014	.0029	0051	0086	0537	0824	1631	3355	5261	6481	7032	8371	9223	9682	t
?	0000	0000	.0000	0000	0000	0001	0002	0004	0009	0017	0163	0281	0676	1249	3345	4569	5188	6919	<b>8273</b>	9165	1
9	0000	0000	.0000	9000	0000	0000	0000	.0001	0001	0003	0041	0079	0233	0775	1920	2793	3344	5122	6831	8204	1
9	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0008	0018	0067	0287	0839	1462	1855	3325	5080	6767	1
-												-	0016	6800	0326	0648	0875	1861	3290	5000	
2	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	1000	0003	0023	0105	0241	0347	0885		3238	
3	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0005	0028	0074	0114	0352	0871	1796	
4	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0006	0019	0031	0031	0342	0835	
5	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0001	0006	0026	0096	
	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000								_	-
7	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0005	0022	1
8	0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	
9	0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	DODO	
											$\overline{}$										
_										A =	20										_
2	1 000	1 000	000	1.000	1 000	1 000	1.000	1-000	1 000	1.000	1 300	1 000	1 000	1 000	1 000	1 000	1 000	1.000	1 000	1 000	20
2	1821	3374	4562	5580	6415	7099	7658	8 13	8484	0.84	9612	9130	9886	9966	9992	9997		1-000	1 000	1-000	15
3	0169	0599	198	1897	2642	3395	4131	4831	5484	6083	8244	8606	0308	9751	9974	9961	9979	9995	9999	1 000	2.8
	0000	0071	0210	0439	0755	1150	7610	2121	2666	323	595	6213	1939	9087	9645	9874	9879	9964	9991	9998	17
5	0000	0000	0003	0010	0026	0290	0421	0706	0993	1330	3523 1702	4995 2313	5886 3704	7748 5852	8929 7625	9396 B485	9556 8818	984D 9490	9951	9987	36
-												-							9811	9941	52
	0000	0000	0000	0000	0000	0009	0019	0006	0968	0113	0673	0321	1958	3828	5836	7028	7546	8744	9447	9793	14
	0000	0000	0000	0000	0000	0000	0000	0006	0013	0004	0219	0371	D867	1018	3920	5207 3385	5834 3990	7500 5841	7480	9423	93
	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0013	0028	0100	0409	1133	1905	2376	4044	5857	483	1:
,	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0002	0006	0026	0139	0480	0919	1718	2447	4086	5881	11
ı	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	.0000	0001	0006	0039	0171						
1	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	.0000	0000	0000	0009	0051	0376	0532	0565	1308	4119 2517	
	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	.0000	0000	0000	0002	0013	0037	0060	0210	0580	1316	3
	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0003	0009	0015	0065	0214	0577	
	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0002	0003	0016	0064	0207	
	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0003	0015	0059	-
	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0003	0013	3
	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0002	
	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	1
Щ	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	7000	0000	000m	0000	0000	0
			.87	.96	.95	.94		-	.91			-				4		-	-	_	1 8

region appropriate for  $H_1\colon p\neq p_0$  is comprised of both of these one-sided regions. The 'curves' are in fact drawn as straight lines joining points corresponding to all n+1 possible values of f (this is seen most clearly for small n). Use of values of  $f_1$  and  $f_2$  which are in fact not reabsable values of f result in conservative critical regions, i.e. actual  $\alpha_1$  or  $\alpha_2$  values which are less than the nominal values.

EXAMPLES: With eight successes out of twenty, i.e. n=20, X=8 and f=8/20=0.4, the  $\gamma=95\%$  confidence interval for p is (0.19.0.64), using the second chart on

page 12. Using the same chart, suppose we wish to test  $H_0: p=0.6$ , again with n=20 We read off  $f_1=0.36$  and  $f_2=0.83$ . So  $f \le 0.36$  (i.e.  $X \le 7$ ) is the  $\alpha_1^L=2\frac{1}{2}\%$  critical region appropriate for  $H_1: p \le 0.6$ ,  $f \ge 0.83$  (i.e.  $X \ge 17$ ) is the  $\alpha_1^R=2\frac{1}{2}\%$  critical region appropriate for  $H_1: p \ge 0.6$ , and these two regions combined constitute the  $\alpha_2=5\%$  critical region appropriate for  $H_1: p \ne 0.6$   $\alpha_1^L$  and  $\alpha_1^R$  denote significance levels for the one-sided tests where  $H_1$  says that p is to the Left or Right respectively of  $p_0$ . The true significance levels here are in all cases slightly less than the nominal figures of  $2\frac{1}{2}\%$  or 5%

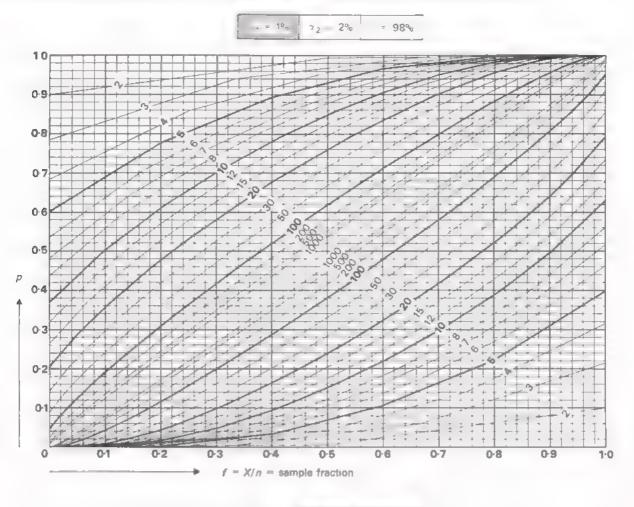
## Charts giving confidence intervals for pand critical values for the sample fraction

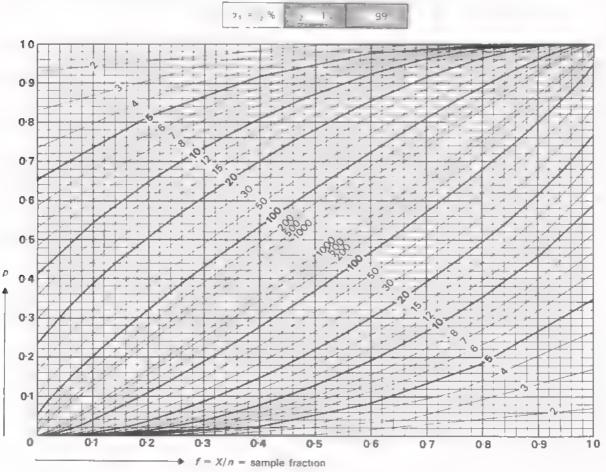


0.8 0.9 10 12 = X/n =sample fraction

0.3

0.2





For description, see pages 10 and 11.

## The Poisson distribution: individual probabilities

Prob 
$$(X = x) = e^{-\mu} \cdot \frac{\mu^x}{x!}$$
  $(x = 0, 1, 2, ...)$ 

Ш	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09	0.10	0.12	0.14	0 16	0.18	0.20	0.25	0.30	0.35
Г	9900	9802	9704	9608	9512	9418	9324	9231	9139	904B	8869	8694	8521	8353	8 87	7.788	7408	7047
ı	0099	0196	.0291	0384	0476	0565	0653	0738	0823	0905	1064	1217	1 1363	1503	1637	1947	2222	2466
ı	0000	.0002	0004	0008	0012	0017	0023	0030	0037	0045	0064	0085	0109	0135	0 64	0243	0333	0432
ı	0000	0000	.0000	0000	0000	0000	9001	0001	0001	0002	0003	0004	0006	0008	0011	0020	0033	0050
l	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0001	0003	0004
l	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	.0000	0000
и	0.40	0.45	0.50	0.56	0.60	0.65	0.70	0.76	0.80	0.85	0.90	0.96	1.00	1 10	1.20	1,30	1 40	1.50
٢	6703	6376	8065	5769	5488	5220	4966	4724	4493	4274	4065	3867	3679	3329	3012	2725	2466	2231
ı	2681	2869	3033	3173	3293	3193	3476	3543	3595	3633	3659	3674	3679	3662	3614	3543	3452	3347
ı	0536	0646	D758	0873	.0988	1103	1217	1329	1438	1544	1647	1745	1839	2014	2169	2303	2417	2510
ı	0072	.0097	.0126	0=60	0198	0339	0284	0332	0383	0437	.0494	0553	0613	0738	0867	0998	1128	1255
ı	0007	0011	0016	0022	.0030	0039	0050	0062	0077	0093	0111	0131	0153	0203	0260	D324	.0395	0471
ı	0001	0001	0002	0002	.0004	0005	0007	0009	0012	0016	0020	0025	0031	0045	0062	0084	0111	0141
H							+-			+			-	0000	0017	2010	DOOC	4000
1	0000	0000	0000	0000	.0000	0001	0001	1000	0002	.0002	0003	0004	0005	0008	0017	0018	0026	0035
1	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0003	0001	0001	0002	0003	0005	OODE
1	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	000	0001	0001
L	0000	0000	.0000	0000	.0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0000	0000	0000	0000
μ	1.80	1 70	1.60	1.90	2.00	2 10	2 20	2.30	2.40	2.50	2.60	2.70	2.60	2.90	3.00	3.10	3,20	3,30
Γ	20 9	1827	653	496	1353	225	1108	1063	0907	0821	0743	0672	0608	0560	0498	6450	340B	0369
L	3230	3106	2975	2842	2707	2577	2438	2306	2177	2062	1931	1815	1703	1596	1494	1397	1304	121
ı	2584	2640	2678	2.700	2707	2700	2681	2657	2613	2565	2510	2450	2384	2314	2240	2166	2087	2006
L	1378	1496	1607	1710	1804	1890	1966	2033	2090	2.38	2176	2205	2225	2237	2240	2237	2226	2209
ı	0551	.0636	0723	0812	0902	0992	1082	1169	1254	1336	1414	1488	1557	1622	1680	1733	1 78 1	182
L	0176	0216	0260	0309	0361	0417	0476	0538	0603	0668	0735	0804	0972	0940	1008	1075	1 40	1200
T	0047	.0061	0078	0098	0120	0146	0174	0206	0241	0278	0319	0362	0407	0455	0504	0555	0608	066
ı	.0011	0015	0070	0027	0034	0044	0055	0068	0083	0099	0118	0139	0163	0188	0216	0246	0278	(131)
ŀ	0002	0003	0005	0006	0009	0011	0015	0619	0025	0031	0038	0047	0057	0068	0081	0095	0.11	0179
ı	0000	0001	0001	0001	0002	0003	0004	0005	0002	0009	0011	0014	0018	0022	0027	0033	0040	004
ŀ	0000	0000	0000	0000	0000	0001	0001	0001	0002	0002	0003	0004	0005	0006	0008	00.00	DO1 3	0016
H				-						+			1	-		0000	0004	0000
ı	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0001	0001	0002	0002	0003	0004	0005
ŀ	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0001	0001	0001
Ł	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	00000	1 0000	0000	3000	0000	0000	0000
Ц	3.40	3.50	3.60	3.70	3.00	3.90	4.00	4.10	4.20	4 30	4.40	4.50	4 60	4.70	4,80	4 90	5.00	6,10
ı	0334	0302	0273	0247	0274	0202	0183	0166	0150	J136	0123	0111	0 31	0091	00R2	0074	0067	0061
1	1135	1057	0984	0915	0850	0789	0733	0619	0630	0583	0540	0500	0462	0427	0395	0365	D337	0311
1	929	1850	1771	692	1615	1539	1465	1393	1323	1254	1188	1175	1063	1005	0948	0894	0942	0793
ı	2186	2158	2125	2087	2046	2001	1954	1904	1862	1798	1743	1687	1631	1574	1517	1460	1404	1348
ı	1858	1888	1912	1931	1944	1951	1954	1951	1944	1933	1917	1898	1875	1849	1820	1789	1755	17 (
	1264	1322	1377	1429	1477	1922	1563	1600	1633	1662	1687	1 /48	1725	1738	1747	1753	1755	175
	0716	0771	0826	0881	0936	0989	1042	1093	1143	1101	1237	1281	1323	1 362	1398	1432	462	149(
ı	0348	0385	.0425	0466	0508	0551	0595	0640	0686	0732	0778	0824	0869	0914	0959	1002	1044	1088
ı	0148	0169	0191	0215	0241	0269	0298	0328	0360	0393	0428	0463	0600	0537	0575	0614	0653	0692
ı	0056	0066	0076	0089	0102	0 16	0 32	0150	0168	0188	0209	0232	0255	0281	030 2	0.334	0363	0393
1	0019	.0023	0028	0033	0039	0045	0053	0061	00.71	0081	0092	0104	n=18	0132	0141	0164	0181	0200
4	0006	0007	0009	0011	0013	0016	0019	0023	0027	0032	0037	0043	0049	005E	0064	0073	0082	009.
L	0002	0002	0003	0003	0004	0005	0006	0008	0009	0011	0013	0016	0019	0022	0026	0030	0034	0039
ı	0000	0001	1000	0001	0001	0002	0002	0002	0003	0004	0005	0006	0007	9000	0009	0011	00 3	00 5
	NAME AND ADDRESS OF	.0000	0000	0000	0000	0000	0002	0001	.0003	0001	0001	0002	D002	0003	0003	0004	0005	0000
	0000			44400	2000	2000	0.00											
	0000			00000	0000	0000	0000	0000	0000	1 00000	0000	0001	CUU	DOM	ThThT ,	DGG 1	UGUZ	0000
	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0001	0001	0000	0000	0002	000

The main uses of the Poisson distribution are as an approximation to binomial distributions having large n and small p (for notation see page 4) and as a description of the occurrence of random events over time (or other continua). Individual probabilities are given on pages 14–16 for a wide range of values of the mean  $\mu$ , and cumulative probabilities are obtained from the Poisson probability chart on page 17

EXAMPLES A production process is supposed to have a 1% rate of defectives. In a random sample of size eighty, what is the probability of there being (a) exactly two defectives, and (b) at least two defectives? The number X of defectives has a binomial distribution with n=80 and p=0.01, its mean  $\mu$  is  $np=80\times0.01=0.8$ . This distribution is well approximated by the Poisson distribution having the same mean,  $\mu=0.8$ . So immediately we find (a) Prob (X=2)=0.1438. For (b) Prob  $(X\ge2)$  we can

use the chart on page 17 directly. However this probability can also be found by noting that  $\text{Prob}(X \ge 2)$  1.  $-\text{Prob}(X \le 1) = 1 - \{\text{Prob}(X = 0) + \text{Prob}(X = 1)\} = 1 - \{0.4993 + 0.3595\} = 0.1912$ , using the above table.

A binomial distribution with large n and a p-value close to 1 may also be dealt with by means of a Poisson approximation if the problem is re-expressed in terms of a small p-value. For example if a treatment has a 90% (p=0.9) success-rate, what is the probability that exactly 95 out of 100 treated patients recover? This is the same as asking what is the probability that exactly 5 patients out of 100 fail to recover when the failure-rate is 10% or 0.1. That is we want Prob (X=5) in the binomial distribution with n=100 and p-0.1 which can be approximated by the Poisson distribution with mean  $\mu=np=100\times0.1=10.0$ . From page 15, this probability is found to be 0.0378

VE.								- 1	Prob									
	5.20	5.30	5.40	5.50	5.80	5.70	5.20	6.90	6,00	5.10	6.20	6.30	6.40	6.50	6.68	6.70	6,80	6.90
0	0055	0050	0045	0041	0037	.0033	0030	0027	.0025	0022	0020	0018	.001.7	00 5	0014	0012	0011	00°D
1	0287	.0265	0244	0225	0207	.0191	0176	0162	0149	0137	0126	01 6	0106	0098	0090	0082	0076	00 3C
3	293	1239	1186	06 B	0580 1082	1033	0509	0477	0446	0417	0390	0364	0340	0.3 %	0296 0652	0276	0258 0584	0240
1	1681	1641	1600	558	1515	1472	1428	1383	1339	1294	1249	205	1162	1118	1076	1034	0395	0952
5	1748	740	1728	1714	1697	1678	1656	1632	1606	1579	1549	5 9	1467	1454	1420	1385	1349	1314
3	1515	1537	1555	1521	1584	1594	1601	1605	1606	1605	1601	1595	1586	1575	1562	1546	1529	1511
7	0731	0771	1200	1234	261	1298	1326	1353	1377	1399	1418	1435	1450	1462	1472	4B0	1486	1489
9	0423	0454	0810	0849	0887	0925	0962	0998	1633	1066	0757	0.291	1160	1 188 0858	12 5 0891	0923	1263 0954	0985
1	0220	0241	0262	0285	0309	.0334	0359	0386	0413	3441	0469	0498	052B	0558	05BB	061B	0649	0679
	0104	0116	0 29	0143	0157	0173	0190	0207	0225	0744	0265	0285	0307	0330	0353	0377	0401	0426
П	0045	0051	0058	0065	0073	.0082	0092	0 02	.0113	0124	0137	0150	0164	0179	0194	02 0	0227	0245
	0018	0008	0024	0028	.0032	.0036	0041	0046	0052	.0058	0065	0073	0081	0089	0099	0108	01 9	0 30
	0002	0003	0003	0004	0005	.0006	0007	8000	0009	BELLEO	0012	0014	0016	0018	0020	0023	0026	0079
	0001	0001	0001	.000	0002	0002	0002	0003	0003	-0004	0005	9005	0906	0007	000B	0010	00 1	0013
ч	0000	.0000	0000	0000	1000	.0001	0001	0001	000	0001	0002	0002	0002	0003	0003	0004	0004	0005
	0000	0000	0000	0000	0000	.0000	0000	0000	0000	0000	0001	3001	0001	0001	0001	0001	0002	0002
	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	0000	9000	0000	0000	0000	0000	000	0000
_																		
4	7.00	7 10	7.20	7.30	7.40	7 50	7 60	7 70	7.80	7.90	8.00	8.10	8.20	6,30	8.40	6.50	6 60	8.70
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ı	0223	0208	0194	0180	0167	0156	0145	0134	0125	01 6	0107	0100	0092	0086	0079	0074	0068	0063
П	052	0492	0464	D438	0413	0389	0.066	0345	0324	0305	0286	0269	0252	0237	0222	0208	0195	0183
Ш	09 2	0874	0836	0799	0764	0220	0696	0663	0632	0602	0523	0544	05.7	0491	0466	0443	D420	0398
4	1277	241	204	1167	1130	1094	057	0.2	0986	0061	0916	9882	0849	0816	0784	0752	0722	0692
1	1490	1468	1486	1420	1394	1367	339 454	1442	782 478	1252	1396	1378	1 80	1 28	1097	1066	271	100 4
Ш	1304	1321	1337	1351	1363	1373	38	1388	1392	1395	1396	395	1392	1388	1387	376	366	1356
Ш	1074	-042	1070	1096	1121	-44	-167	1 :87	>207	1224	1241	256	1269	1280	1290	1299	1306	13:1
Ц	0710	0740	מנייון	0800	0829	0858	0887	0914	0941	0967	0993	10.	1040	1063	1084	1104	1123	1140
Ш	0457	0478	0504	0531	0548	0585	0613	0640	0687	1695	0722	0749	0776	0802	0828	0853	0878	0902
	0263	0.54	D303	0321	0 96	0366	0388	0243	0434	0278	0481	0505	0334	0555	0579	0604	0629	0654
Ш	0071	007B	0086	0095	0104	0 3	0.53	0 34	0145	0157	0 69	0182	0196	02+0	0225	0240	0256	0272
	0033	0037	004	0046	0051	005?	0062	0069	0075	0083	0090	8200	0102	0116	0126	0 36	0147	015R
Н	0014	0016	0019	0021	0024	0026	0030	0033	0037	0041	0045	0050	9055	0060	0066	0072	0079	D086
	0006	0007	0008	0009	0010	0005	0006	0015	0007	0000	0009	0024	0026	0014	0033	0036	0040	D044 D02
	0002	0001	0001	0001	0002	0005	0002	0003	0003	0003	0004	0006	0005	0006	0001	9008	0009	0011
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	0000	0000	0000	0000	0000	0000	0000	0000	0000	200	DOO	0001	0001	0001	0001	1000	0002	0007
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4	8.00	8.90	9.00	9.10	9.20	9.30	9.40	9.50	9.60	9.70	9.80	9.90	10.00	10.50	11 00	11 50	12 00	12.60
ı	0005	0001	0001	0001	0001	000	0001	0003	0001	000	0001	0001	0000	0000	0000	0000	9000	0000
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	0377	0357	0337	0319	0302		ALAA						0378	0393	0224			0095
	0377 0663	0635	0607	0581	0555	0530	0506	0483		0434	04.8	0398						
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	0377 0663 0972 1222 1344 1315 1157 0925 0679 .0459 0289 0169 0093 0048	0635 0941 1197 332 1377 1 72 0948 0703 0481 0306 0182 0701 0053 0026	0607 09 17 1318 1318 1318 186 0970 0728 0504 0324 0194 0109 0058 0029	0581 0881 1145 302 1317 1198 0991 0752 0526 0342 0208 0063 0032	0865 0851 1118 1286 1315 210 1012 0776 0549 0361 0221 0127 0089 0035	0530 0822 1091 1269 13 1 219 031 0799 0572 0380 0235 0137 .0075 .0039	1064 1251 1306 1228 1049 0822 0594 0399 0250 0147 0081	0764 1037 1232 1300 1236 1067 0844 0617 04 9 0265 0157	0736 1010 1212 1293 24 083 0866 0640 0439 0781 0168 0096	0709 0982 1191 1284 1245 098 0662 0459 0297 0180 .0103	0682 0956 1 70 1274 1249 1112 0908 0685 0479 0313 0192 ,0111	0656 0928 1148 1263 1250 1250 125 0 C7 0500 0330 .0204 .0119	0631 0901 1 26 125 126 1137 0948 0129 0521 0347 0217 .0128 J0071	05 3 0769 1009 177 1236 1180 1032 0834 0625 0438 0287 .0177	0646 0888 1095 1194 1194 1094 0926 0*28 0534 036* .0237 .0145	0325 0535 0769 0982 1 29 1181 1001 0822 9630 6463 0306 0 96	0755 0437 0655 0874 1048 1144 1056 0905 0724 0643 0383 0255	0353 0551 0765 0956 1087 1132 084 0972 0810 0633 0465 0323
	0377 0663 0972 1222 1344 1315 1157 0925 0679 0459 0289 0169 0093 0048 0024 0011 0006	0635 0941 1197 332 1377 1 72 0948 0703 0481 0306 0182 0101 0053 0026 .0012 .0005	0607 09 17 1318 1318 1318 186 0970 0728 0504 0324 0194 0109 0058 0029 0014 0006	0581 0881 1145 302 1317 1198 0991 0752 0526 0342 0208 0018 0063 0032 0015 0007	0565 0851 1118 1286 1315 210 1012 0776 0549 0361 0221 0127 0089 0035 0017 0008	0630 0822 1091 1269 13 1 219 031 0799 0572 0380 0235 0137 0076 0038 0019 0009	1293 1064 1251 1306 1228 1049 0822 0594 0399 0250 0250 0447 .0061 .0042	0764 1097 1212 1300 1236 1067 0844 0617 04 9 0265 0157 2008 ,0048 .0023 .0011	0736 1010 1212 1293 24 083 0866 0640 0439 0781 0168 .0096 .0051 .0026 .0012	0709 0982 1191 1284 1245 098 0888 0662 0459 0297 0180 .0103 .0066 .0026 .0014	0682 0956 1 70 1274 1249 1112 0908 0685 0479 0313 0192 ,0111 ,0080 ,0031 ,0015	0656 0928 1148 1263 1260 1250 1250 0 07 0500 0330 .0204 .0119 .0085 .0034 .0017	0631 0901 1 26 125 126 1137 0948 0°29 0521 0347 0217 0128 10071 10037 0019	05 3 0769 1009 177 1236 1180 1032 0834 0625 0438 0287 .0177 .0104 .0057 .0030	0646 0888 1095 1194 1194 1094 0926 0128 0534 0361 .0237 .0145 .0084 .0046	0325 0535 0769 0982 1 29 1181 1131 1001 0822 9630 0463 0306 0 96 0119 0068	0755 0437 0655 0874 1048 1144 1166 0905 0724 0543 0383 0255 0161 0097	0351 0551 0765 0956 1087 1132 084 0972 0810 0633 0465 0323 0211 0133
	0377 0663 0972 1222 1344 1315 1157 0925 0679 0459 0169 0093 0048 0024 0011 0002	0635 0941 1197 332 1377 1 -72 0948 0703 0481 0306 0182 0*01 0053 0026 .0012 .0002	0607 09 17 1318 1318 138 138 186 0970 0728 0504 0324 0194 0109 0058 0029 0014 .0006	0581 0881 1145 202 1317 1198 0991 0752 0526 0342 0208 0118 0063 0032 0015 0007	0565 0851 1118 1286 1215 210 1012 0776 0549 0361 0221 0127 0008 0035 0017 0008	0630 0822 1091 1269 13 1 219 031 0799 0572 0380 0235 0137 .0075 .0039 0019 0009	1293 1064 1251 1306 1228 1049 0822 0594 0399 0250 0250 0147 .0042 .0010	0764 1037 1212 1300 1236 1067 0844 0617 0419 0265 10157 10088 .0048 .0023 .0011	0736 1010 1212 1293 24 083 0866 0640 0439 0781 0168 0096 00012	0709 0982 1191 1284 1246 098 0888 0662 0459 0297 0180 .0103 .0066 .0026 .0014	0682 0956 1 70 1274 1249 1112 0908 0685 0479 0313 0192 .0111 .0060 .0031 .0015	0656 0928 1148 1263 1250 125 0928 0 07 0500 0330 0204 .0119 .0065 .0034 .0017	0631 0901 1 26 125 126 126 1137 0948 0129 0521 0347 0217 0128 J0071 0019	05 3 0769 1009 177 1236 1180 1032 0834 0625 0438 0287 .0177 .0104 .0057 .0030	0646 0888 1095 1194 1194 1094 0926 0128 0534 0361 .0237 .0145 .0084 .0046 .0024	0325 0535 0769 0982 1 29 1181 1100 0822 2630 0463 0306 0 96 0119 0068	0755 0437 0655 0874 1048 1144 1154 10905 0724 0543 0255 0161 0097	0353 0551 0765 0956 1087 1132 089 0972 0810 0633 0465 0323 0215 0133 0079
	0377 0663 0972 1222 1344 1315 1157 0925 0679 0489 0169 0093 0048 0024 0011 0006	0635 0941 1197 332 1377 1 72 0948 6703 0461 0306 0162 0101 0053 0026 .0012 .0005 .0002	0607 09 17 1318 1318 1318 0970 0728 0504 .0324 0194 0109 0058 0029 ,0014 .0006	0581 0881 1146 302 1317 1198 0991 0752 0526 0342 0208 0063 0032 0015 0007 0003	0565 0851 1118 1286 1315 210 1012 0776 0549 0361 0221 0127 0089 0035 0017 0008	0630 0822 1091 1269 13 1 219 031 0799 0572 0380 0235 0137 .0076 .0038 .0019 .0009 .0004 .0002 .0001	1093 1064 1251 1306 1228 1049 0822 0594 0399 0250 10147 10061 10042 10010 10004 10004	0764 1007 1232 1300 1236 1067 0844 0617 04 9 0265 0457 .0088 .0048 .0023 .0011	0736 1010 1212 1293 24 083 0866 0640 0439 0781 0168 .0096 .0051 .0026 .0012	0709 0982 1191 1284 1246 098 0888 0662 0459 0297 0180 .0103 .0066 .0028 .0014	0682 0956 1 70 1274 1249 1112 0908 0685 0429 0313 0192 .0181 .0080 .0031 .0007 .0003 .0003	0656 0928 1148 1263 1250 1250 1250 0 07 0500 0330 0204 .0119 .0085 .0034 .0017	0631 0901 1 26 125 126 126 1137 0948 0129 0521 0347 0217 0128 30071 9019	05 3 0769 1009 177 1236 1180 1032 0834 0625 0438 0287 .0177 .0104 .0057 .0030	0646 0888 1095 1194 1194 1094 0926 0128 0534 0361 .0237 .0145 .0084 .0046 .0024 .0012	0325 0535 0769 0982 1 29 1181 1100 0822 9630 0463 0306 0 96 0119 0068	0755 0437 0655 0874 1048 1144 1166 0905 0724 0543 0255 0161 0097 0055 0030 0016	0353 0551 0765 0956 1087 1132 089 0972 0810 0633 0465 0323 0215 0133
	0377 0663 0972 1222 1344 1315 1157 0925 0679 0459 0169 0093 0048 0024 0011 0002	0635 0941 1197 332 1377 1 -72 0948 0703 0481 0306 0182 0*01 0053 0026 .0012 .0002	0607 09 17 1318 1318 138 138 186 0970 0728 0504 0324 0194 0109 0058 0029 0014 .0006	0581 0881 1145 202 1317 1198 0991 0752 0526 0342 0208 0118 0063 0032 0015 0007	0565 0851 1118 1286 1215 210 1012 0776 0549 0361 0221 0127 0008 0035 0017 0008	0630 0822 1091 1269 13 1 219 031 0799 0572 0380 0235 0137 .0075 .0039 0019 0009	1293 1064 1251 1306 1228 1049 0822 0594 0399 0250 0250 0147 .0042 .0010	0764 1037 1212 1300 1236 1067 0844 0617 0419 0265 10157 10088 .0048 .0023 .0011	0736 1010 1212 1293 24 083 0866 0640 0439 0781 0168 0096 00012	0709 0982 1191 1284 1246 098 0888 0662 0459 0297 0180 .0103 .0066 .0026 .0014	0682 0956 1 70 1274 1249 1112 0908 0685 0479 0313 0192 .0111 .0060 .0031 .0015	0656 0928 1148 1263 1250 125 0928 0 07 0500 0330 0204 .0119 .0065 .0034 .0017	0631 0901 1 26 125 126 126 1137 0948 0129 0521 0347 0217 0128 J0071 0019	05 3 0769 1009 177 1236 1180 1032 0834 0625 0438 0287 .0177 .0104 .0057 .0030	0646 0888 1095 1194 1194 1094 0926 0128 0534 0361 .0237 .0145 .0084 .0046 .0024	0325 0535 0769 0982 1 29 1181 1100 0822 2630 0463 0306 0 96 0119 0068	0755 0437 0655 0874 1048 1144 1154 10905 0724 0543 0255 0161 0097	0353 0551 0765 0956 1087 1132 089 0972 0810 0633 0465 0323 0215 0133 0079
	0377 0663 0972 1222 1344 1315 1157 0925 0679 0459 0169 0093 0048 0024 0011 0006	0635 0941 1197 332 1377 1 72 0948 0703 0481 0306 0102 0053 0026 .0012 .0005 .0002 .0001 .0000 .0000	0607 09 17 1318 1318 1318 0970 0728 0504 0324 0194 0109 0058 0029 ,0014 .0006 .0003 .0001 .0000	0581 0881 1145 302 1117 1198 0991 0752 0526 0342 0208 0018 0063 0032 0015 0007	0555 0851 1718 1286 1315 210 1012 0776 0549 0361 0221 0427 0089 0035 0017 0008 0001 0000	0530 0822 1091 1269 13 1 219 031 0799 0572 0380 0235 00137 0009 0009 0004 0002 0001	1084 1251 1306 1228 1049 0822 0594 0399 0250 0214 00042 0001 0004 0004 0000	0764 1037 1232 1300 1236 1067 0844 0617 04 9 0265 0157 .0088 .0048 .0023 .0011 .0000	0736 1010 1212 1293 24 083 08640 0439 0781 0168 .0096 .0012 .0002 .0008 .0002 .0001	0709 0982 1191 1784 1245 098 0662 0459 0297 0180 .0103 .0065 .0026 .0014	0682 0956 1 70 1274 1249 1112 0908 0685 0479 0313 0192 .0111 .0080 .0031 .0015	0656 0928 1148 1263 1250 1250 1250 0 07 0500 0330 .0204 .0119 .0065 .0034 .0017 .0008 .0004 .0002	0631 0991 1 26 125 126 1137 0948 0129 0521 0347 0128 10071 10037 0019 0009 00004	05 3 0*69 1009 177 1236 1180 1032 0625 0438 0287 .0177 .0104 .0057 .0003 .0001	0646 0888 1095 1194 1194 1094 0926 0534 0361 .0237 .0145 .0084 .0046 .0024 .0006 .0003	0325 0535 0769 0982 1 29 1181 1131 1001 0872 2630 0463 0306 0 96 0119 0068	0755 0437 0655 0874 1048 1144 1166 0905 0724 0543 0383 0255 0161 0097 0055 0030 0016	0353 0551 0765 0956 1087 1132 0840 0972 0810 0633 0465 0221 0133 0070 0045 0024 0013
	0377 0663 0972 1222 1344 1315 1157 0925 0679 0489 0169 0093 0048 0024 0011 0002 0000 0000 0000	0635 0941 1197 332 1377 1 72 0948 0703 0481 0206 0102 0001 .0005 .0002 .0000 .0000 .0000	0607 09 17 1318 1318 1318 1318 0970 0728 0504 0324 0194 0194 0058 0029 ,0014 .0006 .0003 .0001 ,0000 ,0000	0581 0881 1146 302 1317 1198 0991 0752 0526 0342 0208 0063 0032 0015 0007 0000 0000 0000	0555 0851 1718 1286 1315 210 1012 0776 0549 0361 0221 0009 0035 0017 0000 0000 0000 0000	0530 0822 1091 1269 137 0799 0572 0380 0235 0035 0019 0009 0004 .0002 .0000 .0000 .0000	0793 1064 1251 1306 1228 1049 0822 0594 0399 0250 02147 0001 0001 0004 0002 0001 0000 0000	0764 1007 1232 1300 1236 1067 0844 0617 04 9 0265 0157 .0088 .0048 .0021 .0001 .0000 .0000	0736 1010 1212 1293 24 083 9866 0640 0439 0781 0168 .0096 .0001 .0002 .0008 .0002 .0000 .0000	0709 0982 1191 1284 1246 098 0888 0662 0459 0297 0180 .0103 .0065 .0028 .0014 .0006 .0003	0682 0956 1 70 1274 1249 1112 0908 0685 0429 0313 0192 .0111 .0000 .0031 .0007 .0003 .0001 .0000	0656 0928 1148 1263 1260 1250 1250 0928 0 C7 0500 0330 .0204 .0119 .0065 .0034 .0017 .0008 .0004 .0002 .0001	0631 0901 1 26 125 126 126 1137 0948 0129 0521 0347 0217 0128 J0071 J0031 0009 0004 0002 9001	05 3 0769 1009 177 1236 1180 1032 0625 0438 0287 .0177 .0104 .0052 .0007 .0003 .0001	0646 0888 1095 1194 1194 1094 0926 0728 0534 0367 8237 ,0145 ,0046 ,0046 ,0046 ,0003 ,0001	0325 0535 0769 0982 1 29 1181 1191 1001 0822 9630 0463 0306 0 96 0119 0068 0005 0005	0755 0437 0655 0874 1048 1144 1166 0905 0724 0643 0283 0255 0161 0097 0055 0030 0016 0008 0004	0353 0551 0765 0956 1087 1137 088 0972 0810 0633 0465 0323 0213 0133 0079 0045 0024 0013 0006

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1	0027	.0019	00 3	0009	0006	0003	0001	000)	0000	0000	0000	0000	0000	0000	3000	0000	ODOD	0000	ш
L	0070	0051	0037	0027	0019	0010	0005	0002	0001	0001	0000	0000	0000	0000	0000	0000	0000	0000	Ш
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ı	028	0222	0174	0135	0104	0060	0034	0019	00-0	0005	0003	.0001	0.00	0000	0000	0000	0000	0000	ш
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L	0859	0760	.0663	.0571	.0486	.0341	.0230	.0150	.0096	.D058	,0036	.0020	.0012	.0007	.0004	,0000	.0000	,000Q,	H
Æ	10 5	.0932	.0844	.0753	.0663	.0496	.0356	.0245	.0164	.0106	.0067	,0041	.0024	.0014	8000.	.0000	.0000	,0000	
ı	1099	1049	.0984	,0910	.0829	.0661	.0504	.0368	.0259	.0176	.0116	.0075	.0047	.0029	.0017	.0001	.0000	.0000	
ı	1089	→OB9	1060	.1014	.0958	.0814	.0658	.0509	.0378	.0271	.0168	.0127	.0083	,0053	Ø033	.0002	.0000	,0000	
Л	1021	1050	1060	1061	1024	.0930	,0800	.0655	.0514	.0387	.0282	.0199	.0136	1900.	.0059	.0005	.0000	,0000	1
Ц	0885	0945	.0989	1018	1024	,0992	.0906	.0786	.0650	.0516	.0395	.0292	.0209	.0146	,0099	.0010	.0000	.0000	H
	.0719	.D798	.0866	.0920	.0990.	.0992	.0963	.0884	.0772	0645	.0518	.0401	.0301	.0219	.0156	.0019	,0000	.0000	
ı	.0550	.0833	.0713	.0785	.0847	,0934	.0963	.0936	.0863	.0780	.0640	.0520	.0407	,0309	.0227	.0034	.0000	,0000	
I	.0397	.0475	.0554	.0632	.0706	.0830	9090,	.0936	,0911	.0844	.0747	.0635	.0520	.0412	.0316	.0057	.0000	,0000	
I	.0272	.0337	,0409	.0483	.0557	.0699	.0814	.0887	.0911	.0688	.0826	.0735	,0629	.0520	,0415	.0089	.0001	.0000	ш
Ц	.0177	.0228	.0286	.0350	.0418	.0559	.0692	.0798	.0866	.0888	.0867	.0609	.0724	.0624	.0519	.0134	.0002	,0000	Ш
П	.0109	.0148	.0191	.0242	.0299	.0426	.0560	.0684	.0763	.0848	.0867	.0847	.0793	.0713	,0618	.0192	.0004	.0000	Ш
I	.0085	,0090	.0121	.0158	.0204	.0310	,0433	,0560	,0676	.0769	.0828	.0847	.0829	.0778	.0702	.0261	,0007	,0000	Ш
ı	0037	.0063	.0074	.0100	.0133	,0216	.0320	.0438	.0559	.0689	.0756	.0810	.0829	.0812	.0763	.0341	.0012	.0000	Ш
11	.0020	.0030	.0043	.0061	.0083	,0144	.0226	.0328	.0442	.0557	.0681	.0743	.0794	.0812	.0795	.0428	.0019	.0000	Ш
lì	0010	.0016	.0024	.0035	.0050	.0092	.0164	.0237	.0336	0448	.0555	.0654	.0731	.0779	,0795	-0511	.0031	.0000	Ш
I	.0005	.0008	.0013	.0020	.0029	.0057	.0101	.0164	.0246	.0343	.0449	.0563	.0646	,0719	,0786	.0590	.0047	,0001	1
1	0002	.0004	.0007	.0011	.0016	.0034	.0063	.0109	.0173	.0254	.0349	.0451	.0551	.0839	.0708	.0855	.0070	.0001	
ı	.0001	.0002	,0003	.0006	0009	.0019	.0038	.0070	,0117	,0181	.0262	.0354	.0452	.0548	.0632	.0702	.0100	.0002	Ш
ı	.0001	.0001	.0002	.0003	,0004	,0011	.0023	.0044	.0077	.0125	.0190	.0269	.0359	.0453	.0545	.0726	.0138	.0004	
U	.0000	.0000	.0001	.0001	.0002	.0006	.0013	.0026	.0049	10083	.0133	.0197	.0275	.0363	.0464	.0726	.0185	.0007	Ш
1	.0000	.0000	,0000	.0001	.0001	.0003	.0007	.0015	.0030	.0054	.0090	.0140	.0204	.0281	,0368	.0703	.0238	.0011	
ı	.0000	.0000	.0000	.0000	.0001	.0001	.0004	.0000	.0018	.0034	.0059	9600	.0147	.0211	,0268	,0659	.0298	.0017	111
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	-														фор	0,001	0139	0552	

The Poisson probability chart on page 17 gives cumulative probabilities of the form  $\operatorname{Prob}(X \ge x)$  where X has a Poisson distribution with mean  $\mu$  in the range  $0.01 \le \mu \le 100$ . To find such a probability, locate the appropriate value of  $\mu$  on the right-hand vertical axis, trace back along the horizontal to the line or curve labelled with the desired value of x, and read off the probability on the horizontal axis. The horizontal scale is designed to give most accuracy in the tails of the distribution, i.e. where the probabilities are close to 0 or 1, and the vertical scale has been devised to make the curves almost linear

EXAMPLES. A production process is supposed to have a 1% rate of defectives. In a random sample of size eighty, what is the probability of there being at least two defectives? This question has already been answered on p. 14 using individual probabilities. Here we may read off the probability directly, following the above directions with  $\mu=0.8$  and x=2, giving Prob  $(X \ge 2)=0.19$ . Obviously, accuracy may be somewhat limited when using the chart.

Probabilities of events such as  $X \le 2$  can also be easily found. For Prob  $(X \le 2) = 1 - \text{Prob}(X \ge 3)$ , and Prob  $(X \ge 3)$  is seen to be just less than 0.05, say 0.048, giving Prob  $(X \le 2) - 1 - 0.048 = 0.952$ 

As a final example, suppose the number X of serious road accidents per week in a certain region has a Poisson distribution with mean  $\mu=2.0$  What is the probability of there being no more than three accidents in a particular week? This again can be calculated using either individual probabilities or the chart. From page 14, the probabilities of 0, 1, 2 or 3 accidents are respectively 0.1353, 0.2707, 0.2707 and 0.1804, and adding these we have  $\text{Prob}(X \leq 3) = 0.8571$ . Using the chart, since  $\text{Prob}(X \leq 3) = 1 - \text{Prob}(X \geq 4)$ , we obtain  $\text{Prob}(X \leq 3) = 1 - 0.14 = 0.86$ 

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0000	0000	0000	00 ×	67
0000	0000	0000	0026	68
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0000	0000	0000	0014	70
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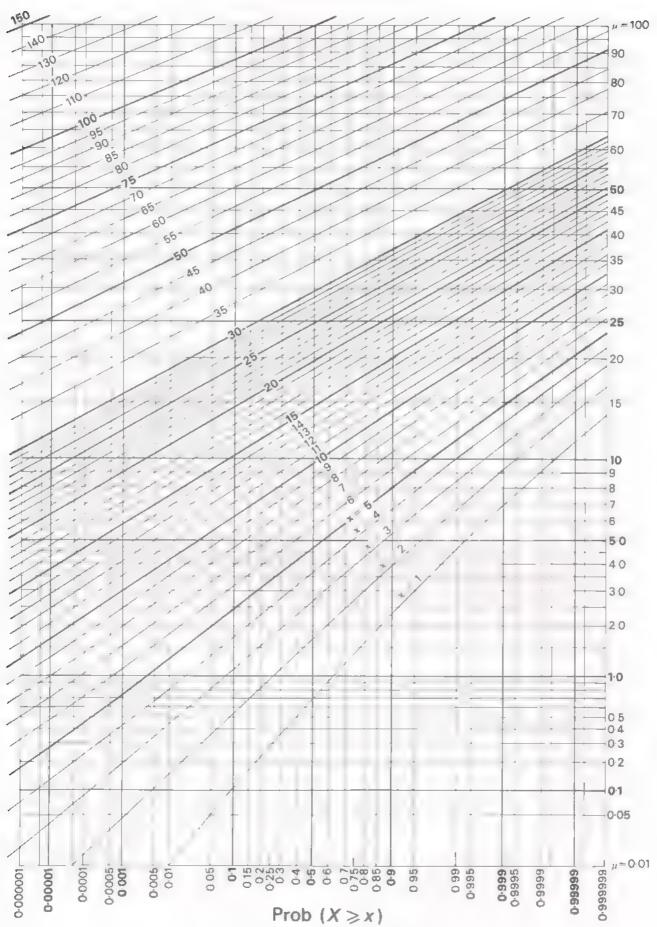
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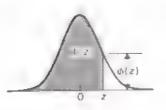
## Poisson probability chart (cumulative probabilities)

Prob 
$$(X \geqslant x) = \sum_{r=x}^{\infty} e^{-\mu_r} \frac{\mu^r}{r!}$$



## Probabilities and ordinates in the normal distribution

$$\phi(z) = \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}z^2}; \quad \Phi(z) = \text{Prob}(Z \le z) = \int_{-\infty}^{z} \phi(t) dt$$



50 59 5.8 5.7 5.6 5.5 5.3 5.2 5.1 5.0 4.8 4.7 4.6 4.5 4.4 4.1 4.2 4.1	0.0°987 0 0°182 0 0°332 0 0°332 0 0°199 0 0.0°190 0 0°333 0 0°578 0 0°996 0 0°170 0 0°479 0 0°479 0 0°479 0 0°540 0 0°340 0 0°340 0 0°586 0 0°133 0 0°586	0"928 0"171 0"392 0"565 0 101 0 179 0"2315 0 548 0"944 0"612 0"755 0"755 0"124 0"201 0"324 0"517 0"517	0°672 0°161 6°294 0°533 0°955 0°169 0°298 0°53 0°53 0°433 0°718 0°110 0°192 0°494	0°820 0°161 0°277 0°502 0°901 0°60 0°282 0°491 0 848 0°145 0°245 0°6112 0°583 0°112 0°283	0° 771 0° 143 0° 261 0° 473 0° 850 0° 161 0° 266 0° 465 0° 465 0° 433 0° 137 0° 233 0° 233 0° 301 0° 649 0° 649	0*724 0*134 0*246 0*446 0*802 0 143 0*252 0*440 0 760 0*130 0*271 0*371	07681 07126 07231 07421 07757 0 135 07238 0 416 0 720 06123 06210 06382	0°640 0°119 0°218 0°396 0°114 0°127 0°226 0°394 0°682 0°117 0°199	0°60: 0°112 0°206 0°374 0°673 0 120 0°213 0°372 0 646 0°111	0 565 0' 105 0' 193 0' 362 0' 635 0 114 0 201 0' 352 0 612 0" 105 0* 179	th	0 <sup>8</sup> 1	0.0	person ndica 18182 83	tes a	0 00 0 0 0	0 000 15er (	of ze	ras.
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57 58 55 53 52 51 50 48 47 48 47 48 47 48 47 48 41 42 41	0.0°599 0.0°190 0.0°130 0.0°333 0 0 579 0 0 996 0 0°170 0.0°479 0 0°793 0 0°130 0 0°211 0 0°541 0 0.0°541 0 0.0°543 0 0.0°133 0 0.0°133 0 0.0°133	0 <sup>4</sup> 565 0 101 0 179 0 <sup>7</sup> 315 0 548 0 <sup>9</sup> 944 0 <sup>6</sup> 61 0 <sup>6</sup> 272 0 <sup>4</sup> 456 0 <sup>6</sup> 765 0 <sup>5</sup> 124 0 <sup>7</sup> 201 0 <sup>8</sup> 324 0 <sup>1</sup> 517 0 <sup>5</sup> 816	0*533 0*955 0 169 0*519 0 895 0*53 0*256 0*433 0*718 0*118 0*192 0*300	0°502 0°901 0°160 0°262 0°491 0°848 0°145 0°245 0°411 0°683 0°112 0°183	0°473 0°850 0°.51 0°268 0.465 0.803 0°137 0°233 0°301 0°649 0°107	0*446 0*802 0 143 0*252 0*440 0 760 0*130 0*221 0*371 0*617	0° 421 0° 757 0 135 0° 238 0 416 0 720 0° 123 0° 210 0° 352	0° 396 6° 714 0 127 0°226 0°394 0 682 0°117 0°199	0°374 0°673 0°120 0°213 0°372 0°646 0°111	0° 362 0° 635 0° 114 0° 201 0° 352 0° 612 0° 105	th	0 <sup>8</sup> 1	0.0	ndica 182	tes a	0 00 0 0 0	0 000 15er (	of ze	ras.
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50 49 48 47 46 45 44 41 42 41	0.0°287 0.0°479 0.0°793 0.0°130 0.0°211 0.0°340 0.0°541 0.0°854 0.0°133 0.0°207	0°272 0°456 0°755 0°124 0°201 0°324 0°517 0°517	0 <sup>4</sup> 258 0 <sup>4</sup> 433 0 <sup>6</sup> 718 0 <sup>5</sup> 118 0 <sup>2</sup> 192 0 <sup>3</sup> 309 0 <sup>3</sup> 494	0°245 0°411 0°683 0°112 0°183	0 <sup>4</sup> 233 0 <sup>4</sup> 301 0 <sup>4</sup> 649 0 <sup>5</sup> 107	0° 221 0° 371 0° 617	0° 210	Q <sup>6</sup> 199	0° 189										
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4 8 4 7 4 8 4 5 4 4 4 3 4 2 4 1 4 0	0 0 <sup>6</sup> 793 0 0 <sup>1</sup> 130 0 0 <sup>1</sup> 211 0 0 <sup>1</sup> 340 0.0 <sup>1</sup> 541 0.0 <sup>1</sup> 854 0.0 <sup>1</sup> 133 0.0 <sup>4</sup> 207	0 <sup>5</sup> 124 0 <sup>5</sup> 201 0 <sup>5</sup> 324 0 <sup>5</sup> 517 0 <sup>5</sup> 816	0 <sup>5</sup> 118 0 <sup>4</sup> 192 0 <sup>3</sup> 309	Q <sup>5</sup> 112 Q <sup>5</sup> 183	0° 107		04 587		01318	0°302									
46 45 44 43 42 41	0.0°211 0.0°340 0.0°541 0.0°854 0.0°133 0.0°207	0 <sup>5</sup> 201 0 <sup>5</sup> 324 0 <sup>5</sup> 517 0 <sup>5</sup> 816	0 <sup>4</sup> 192 0 <sup>3</sup> 309 0 <sup>5</sup> 494	0*183		05102		01568	0*530	0°504									
45 44 43 42 41 40	0.0 <sup>4</sup> 541 0.0 <sup>3</sup> 854 0.0 <sup>4</sup> 133 0.0 <sup>4</sup> 207	0 <sup>1</sup> 324 0 <sup>1</sup> 517 0 <sup>5</sup> 816	0° 309		- 0° 174		0° 968	0 921	0° 876 0° 143	0°834 0°137									
44 43 42 41 40	0.0 <sup>4</sup> 541 0.0 <sup>3</sup> 854 0.0 <sup>4</sup> 133 0.0 <sup>4</sup> 207	0 <sup>5</sup> 517 0 <sup>5</sup> 816	0*494	0.560	01281	0 <sup>5</sup> 166 0 <sup>5</sup> 268	05 158 05 258	0 <sup>4</sup> 151 0 <sup>4</sup> 244	0, 143	0,255		D.		tions	Low	rte h	owa r	ot h	ееп
4 3 4 2 4 1 4 0	0.0 <sup>3</sup> 854 0.0 <sup>4</sup> 133 0.0 <sup>4</sup> 207	D <sup>5</sup> B 1 6		and a sec		01429	01410	01391	0 <sup>1</sup> 373	01356	ei	ven	iñ iñ	this	regi	on	becat	se 1	hey
4 2 4 1 4.0	0.0 <sup>4</sup> 133 0.0 <sup>4</sup> 207			0 <sup>3</sup> 471 0 <sup>3</sup> 748	0°450 0°712	01881	0*850	Q1621	0,213	D <sup>3</sup> 587				t be					
41	0.04207		0" 122	01117	04112	04 107	0 <sup>4</sup> 102	01977	05934	0,883									
		04196	01189	04 181	0"174	0° 168	04159	0, 125	0 <sup>4</sup> 146	0"139									
	0.01317	0*304	01291	01279	01267	0° 258	0,342	0*235	0*225	0*216									
3.9	0.04481	0*461	04443	01475	0*407	04 391	04375	01359	0*345	01 330									
3.8	0.04723	0*695	0*687																
						1													
							0 185	0,138	01172	0166				st	BTRA	LCT			-
			-				0,270	Q <sup>3</sup> 260	01251	01242			PR				RT\$		
		0 466	01450	0 434	0 419	0 404	0 190	0 376	0 362	0 349	_	_			_			-	
32	0.0 687	0 664	01641	0,618	0 598	0 577	0 557	0 538	0,216	0,20	1	2	3	4	5	G	7	8	9
31	0.0 968	0 935	0 904	0'874	0'845	0,819					^	1	, [	2	2	2	3	3	3
3.0	0.00135	00131	00126	00122							-	_	-		_	-			5
2.9	0.00187	00 B1	00175	00169							1		- 1			4	5	6	6
										00264	+	2	3	4	5	6	6	2	8
				00427	00415	00402	00391	00379	0036B	00357	1	2	4	5	6	7	8	10	11
25	0.00621	00604	00587	00570	00554	00539	00523	00508	00494	00480	2	3	-			-			14
24	0 00820	00798	00776	00755	00734	007-4	00695	00676	00657	00639	2	4		8					18
2.3	0 0107	0104	0102	0099									7	1		2		3	3
_										0143	Q	1	4	2	2	2	3	3	4
					0207	0202	0197	0192	0188	01A3	0	1	1	2	2	3	3	4	4
	-				0282	0256	0250	0244	0239	2233	1	1	- 2	2	3	4	4	5	5
_		0351	0344	0336	0329	0322	0314	0307	0301	D294	1	1	2	3	4	4	5		6
1.7	0 0446	0436	0427	0418	0409	0401	0392	0384	0375	0367	١.					-			B 9
16	0.0548	0537	0526	0518	0505						1	-				2		10	11
15	0.0668	0655	0643			-		_			٠,	_	-		_	В		11	13
1.4	0.0808	0793	0778								1		5	6	8	to	11	13	14
									1003	0985	2	4	5	7	미	11	13	15	16
	4		1314	1792	1271	1251	1230	1210	1190	1170	2	4	6	В	10	12	14	16	19
10	0 1587	1562	1539	1515	1492	1469	1446	1423	140	1379	2	5	1	ģ	12	14	16	181	21
0.9	0 1841	1814	1768	1762	1736	1211	1685	1660	1635	1617	3	5	B	10	13	15	18	20	23
-0 B	0.2119	2090	2061	2033	2005	1977	1949	1922	894										25
0.7	D 2420	2389	2358	2327														26	29
0.6										2776	4	7	10	14	1.7	21	24	27	31
-						_				3121	4	Ŷ	1	14	18	22	25	29	32
_						1			3520	34EJ	4	В	1 1	15	19	22	26	30	34
					4052	4013	3974	3936	3891	3859	4	8	12	15	19	23	27	31	35
0.1	0 4602	4562	4522	4483	4443	4404	4354	4325	4296		1			1					36 36
0.0	0 5000	4950	4920	4880	4840	4801			_				_		_				9
Z	0	1	2	3	4	5	6	. 7	8	9		2	3	-	D	9			
	3.7 -3.0 3.5 2.6 3.3 3.2 3.1 3.0 2.8 2.7 2.8 2.5 2.4 2.3 2.2 2.1 2.0 1.9 1.8 1.7 1.6 1.5 1.4 1.3 1.7 1.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0	3.8	3.8 0 0 ° 723 0 ° 695 3.7 0 0 ° 108 0 104 -3.0 0 0 ° 136 0 0 104 -3.0 0 0 ° 136 0 0 ° 163 3.5 0 0 2 ° 23 0 ° 224 3.3 0 0 483 0 ° 466 3.2 0 6 687 0 664 3.1 0 968 0 935 3.0 0 00187 0 0 61 2.8 0 0026 00248 2.7 0 00347 00347 2.8 0 00466 00463 2.5 0 00621 00604 2.4 0 00620 00798 2.3 0 0107 0104 2.2 0 0139 0 ° 136 2.1 0 0179 0 ° 104 2.2 0 0187 0 0 ° 124 2.0 0 0278 0 0272 1.9 0 0287 0 0281 1.8 0 0359 0 0351 1.7 0 0446 0 0436 1.6 0 0548 0 055 1.4 0 0808 0 ° 93 1.3 0 0968 0 951 1.2 0 ° 1151 1 131 1.1 0 ° 357 1 335 1.0 0 ° 1587 1 562 0.9 0 1841 1814 0.8 0 2 ° 119 2 0 90 0.7 0 2 ° 420 2 389 0.5 0 3085 3050 0.4 0 3446 3409 0.5 0 3082 3783 0.2 0 ° 4207 4 168 0.1 0 6602 4562 0.0 0 5000 4960	3.8  0 04723 04695 04687 3.7  0 01108 0 104 0496 -3.0  0.01160 03183 03147 3.6  0 0233 07224 0 216 3.3  0 0483 0466 0450 3.2  0 687 0664 0643 3.1  0 0968 0 935 0 904 3.0  00135 00131 00126 2.9  0 00187 00 81 00126 2.8  0 00266 00248 00240 2.7  0 00347 00336 00326 2.6  0 00466 00463 0040 2.5  0 00627 00604 00587 2.4  0 00820 00798 00776 2.3  0 0107 0104 0102 2.2  0 0139 0136 0132 2.1  0 0179 0124 0170 2.2  0 0139 0136 0132 2.1  0 0179 0124 0170 2.0  0028 0227 0217 3.9  0.0287 0281 0274 3.8  0 0368 0655 0643 3.7  0.0688 0655 0643 3.8  0.0688 0655 0643 3.9  0.0688 0655 0643 3.0  0.0688 0655 0643 3.0  0.0688 0655 0643 3.1  0.0688 0655 0643 3.1  0.0688 0655 0643 3.2  0.151 1131 1112 3.3  0.151 1131 1112 3.3  0.151 1131 1112 3.3  0.151 1131 1112 3.3  0.1567 1562 1539 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.0  0.1841 1814 1788 3.1  0.1867 1562 1539 3.1  0.1841 1814 1788 3.1  0.1867 1562 1539 3.1  0.1841 1814 1788 3.1  0.1867 1562 1539 3.1  0.1841 1814 1788 3.1  0.1867 1562 1539 3.1  0.1841 1814 1788 3.1  0.1867 1562 1539 3.1  0.1841 1814 1788 3.1  0.1867 1562 1539 3.1  0.1841 1814 1788 3.1  0.1867 1562 1539 3.1  0.1841 1814 1788 3.1  0.1867 1562 1539 3.1  0.1841 1814 1788 3.1  0.1867 1562 1539 3.1  0.1841 1814 1788 3.1  0.1867 1562 1539 3.1  0.1841 1814 1788 3.1  0.1867 1562 1539 3.1  0.1841 1814 1788 3.1  0.1867 1562 1539 3.1  0.1841 1814 1814 1814 1814 1814 1814 1814	3.8  0 0°723 0°695 0°687 0°641 3.7  0 0°108 0 104 0°996 0°957 -3.0 0.0°158 0°153 0°147 0°142 3.5  0 0 233 0°224 0 216 0°208 3.4  0 0 883 0°466 0°450 0 434 3.2  0 687 0°664 0°640 0°618 3.1  0 0 968 0 935 0 904 0°874 3.0  0 00187 0 681 00125 00169 2.8  0 00256 00248 00240 00232 2.7  0 00347 00336 00326 00317 2.8  0 00466 00453 00440 00427 2.8  0 0066 00453 00440 00427 2.8  0 0066 00453 0040 00587 2.8  0 0066 00453 0040 00587 2.8  0 0066 00453 0040 00587 2.8  0 00466 00453 0040 00587 2.8  0 00466 00453 0040 00587 2.8  0 00466 00453 0040 00587 2.8  0 00466 00453 0040 00587 2.8  0 00466 00453 0040 00587 2.8  0 00466 00453 0040 00587 2.9  0 00820 00798 00776 00755 2.1  0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	3.8	3.8  0 0°723 0°695 0°687 0°641 0°615 0°591 3.7  0 0°108 0 104 0°996 0°957 0°920 0°884 -3.0 0.0°169 0°183 0°147 0°142 0°335 0°131 3.6  0 0 233 0°224 0 216 0°208 0°200 0 193 3.6  0 0 483 0°466 0°450 0 434 0 419 0 404 3.2  0 0 687 0 664 0°641 0°618 0 598 0 577 3.1  0 0 988 0 935 0 904 0°874 0°845 0°616 3.0  0 00187 0 061 00122 00118 00114 2.9  0 00187 0 061 00125 00169 00164 00169 2.8  0 00266 00248 00240 00233 00226 00219 2.8  0 00466 00463 00440 00427 00415 00402 2.8  0 00466 00463 00440 00427 00415 00402 2.8  0 00466 00463 00440 00427 00415 00402 2.8  0 00026 00248 00240 00233 00226 00719 2.8  0 00466 00463 00440 00427 00415 00402 2.8  0 00267 00604 00587 00570 00554 00539 2.1  0 0019 0°16 0012 0012 00159 00164 2.2  0 0092 00798 00776 00755 00734 00744 2.3  0 0°07 0°04 0°02 0099 0096 0094 2.2  0 0°09 0°16 0°12 0°12 0°12 0°15 0°12 2.0  0 0228 0222 0217 0°212 0029 0096 3.0 0028 0°227 00217 0°10 0°166 0°162 0°158 3.0 00868 0655 0643 0630 0618 0769 3.0 00868 0655 0643 0630 0618 0769 3.0 00868 0655 0643 0630 0618 0606 3.0 00868 0655 0643 0630 0618 0769 3.0 00868 0655 0643 0630 0618 0606 3.0 00868 0655 0643 0630 0618 0606 3.0 00868 0655 0643 0630 0618 0606 3.0 00868 0655 0643 0630 0618 0606 3.0 00868 0655 0643 0630 0618 0606 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0749 0735 3.0 00868 0793 0788 0784 0799 0799 0799	3.8 0 0°723 0°695 0°687 0°641 0°615 0°593 0°567 3.7 0 0°108 0 104 0°996 0°957 0°920 0°884 0°850 0.0°1560 0°153 0°147 0°142 0°138 0°131 0°126 3.6 0 0 233 0°224 0 216 0°208 0°200 0°193 0°186 3.6 0 0 233 0°224 0 216 0°208 0°200 0°193 0°186 3.3 0 0 483 0°1466 0°1450 0 434 0 419 0 404 0°390 3.2 0 0 687 0 664 0°641 0°618 0°598 0°577 0°557 3.1 0 0 988 0 935 0 904 0°874 0°845 0°815 0 289 3.0 0 00135 00131 00126 00122 00118 00114 00111 2.9 0 00187 0 0 81 00125 00169 00164 00159 00154 2.8 0 00256 00248 00240 00233 00276 00279 00249 2.7 0 00347 00336 00326 00317 00307 00299 00289 2.8 0 00466 00463 00440 00427 00445 00402 00391 2.5 0 00664 00587 00570 00554 00539 00523 2.6 0 00620 00798 00776 00755 00734 00695 2.1 0 0179 0104 0102 0099 0096 0094 0091 2.2 0 0139 0°136 0332 0129 0125 0122 0119 2.1 0 0179 0174 0170 0165 0162 0158 0158 3.8 0 0359 0351 0344 0336 0329 0329 0320 3.9 0 0288 0555 0643 0630 0638 0630 0638 3.0 00466 0436 0427 0448 0409 0401 0392 3.1 0 01587 0581 0274 0768 0622 0256 0250 3.1 0 00889 0351 0344 0336 0329 0329 0320 3.1 0 00888 0555 0643 0630 0618 0606 0594 3.1 0 00466 0436 0427 0418 0409 0401 0392 3.1 0 01567 1562 1539 1515 1492 1469 1446 3.0 0 0988 0555 0643 0630 0618 0606 0594 3.1 0 0587 1562 1539 1515 1492 1469 1446 3.0 0 0880 0793 0778 078 0789 0749 0735 1251 1251 1230 3.0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	3.8 0 0°723 0°695 0°687 0°641 0°615 0°593 0°567 0°544 3.7 0 0°108 0 104 0°996 0°957 0°920 0°884 0°880 0°816 3.8 0 0°186 0°183 0°147 0°142 0°138 0°131 0°126 0°127 3.6 0 0°333 0°1274 0 216 0°208 0°200 0°193 0°185 0°127 3.6 0 0°337 0°325 0°331 0°302 0°291 0°280 0°270 0°260 3.3 0 0 483 0°466 0°450 0 434 0 419 0 404 0°190 0°376 3.2 0 0 687 0°664 0°44 0°618 0°596 0°577 0°557 0°538 3.1 0 0 968 0 935 0 904 0°874 0°845 0°616 0 2°89 0°762 3.0 0 00187 0 00131 00°126 00122 00118 00114 00111 00107 2.8 0 0 00187 0 0 81 00175 00169 00164 00159 00154 00162 2.8 0 0 0066 00463 00440 00427 00415 00402 00391 00379 2.8 0 0 0066 00463 00440 00427 00415 00402 00391 00379 2.8 0 0 0066 00463 00440 00427 00415 00402 00391 00379 2.8 0 0 00627 00604 00587 00570 00554 00599 00523 00508 2.3 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	38 0 0 772 0 0 695 0 667 0 607	38 004723 0'895 0'687 0'641 0'615 0'4891 0'8567 0'544 0'522 0'501 37 00108 0 104 0'896 0'497 0'920 0'884 0'886 0'816 0'784 0'753 36 00733 0'724 0'747 0'7142 0'7138 0'7301 0'786 0'712 0'716 35 00 233 0'724 0'747 0'7142 0'738 0'7301 0'727 0'716 36 00 233 0'724 0'747 0'7142 0'738 0'720 0'728 0'727 0'766 37 00 233 0'724 0'760 0'728 0'720 0'7280 0'727 0'766 38 00 233 0'724 0'747 0'7142 0'736 0'720 0'7280 0'727 0'766 38 00 233 0'724 0'726 0'728 0'720 0'7280 0'7280 0'7280 0'7281 0'7172 0'7165 38 00 337 0'325 0'313 0'302 0'7291 0'7280 0'7270 0'7280 0'7280 0'7281 0'7172 0'7165 39 00 687 0'664 0'664 0'664 0'664 0'664 0'664 0'664 0'664 0'766 0'789 0'762 0'738 0'769 0'7	38 00*723 0*995 0*667 0*041 0*615 0*693 0*567 0*544 0*522 0*503	38 00*723 0*995 0*687 0*641 0*615 0*5891 0*587 0*544 0*522 0*551 0*10*10*10*10*10*10*10*10*10*10*10*10*10	38 007723 0'695 0'685 0'687 0'641 0'615 0'993 0'897 0'944 0'622 0'591 0'108 0 104 0'996 0'997 0'992 0'884 0'860 0'816 0'798 0'753 0'117 0'112 0'113 0'117 0'114 0'111 0'117 0'	3.8 0 0°723 0°695 0°687 0°697 0°697 0°693 0°597 0°594 0°452 0°590 0°497 0°790 0°488 0°485 0°486	3.8 0 0°723 0°695 0°687 0°697 0°697 0°697 0°597 0°598 0°596 0°396 0°497 0°497 0°498 0°496 0°496 0°497 0°497 0°498 0°497 0°497 0°498 0°497 0°497 0°498 0°498 0°497 0°498	3.8	18	18

The left-hand column gives the ordinate  $\phi(z) = e^{-\frac{1}{2}z^2} \sqrt{2\pi}$  of the standard normal distribution (i.e., the normal distribution having mean 0 and standard deviation 1), z being listed in the second column. The rest of the table gives  $\Phi(z) = \int_{-\infty}^{z} \phi(t) dt = \operatorname{Prob}(Z \leq z)$ , where Z is a random variable having the standard normal distribution. Locate z, expressed to its first decimal place in the second column, and its second decimal place along the top or bottom

horizontal, the corresponding table entry is  $\Phi(z)$ . Proportional parts are given for the third decimal place of z in part of the table. These proportional parts should be subtracted if z < 0 and added if z > 0.

PROPORTIONAL PARTS

EXAMPLES:  $\Phi(-1.2) = \text{Prob}(Z \le -1.2) - 0.1151$ ;  $\Phi(-1.23) = 0.1093$ ;  $\Phi(-1.234) = 0.1086$ 

														PR	DPOR	AD MOITI	IAL P.	ARTS		
φ(z)	Z	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	
3989	00	0 5000	5040	5080	5120	5160	5199	5239	5279	5319	5359	4	8	12	16	20	24	, 28	32	3(
3970	0.1	0 5398	6438	5478	5517	5557	5596	5636	56 75	5714	5753	4	8	12	16	20	24	28	32	30
3910	0.2	0 5793	5832	5871	5910	5948	5987	5026	6064	6103	6141	4	8	12	15	19	23	27	31	3
3814	03	0 61 79	6217	6255	6293	6331	6368	6406	6443	6480	6517	4	8	11	15	19	22	26	3O	34
0 3683	0.4	0 6554	6591	6628	6664	6700	6736	6772	6808	6844	6879	4	7	11	14	18	22	25	29	33
0 3521	0.5	0 6915	6950	6985	7019	7054	7088	7123	7157	7190	7224	3	7	10	14	17	21	24	27	31
0 3332	06	0 7257	7291	7324	7357	7389	7422	7454	7486	7517	7549	3	6	10	13	16	19	23	26	29
0 3123	0.7	0 7580	7611	7642	7673	7704	7734	7764	7794	7823	7852	3	6	9	12	15	18	21	24	2
0.2897	0.8	0.7881	7910	7939	7967	7995	8023	8051	80.78	8106	8133	3	6	8	11	14	17	19	22	25
0 2661	0.9	0.8159	8186	8212	B238	8264	8289	8315	8340	8365	B389	3	5	8	10	13	15	18	20	23
0 2420	10	0 8413	8438	8461	8485	8508	8531	8554	8577	8599	8621	2	5	7	9	12	14	16	18	21
0 2179	7.1	0 8643	8665	8686	8708	8729	8749	8770	8790	8810	8830	2	4	6	В	10	12	14	16	15
0 1942	12	0 8849	8869	6868	8907	<b>B</b> 925	8944	8962	8980	8997	9015	2	4	5	7	9	11	13	15	16
0.1714	1 3	0 9032	9049	9066	9082	9099	9115	9131	9147	9162	9177	2	3	5	6	8	10	13	13	14
0.1497	1.4	0 9192	9207	9222	9236	9251	9265	9279	9292	9306	9319	ī	3	4	6	7	В	10	11	13
0 1295	15	0 9332	9345	9357	9370	9382	9394	9406	9418	9429	9441	1	2	4	5	6	7	8	10	1 1
0.1109	16	0 9452	9463	9474	9484	9495	9505	9515	9525	9535	9545	1	2	3	4	5	6	7	В	9
0 0940	17	0 9554	9564	9573	9582	9591	9599	9608	9616	9625	9633	1	2	3	3	4	5	6	7	8
0 0790	1.8	0 9641	9649	9656	9664		9678	9686	9693	9699	9 7 0 6	1	1	2	3	4	4	5	6	6
0 0856	19	0 9713	9719	9726	9732		9744	9750	9756	9761	9767	1	1	2	2	3	4	4	5	5
0 0540	20	0 9772	9778	9783	9788	9793	9798	9803	9808	9812	9817	0	1	1	2	2	3	3	4	4
0 0440	2.3	0 9821	9828	9830	9834	9838	9842	9846	9850	9854	9857	0	1	1	2	2	2	3	3	4
0 0355	22	0 9861	9864	9868	9871	9875	9878	9881	9884	9887	9890	0	1	1	1	2	2	2	3	3
0 0283	23	0 9893	9896	9898	9901	9904	9906	9909	9911	9913	9916	0	0	1	1	1	2	2	2	2
0 0224	2.4	0 99180	99202	99224	99245	99266	99286	99305	99324	99343	99361	2	4	6	8	10	12	14	16	18
0 0175	2.5_	0.99379	99396	99413	99430	99446	99461	99477	99492	99506	99520	2	3	5	6	8	9	11	12	14
0.0136	2.6	0 99534	99547	99560	99573	99585	99598	99609	99621	99632	99643	1	2	4	5	6	7	8	10	1)
0.0104	27	0 99653	99664	99674	99683	99693	99702	99711	99720	99128	99736	1	2	3	4	5	5	6	7	8
0.00792	2.8	0 99744	99752	99760	99767	99774	99781	99788	99795	99801	99807	1	1	2	3	3	4	5	6	6
0.00595	29	0 99813	99819 99869	99825 99874	99831	99836	99841	99846	99851	99856	99861	0	1	2	2	3	3 2	3	4	5
	3.0	0 99865			99878	99882	99886	99889	99893	99896	99900	U	÷		1 4	_	_	-	_	_
0 00327	3 1	0 8,035	93 065	9,096	93 126	93 155	9,184	91211	9,538	91264	9,588	1	2	3	4	- 5	- 6	7	8	9
0.00238	3.2	0 9 313	9 <sup>3</sup> 336	93359	93381	91402	93423	9'443	9'462	9 481	9'499					AD	D			
0.00172	33	0.8 <sup>3</sup> 517 0.9 <sup>3</sup> 663	9 <sup>3</sup> 534 9 <sup>3</sup> 675	9°550 9°687	9'566 9'698	9 <sup>3</sup> 581	93596	93610	9 <sup>3</sup> 624 9 <sup>3</sup> 740	9°638 9°749	93651			PRO	POR		IAL P	ARTS		
0 0 0 1 2 3	3.5	0.9 767	9 776	9 784	9, 999	9 <sup>3</sup> 709 9 <sup>3</sup> 800	9 <sup>3</sup> 720 9 <sup>3</sup> 807	9 <sup>3</sup> 730 9 <sup>3</sup> 815	91822	91828	9 <sup>3</sup> 758 9 <sup>1</sup> 835		_						_	_
0.03612	36	0.93841	93847	91853	93858	91864	93869	9 <sup>3</sup> B74	93879	9,883	9'888									
0.0 <sup>3</sup> 425 0.0 <sup>3</sup> 292	37	0.9 <sup>3</sup> 892 0.9 <sup>4</sup> 277	9° 896 9° 305	9°004 9°333	9 <sup>4</sup> 043 9 <sup>4</sup> 359	94 080 94 385	9 <sup>4</sup> 116 9 <sup>4</sup> 409	91150 91433	9* 184 9* 456	9 <sup>4</sup> 216 9 <sup>4</sup> 478	9° 247 9° 499						t in m			
0.0 199	39	0.9 277	94539	94 557	94575	9 593	94609	9 433	94641	9 476	9 499		0.91	401	indic	cates	ន ព្រ	mber	of n	ilne
0.0 <sup>3</sup> 134	40	0.94683	91696	94 709	94 721	9 <sup>4</sup> 733	94 744	94 755	94 765	94 775	9* 784						0.99		9 99	40
													and	0.94	032	= 0.9	99 03	32.		
0.0 <sup>4</sup> 893 0.0 <sup>4</sup> 589	41	0 94 793 0 94 867	9 <sup>4</sup> 802 9 <sup>4</sup> 872	9 <sup>4</sup> 811	94819	9*826	94 834	94841	9 <sup>4</sup> 84B	9"854	9*861									
0.0 589 0.0 385	42	0.95146	9'0/2	9 <sup>4</sup> 878 9 <sup>5</sup> 220	9 <sup>4</sup> 883 9 <sup>5</sup> 254	9 <sup>4</sup> 888 9 <sup>4</sup> 288	9 <sup>4</sup> 893 9 <sup>5</sup> 319	94 898 91 350	9°023 9°379	9'066	9°107 9 433									
0.01249	4.4	0.95459	95 483	95506	95529	9 550	95571	91590	91609	9 627	9 433									
0.04160	4.5	0.9 450	95 676	9*691	95 705	9 <sup>5</sup> 719	95732	91744	91756	9 768	91778									
0.0 <sup>4</sup> 101 0.0 <sup>5</sup> 637	46	0.95 789 0.95870	9°799 9°878	9°808 9°882	9°817 9°888	9°826 9°893	95834	9°842 9°032	9°849 9°079	9°857	9°863 9°166									
0.05396	4.8	0.9 870	98 245	9° 282	9*317	9° 351	91898 91383	9°413	9*442	9 24	9*496									
0.01244	4.0	0.9 521	9° 546	9° 587	9 <sup>6</sup> 589	96 609	9629	9*648	9*665	9*682	9* 698		p	rone	offici	nal n	arts ?	ave :	ton	hee
).0 <sup>5</sup> 149	5.0	0.96713	96 728	9° 742	94 755	96 767	9 <sup>6</sup> 779	9° 790	91801	9*811	9*821						glon			
0.06897		0 96 830	9 <sup>6</sup> 839					_					-				suffic			
0°536	51	0 9"830	9"839	9°847 9°105	9 <sup>4</sup> 855 9 <sup>7</sup> 152	9° 863 97 197	9°870 9°240	9°877 9°280	9°883 9 318	9°889 9 354	9°895 9 388									
0°317	63	0.9 004	97452	97481	9 152 9 2 509	9 197 9 535	9 240	9 280	9 3 18	9 354	9 368									
0.06 186	54	0.9 667	9'685	9°702	9°718	9 <sup>7</sup> /34	97748	9 762	9 775	9 020	9 799									
0.06 108	5.5	0.9 810	9 <sup>7</sup> 821	9 831	97840	9 7 849	97857	9 865	9 873	9 880	9 886									
0.07618	5.6	0.9 <sup>7</sup> 893 0.9 <sup>8</sup> 401	97899	9 <sup>8</sup> 045	91099	9 <sup>8</sup> 150	96 198	95243	9*286	9 <sup>k</sup> 327	91365									
07984	57	0.9*401	9"435 9"688	9 <sup>8</sup> 487 9 <sup>8</sup> 706	9 <sup>6</sup> 498 9 <sup>6</sup> 723	9 <sup>8</sup> 527 9 <sup>8</sup> 739	9 <sup>8</sup> 554 9 <sup>8</sup> 754	9*579 9*769	9° 604 9° 782	9° 626 9° 795	9°648 9°807									
	6.0			T 25 PT	27 1 4.5	39 7.334	29 7 766	3 /09	23 187	PH / 1451	74 201 /									
0.0198	5.8																			
0,0°351 0.0°198 0.0°110 0.0°608	5.8	0.9°818 0.9°013	9*829 9*072	9" 839 9" 128	9° 180	9*857 9*229	9°866 9°276	9*874 9*319	9*881 9*360	9°888	9 <sup>6</sup> 895 9 <sup>9</sup> 435									

EXAMPLES:  $\Phi(1\ 2)$  = Prob  $(Z \le 1.2)$  = 0.8849,  $\Phi(1.23)$  = 0.8907,  $\Phi(1\ 234)$  = 0.8914, Prob  $(Z \ge 2\ 3)$  = Prob  $(Z \le -2\ 3)$  =  $\Phi(-2\ 3)$  = 0.0107 (making use of the symmetry of the normal distribution), Prob  $(0\ 32\le Z\le 1.43)$  =  $\Phi(1\ 43)$  =  $\Phi(0\ 32)$  = 0.9236 = 0.6255 = 0.2981.

Other normal distributions may be dealt with by standardisation, i.e. by subtracting the mean and dividing by the standard deviation. For example if X has the normal distribution with mean 10.0 and standard deviation 2.0,  $\text{Prob}(X \leq 17.5) = \text{Prob}(Z \leq \frac{1}{2}(17.5 - 10.0)) = \text{Prob}(Z \leq 3.75) = \Phi(3.75) = 0.9999116$ .

## Percentage points of the normal distribution



y = 0(x)	af	97	7	المت
0.50				0.0000
0.60	40%			0 2533
0.70	30%			0 5744
0.80	20%	40%	60%	0.84 5
0.85	15%	30%	7()%.	1 0364
0.90	1-0%	20%	80%	2816
0.91	9%	18%	82%	1 3408
0.92	8%	16%	84%	4061
0.93	7%	14%	86%	1 4758
0.94	6%	12%	884	1 554R
0 950	-100m	10.0%	90.0%	1 6449
0.952	4.8%	9.6%	90 4%	1 6646
0.954	4.6%	9.2%	90.8%	1 6849
0 956	4 4%	8 8%	9 2%	1 7060
0.958	4 2%	8 4%	9 64	1 72-29
0 960	4.0%	B 0%	92.0%	1 2507
0.962	3 8%	7.6%	92.4%	7744
0.964	36%	7 2%	92.8%	1 7991
0.966	3.4%	6.8%	93 24	8250
0.968	3 2%	6 4%	93.5%	8527

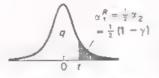
g = OUT	45	a <sub>0</sub>	γ	
(3°C)	30.	E = =	94.0	* 8RDA
0 971	2 9%	58%	94.2%	1 8957
0.972	284	56%	94.45	19110
0 973	2 74	5 4%	94.65	1 9268
0 9 7 4	26%	5.24	94.8	1 9431
0.975	26%	16.00	18.07k	1 9600
0 9 76	245	49	35.	1 9274
0.977	235	463	95 41	9954
0 9 7 8	22%	4.4%	95 6%	2 0141
0 9 7 9	2 1%	4 2%	95.8%	2 0335
0.980	2.0%	40%	96 O's	2 0537
0.98	19%	384	96.2%	2 0749
0.987	1.8%	3.6%	96.45	2 0969
0.983	7 73	3 4%	96 6%	2 201
0.984	16.	3.2%	95.8%	2 1444
0.985	15%	3.0%	410	2 1 10
0.986	1.6%	2.9%	972"	2 1973
0.987	1.3%	265	9244	2 2262
0.988	1.2%	24%	9765	2 25 1
0.989	1.1%	2 2%	978%	2 2904

q = 4ki	0/h	ů <sub>3</sub>	γ	2
C 990 %	1.0%	2 🧬	· 69 (2)	75.03
0.991	09%	1 B1	98 20.	2 3656
0.992	0 81%	1.65	98.4"	2 4089
0 993	0.7%	14	gя Б″ <sub>і:</sub>	2 4573
D 994	0.6%	1.2"	90.8%	25 21
0 995	D 5%	1.0%	20.0%	2 5758
D-396	0.4%	D.8 .	90 Z	2 6521
2 997	0.3%	0.6%	99.4%	2.7478
0.998	0.2%	0.4%	99.6%	2 8 78 2
D 999	0.1%	0.2%	99.8%	3 0902
0 9995	0.05%	0.1%	99.9%	3 2905
0.9999	0.01%	0.02%	99 98%	3 7190
0 99995	0.005%	0.01%	99 99%	3 89D6
0 99999	0.001%	0.002%	99 998%	4 2849
0 999995	0.0005%	0.001%	99.999%	4.4 72
0 999999	3.0001%	0.0002""	99 9998".	4 7534
0.9999995	0.00005%	0.0001%	99 9999%	4 8916
0 9999998	0.00001%	0.00002%	89 999985	5 993
0 99999995	0.000005%	0.00001%	99 99999%	5 3267
0 99999999	0.000001%	0.000002%	#866666 BB	56 20

The following notation is used in this and subsequent tables, q represents a quantile, i.e. q and the tabulated value z are related here by  $\operatorname{Prob}(Z \leqslant z) = q = \Phi(x)$ ; e.g.  $\Phi(1.9600) = q = 0.975$ , where z = 1.9600,  $\alpha_1$ ,  $\alpha_1^L$  and  $\alpha_1^R$  denote significance levels for one-tailed or one-dided critical regions. Sometimes  $\alpha_1^L$  and  $\alpha_1^R$  values, corresponding to critical regions in the left-hand and right-hand tails, need to be tabulated separately; in other cases one may easily be obtained from the other. Here we have included only  $\alpha_1^R$ , since  $\alpha_1^L$  values are obtained using the symmetry of the normal distribution. Thus if a 5% critical region in the right-hand tail is required, we find the entry corresponding to  $\alpha_1^R = 5\%$  and obtain  $Z \ge 1.6449$ . Had we required a 5%

critical region in the left-hand tail it would have been  $Z \leq -1.6449$ ,  $\alpha_2$  gives critical regions for two-sided tests, here  $|Z| \geq 1$  9600 is the critical region for the two-sided test at the  $\alpha_2 = 5\%$  significance level. Finally,  $\gamma$  indicates confidence levels for confidence intervals – so a 95% confidence interval here is derived from  $|Z| \leq 1.9600$ . For example with a large sample  $X_1, X_2, \ldots, X_n$  we know that  $(\overline{X} - \mu)/(s/\sqrt{n})$  has approximately a standard normal distribution, where  $\overline{X} = \sum X_i/n$  and the adjusted sample standard deviations is given by  $s = \{\sum (X_i - \overline{X})^2/(n-1)\}^{1/2}$ . So a 95% confidence interval for  $\mu$  is derived from  $|(\overline{X} - \mu)/(s/\sqrt{n})| \leq 1.9600$ , which is equivalent to  $\overline{X} = 1.96s/\sqrt{n} \leq \mu \leq \overline{X} + 1.96s/\sqrt{n}$ 

## Percentage points of the Student t distribution



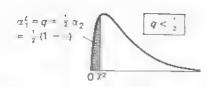
a = 1	0.95	0.975	n 90	0 995
OR I		7	ART IN	
03	Qs.	9%	2".	12
7	90%	96%	98%	98%
P				
1	5.3138	12 7062	31 8205	63 6567
2	2 9 2 0 0	4 3027	6 9846	9 9248
1	2 3534	3 1824	4 540 7	5 8409
4 ]	2 1318	2 7 7 5 4	3 7489	4 6041
9	2 0 1 5 0	2 5 7 0 6	3 3649	4 0321
6	1 9432	2 4469	3 1427	3 70 74
7	1 8946	2 3646	2 9980	3 4995
8 1	1 8595	2 3060	7 8965	3 3554
9.	1 8331	2 2622	2 8214	3 2408
10	1 8125	2 7 7 8	2 7638	3 1693
11	1 7959	2 2010	2 7181	3 1058
12 1	1 7823	2 1788	2 68 10	3 0545
13	1.7709	2 1604	2 6503	3 0 23
14	1 7613	2 1448	2 6245	2 9 7 6 8
15	1 7531	2 1314	2 6025	2 9467
16	1 7459	2 1199	2 5835	2 9208
17	1 7396	2 1098	2 5669	2 8982
18	1.7341	2 1009	2 5524	2 8 7 8 4
19	1 7291	2 0930	2 5395	2 8609
30.	1 7247	2 0860	2 5 2 8 0	2 8453

g .	n 16,	0 975	ባ ኅሳ	0 995
41	984	2	5 75	
0.2	10:	5%	2~	7%
7	90%	95%	98%	99%
21	1 7207	2 0 796	2 51 78	2 8314
22	1.7171	2 0739	2 5083	2 8188
23	1 7139	2 0687	2 4999	2 8023
24	1 2109	2 0639	2 4922	2 7969
25	1.7081	2 0595	2 4851	2 2824
26	1 2056	2.0555	2 4 7 8 6	2 7787
27	1 7033	2 0518	2 4 7 2 7	2.7707
28	1-2011	2 0484	2 4671	2 7633
29	1 6991	2 0452	2 4620	2 7564
30	1 6973	2 0423	2 4573	2 1500
31	1 6966	2 0395	2 4528	7 7440
32	1 6939	2 0369	2 4487	2 7385
33	1 6924	2 0345	2 4448	2 1333
34 -	1 6909	2 0322	2 4411	2 7284
35	1 6896	2 0301	2 4377	2 7238
36	1 6883	2 0281	2 4349	2 7195
37	1 6871	2 0262	2 4314	2 7154
38	1 6860	2 0244	2 4 2 8 6	2 7116
39	1 6849	2 0227	2 4258	2 7079
40	1 6839	2 0211	2 4 2 3 3	2 7045

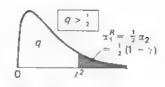
9	D JE	0975	0.09	0.995
of 1	The Party of the P	2 11	196 1	Tr.
Own		5%	74.	1%
, ,	90%	96%	08%	09%
42	1 6820	2 0181	24185	2 6981
- 64	1 6807	20154	2.4141	2 6923
4.0	1 6767	2 0 1 2 9	2 4107	2 6870
48	1 6777	2 0106	2.4086	2 8822
50 :	1 6759	2 0086	2 4033	2 G77B
95	1 6730	2 0040	2 3961	2 6682
60	1 6706	2 0003	2 3901	2 6603
85	1 6686	1 9971	2 3851	2 6536
70	1 6669	1 9944	2 3808	2 64 79
75	1 6654	1 9921	2 3771	2 6430
90	1 6641	1 9901	2 3739	2 6387
85	1 6630	1 9883	2.3710	2 6349
90	1 6820	1 9867	2 3685	2 6316
95	1 6617	1 9853	2 3662	2 6 2 8 6
100	1 6602	1 9840	2 3642	2 6259
125	1 6571	1 9791	2 3665	2 6157
150	1 6551	1 9759	2 3515	2 6090
125	1 6536	1 9736	2 3478	2 6042
200	1 6525	9719	2 3451	2 6006
- 09	2.0449	1,9600	2.3263	2,6758

The t distribution is mainly used for testing hypotheses and finding confidence intervals for means, given small samples from normal distributions. For a single sample,  $(\bar{X}-\mu)/(s/\sqrt{n})$  has the t distribution with  $\nu=n-1$  degrees of freedom (see notation above) So, e.g. if n=10, giving  $\nu=9$ , the  $\gamma=95\%$  confidence interval for  $\mu$  is  $\bar{X}-2.2622s/\sqrt{10} \le \mu \le \bar{X}+2.2622s/\sqrt{10}$ . Given two samples of sizes  $n_1$  and  $n_2$ , sample means  $\bar{X}_1$  and  $\bar{X}_2$ , and adjusted sample standard deviations  $s_1$  and  $s_2$ ,  $(\bar{X}_1-\bar{X}_2)/\sqrt{10}$ 

 $\{s\sqrt{(1/n_1)+(1/n_2)}\}$  has the t distribution with  $\nu=n_1+n_2-2$  degrees of freedom, where  $s=\{(n_1-1)s_1^2+(n_2-1)s_2^2\}/(n_1+n_2-2)\}^{1/n}$ . So if the population means are denoted  $\mu_1$  and  $\mu_2$ , then to test  $H_0: \mu_1=\mu_2$  against  $H_1:\mu_1>\mu_2$  at the 5% level, given samples of sizes 6 and 10, the critical region is  $(\bar{X}_1-\bar{X}_2)/(s\sqrt{3}+\frac{1}{10})\geq 1.7613$ , using  $\nu=6+10-2=14$  and  $\alpha_1^R=5\%$ . As with the normal distribution, symmetry shows that  $\alpha_1^L$  values are just the  $\alpha_1^R$  values prefixed with a minus sign.



# Percentage points of the chi-squared $(\chi^2)$ distribution



9	0 005	0.0	0.025	0.05	0 10	0.50	0.90	0 95	0.975	0.99	0.99
o <sup>L</sup>	4		2.%		10%						
or <sub>1</sub>							10%	THE STATE OF	21:46		1%
cr <sub>1</sub>	1%	2%	96	10%	20%		20%	10%	93	2%	1%
2	98%	98%	95%	90%	80%		80%	90%	96%	98%	999
P										_	
1 2	00004	00016	00098	00393	0158	0 455	2 706	3 841	6.024	6.636	7.87
3	D1D0 0717	0201	0506	0 03	0.211	1 386	4 605	5 991	7.378	9.210	10 59
4	0 207	0 297	0 216 0 484	0 352	0 584 1 D64	2 368	6 251	7.815	9 348	11 345	12.8
5	0.412	0 554	0.831	1 145	* 510	4 351	7 779 9 236	9 488 11 070	11 143 12 833	13.277 15 086	14.60 16.79
8	D 676	0.872	1 237	1 635	2 204	5 348	10 645	+2 592	14 449	16 812	18.5
7	0 989	1 239	1 690	2 167	2 833	6 346	12 01 2	14 067	16 013	18 475	20.2
В	344	1 646	2 180	2 733	3 490	7.344	13 382	15 507	17 536	20.090	21 9
9	1 735	2 088	2 700	3 325	4 168	8 343	14 684	16 919	19 023	21 558	23 5
10	2 158	2 558	3 247	3 940	4 865	9 342	15 98 7	18 307	20 483	23 209	25 1
11	2 803	3 053	3 816	4 575	5 578	10 341	17 275	19675	21 920	24 725	76 7
12	3 074	3 5 7 1	4 404	5 228	6.304	1 340	18 549	21 DZ8	23 337	26.217	28 3
13	J 565	4 107	5 DD9	5 892	7 04 2	12 340	19.812	22 362	24 736	27 688	29 B
14	4 075	4 660	5 829	6.571	7 790	13 339	21 064	23 685	26 110	29 141	31 3
15	4 601	5 229	6 262	7.261	8 547	14 339	22 307	24 996	27 488	30 578	32 6
16	5 142	5 012	6 908	7.982	9 3 2 2	15 338	23 547	26 296	28 845	32.000	34.2
18	5.697	6.408	7 564	8 672	10 085	16 338	24 769	27 587	30 191	33.409	35.7
19	6 265 6 844	7 D15 7 B33	8 231	9 390	10 865	17.338	25 989	28 869	31 528	34 805	37 1
20	7 434	8 280	8 907 8 591	10 117	11.651	18 338	27 204	30 144	12 852	36 191	38 5
21					12 443	19 33?	28 4+2	31 410	34 170	37 566	39 9
22 :	8 034 8 643	8 897	10 283	11.591	13 240	20-337	79 6 1 5	32 671	35 479	38 932	41.4
23	9 260	9 542	10 982	12:338	14 849	21 337	30 813	33 924	38.781	40 289	42.7
24	9 886	10 856	12 401	13.848	15 859	22 337 23 337	37 007	35 172	38 075	41 638	44 1
26	10 520	11 524	13 120	14 611	16.473	24-337	34 382	36 415	39 364 40 646	42 980 44 314	45 5 45 9
36	11 160	12 198	13 844	15 379	17 292	25 336	35 563	38 885	41 923	45.642	48 21
27	11 808	12 879	14.573	18 151	18 114	26 336	36 741	40 113	43 195	46 963	49 6
28	12-461	13 585	15 306	18 928	18 939	27 336	37916	41 337	44 461	48.278	50 9
29	13 2+	14 256	16 047	17.708	19 768	28 336	39 087	42 557	45 727	49 58B	52 3
30	13 787	14 953	16 791	18 493	20 599	29.338	40 256	43.773	46 979	50 B92	53 6
31	14 458	15 655	17 539	19 281	21-434	30 336	41 422	44 985	48 232	57 191	55 D
22	15 134	18 382	1B 291	20 072	72 271	31 336	42 585	46 194	49 480	53 486	56 3
33	1585	17 024	19 04 7	20 96 7	23 110	32 336	43 745	47 400	50 725	54 778	57 5
34	16 50	17 789	19 806	21 664	23 952	33 336	44 903	48 602	51 966	56.051	58 9
35	17 192	18 509	20 569	22 465	24 797	34 336	46 059	49 802	53 203	57 342	60 2
36	17887	19 233	21 338	23 269	25 643	35 336	47 212	50 998	54 437	58.619	61 50
37	18 586	19 960	27 OG	24 075	26 492	36 336	48 363	52 192	55 668	59 693	82 88
35	9 289	20 691	22 676	24 884 25 695	27 343	37-335	49.513	53 384	56 996	61 162	64.16
40	20 207	27 164	24 433	76 509	28 196	38 335 39 335	50 660 51 805	54 572 55 758	58 120 59 342	62.428	86.43
45	24 311	25 90*	28 366							63 691	68.78
50	27 991	29 107	32 357	30 612	33 350 37 689	44 335	57 505 63 167	61 656 67 505	65.410	89 967	73 16
80 .	35-534	37 485	40 482	43 188	46 459	59 335	74 397	79 082	71 420 63 298	76.154 88 379	76 49
70	43 275	45.442	48 258	51 139	65 329	69 334	85 52	90 531	95.023	100.43	81 95 104 2
80	51 172	53 540	57 153	60 39*	84 278	79 334	96 578	101 88	106 63	112 33	1163
90	59 196	61-254	55 64 7	69 176	73 291	89 334	107.57	113 15	118.14	124 12	128 3
00	67 328	70 085	74 222	77 979	82 358	99 334	118 50	124 34	129 68	135 81	140 1
20	83 852	B6-923	9 573	95 205	100 62	119 33	140 23	146.57	152 21	168.95	183 6
50	109 14	11267	117.98	122 69	128.28	149.33	172.58	179 58	186.80	193.21	198 3
tou ,	152 24	156 43	162 73	168 28	174 64	199 33	226 02	233 99	241.06	249.45	265 2

The  $\chi^2$  (chi-squared) distribution is used in testing hypotheses and forming confidence intervals for the standard deviation  $\sigma$  and the variance  $\sigma^2$  of a normal population. Given a random sample of size n,  $\chi^2=(n-1)e^2/\sigma^2$  has the chi-squared distribution with  $\nu=n-1$  degrees of freedom (s is defined on page 20). So if n=10, giving  $\nu=9$ , and the null hypothesis  $H_0$  is  $\sigma=5$ , 5% critical regions for testing against (a)  $H_1$ :  $\sigma<5$ , (b)  $H_2$ :  $\sigma>5$  and (c)  $H_1$ .  $\sigma\neq 5$  are (a)  $9e^2/25 \leq 3.325$ , (b)  $9e^2/25 \geq 16.919$  and (c)  $9e^2/25 \leq 2.700$  or  $9e^2/25 \geq 19.023$ , using significance levels (a)  $\sigma^2_1$ , (b)  $\sigma^2_1$  and (c)  $\sigma^2_2$  as appropriate. For example if  $s^2=50.0$ , this would result in rejection of  $H_0$  in favour of  $H_1$  at the 5% significance level in case (b) only. A  $\gamma=95\%$  confidence interval for  $\sigma$  with these data is derived from  $2.700 \leq (n-1)s^2/\sigma^2 \leq 19.023$ , i.e.  $2.700 \leq 450.0/\sigma^2 \leq 19.023$ , which gives  $450/19.023 \leq \sigma^2 \leq 450/2.700$  or, taking square roots,  $4.864 \leq \sigma \leq 12.910$ .

The  $\chi^2$  distribution also gives critical values for the familiar  $\chi^2$  goodness-of-fit tests and tests for association in contingency tables (cross-tabulations). A classification scheme is given such that any observation must fall into precisely one class. The data then consist of frequency-counts and the statistic used is  $\chi^2 = \Sigma (Ob, -Ex)^2 / Ex$ .

where the sum is over all the classes, Ob. denoting Observed frequencies and Ex. Expected frequencies, these being calculated from the appropriate null hypothesis  $H_0$ . It is common to require that no expected frequencies be less than 5, and to regroup if necessary to achieve this. In goodness-of-fit tests, Ho directly or indirectly specifies the probabilities of a random observation falling in each class. It is sometimes necessary to estimate population parameters (e.g. the mean and/or the standard deviation) to do this. The expected frequencies are these probabilities multiplied by the sample size. The number of degrees of freedom  $\nu =$ (the number of classes - 1 - the number of population parameters which have to be estimated) With contingency tables, Ho is the hypothesis of no association between the classification schemes by rows and by columns, the expected frequency in any cell is (its row's subtotal) x (its column's subtotal) + (total number of observations), and the number of degrees of freedom v is (number of rows - 1) x (number of columns - 1).

In all these cases, it is large values of  $\chi^2$  which are significant, so critical regions are of the form  $\chi^2 \geqslant tabulated$  value, using  $\alpha_1^R$  significance levels.

### Percentage points of the F distribution

 $\begin{array}{c|c}
 & \gamma_1^R = \frac{1}{2} \gamma_2 \\
 & = \frac{1}{2} (1)
\end{array}$ 

Three of the main uses of the F distribution are (a) the comparison of two variances, (b) to give critical values in the wide range of analysis-of-variance tests and (c) to find critical values for the multiple correlation coefficient.

have  $1/9.074 \le 4.0/(\sigma_1^2/\sigma_2^2) \le 5.23$  which, after a little manipulation, gives  $4.0/5.523 \le \sigma_1^2/\sigma_2^2 \le 4.0 \times 9.074$ , and taking square roots yields (0.851:6.025) as the  $\gamma = 95\%$  confidence interval for  $\sigma_1/\sigma_2$ .

#### (a) Comparison of two variances

Given random samples of sizes  $n_1$  and  $n_2$  from two normal populations having standard deviations  $\sigma_1$  and  $\sigma_2$  respectively, and where  $s_1$  and  $s_2$  denote the adjusted sample standard deviations (see page 20),  $(s_1^2/s_2^2)/(\sigma_1^2/\sigma_2^2)$  has the F distribution with  $(\nu_1, \nu_2) = (n_1 - 1, n_2 - 1)$  degrees of freedom. In the tables the degrees of freedom are given along the top  $(\nu_1)$  and down the left-hand side  $(\nu_2)$ . For economy of space, the tables only give values in the right-hand tail of the distribution. This gives rise to minor monvenience in some applications, which will be seen in the following illustrations:

- (i) One-sided test  $-H_0$ :  $\sigma_1 = \sigma_2$ ,  $H_1$ :  $\sigma_1 > \sigma_2$ . The tabulated figures are directly appropriate. Thus if  $\sigma_1$ ,  $\sigma_2$  and  $\sigma_2 = 8$ , giving  $\nu_1 = 4$  and  $\nu_2 = 7$ , the  $\alpha_1^R = 5\%$  critical region is  $s_1^2/s_2^2 > 4.120$ .
- (ii) One-nded test  $-H_0$ :  $\sigma_1 = \sigma_2$ ,  $H_1$ :  $\sigma_1 < \sigma_2$ . Here we would normally need  $\alpha_1^L$  values for  $s_1^2/s_2^2$ . However the tabulated values are appropriate if we use the statistic  $s_2^2/s_1^2$  and switch round the degrees of freedom. So if  $n_1 = 5$  and  $n_2 = 8$ , the appropriate  $\alpha_1^R = 5\%$  critical region is  $s_2^2/s_1^2 \ge 6.094$  (using  $\nu_1 = 7$ ,  $\nu_2 = 4$ ).
- (fii) Two-sided test  $H_0$   $\sigma_1 = \sigma_2$ ,  $H_1$ ,  $\sigma_1 \neq \sigma_2$ . Calculate either  $s_1^2/s_2^2$  or  $s_2^2/s_1^2$ , whichever is the larger, switching round the degrees of freedom if  $s_2^2/s_1^2$  is chosen, and enter the tables using the  $\sigma_2$  significance levels. So if  $n_1 = 5$  and  $n_2 = 8$ , giving  $\nu_1 = 4$  and  $\nu_2 = 7$ , then we reject  $H_0$  in favour of  $H_1$  at the  $\sigma_2 = 5\%$  significance level if either  $s_1^2/s_2^2 \ge 5.523$  or  $s_2^2/s_1^2 \ge 9.074$ .
- (iv) Confidence interval for  $\sigma_1/\sigma_2$  or  $\sigma_1^2/\sigma_2^2$ . This is derived from an interval of the form  $f_1 \leq (s_1^2/s_2^2)/(\sigma_1^2/\sigma_2^2) \leq f_2$  where  $f_2$  is read directly from the tables, using the desired confidence level  $\gamma$ , and  $f_1$  is the reciprocal of the tabulated value found after switching the degrees of freedom. Thus if  $\gamma = 95\%$ , and  $\pi_1 = 5$ ,  $\pi_2 = 8$  giving  $\nu_1 = 4$ ,  $\nu_2 = 7$  again, then  $f_2 = 5.523$  and  $f_1 = 1/9.074$ . So, e.g. if  $s_1^2 s_2^2 = 4.0$  we

#### (b) Analysis-of-variance(ANOVA) tests

The F statistics produced in the standard analysis-of-variance procedures are in the correct form for direct application of the tables, i.e. the critical regions are  $F \ge tabulated$  value. Note that  $\alpha_1^R$  (not  $\alpha_2$ ) significance levels should be used. in the one-way classification analysis-of-variance,  $\nu_1$  is one less than the number of samples being compared, otherwise in experiments where more than one factor is involved, F statistics can be found to test the effect of each of the factors and P1 is then one less than the number of levels of the particular factor being examined. If an F statistic is being used to test for an interactive effect between two or more factors, P1 is the product of the numbers of degrees of freedom for the component factors, P2 is the number of degrees of freedom in the residual (or error, or withinsample) sum of squares, and is usually calculated as (total number of observations - 1) - (total number of degrees of freedom attributable to individual factors and their interactions (if relevant)). If the experiment includes replication, and a replication effect is included in the underlying model, this also counts as a factor for these purposes.

#### (c) Testing a multiple correlation coefficient

In a multiple linear regression  $\hat{Y}=a_0+a_1X_1+a_2X_1+\dots+a_kX_k$ , where  $a_0,a_1,a_2,\dots,a_k$  are estimated by least squares, the multiple correlation coefficient R is a measure of the goodness-of-fit of the regression model R can be calculated as  $R=+\sqrt{\sum(\hat{Y}-\hat{Y})^2/\sum(Y-\hat{Y})^2}$ , where Y denotes the observed values and  $\hat{Y}$  their mean, R is also the linear correlation coefficient of  $\hat{Y}$  with Y. Assuming normality of residuals, R can be used to test if the regression model is useful. Calculate  $F=(n-k-1)R^2/k(1-R^2)$ , where n is the size of the sample from which R was computed, and the critical regions showing evidence that the model is indeed useful are of the form  $F \ge tabulated$  value, using the F tables with  $\nu_1 = k$ ,  $\nu_2 = n-k-1$  and  $\alpha_1^R$  significance levels

								0 0 90	) ,	R = 104	Ţ	- 20%	7	90%							
3	1	2	3	4	5	- 5	7	- 1	9	10	12	16	20	25	30	50	76	100	150		P1
1	39 86	49.50	53 35	55 83	5 74	58 20	58.9	59 44	59 86	60 9	60-71	6 72	61.74	62.05	5, 76	62.69	82.90	63.01	63 11	63.33	
2	8 576	9 000	9 62	9 243	9 293	9 326	9 349	9 36	9 381	9 392	9 408	9 425	9.44	9.451	9 458	9.421	9478	9 48 1	9 485	9 491	
3	5 538	5 462	5 391	5 343	5 300	5 286	5 266	5 252	5 240	5 230	5 216	5 200	5 184	5 176	5 168	5 66	5 148	5 144	5 141	5.134	
4	4 545	4 325	4 91	4 107	4 05	4.010	3979	3 955	3 936	3 9 2 0	3 896	3 870	3 644	3 828	3817	3 795	3 784	3.778	3 777	3.761	
5	4 060	3 780	3 610	3 5 2 0	3 453	3 405	3 368	3 339	3316	3 29	3 268	3 238	3 207	3 18"	3 174	3 142	3 133	3 1 2 6	3 1 1 9	3 105	
6	3 776	3 463	3 289	3 181	3 *0B	3 055	3 014	2 983	2 958	2 937	2 905	2871	2,836	2 815	3 800	2 270	2.754	7.746	2 738	2 722	
2	3 589	3 257	3-074	2 961	2 683	2 827	2 785	2 752	2 725	2 103	2 668	2 632	2 595	2571	2.555	2 523	2 506	2.497	2 488	247	
8	3 458	3 113	2 974	2.806	2 7 2 6	2 668	2 624	2 589	2 561	2 538	2 502	2 464	2 425	2 400	2 38 3	2 348	5 330	2 321	232	Z 293	
9	3 350	3 000	7 813	2 593	2811	2 551	2 505	2 469	2 440	246	3 319	7 340	2 298	2 272	2 255	2218	2 199	2 189	2 29	2 169	
q	3 285	2 924	2 72B	2 605	2 527	2 461	2 414	2371	2 34	2 323	2 284	2 204	2 201	2 * 74	2 755	2 111	2 091	2 08 ?	2077	2 055	
3	3 225	2 860	2 660	Z 536	2 451	2 389	2 342	2 304	2 274	2 248	2 209	2.16	2 73	2 095	2.076	2 D36	2016	2 005	994	1 972	
2	3 77	2 80 7	. 606	2 480	2 394	2 331	2 283	2 245	2 214	2 188	2 14 7	2 05	2 060	2 031	29	9,0	1 949	938	1 971	1 904	
3	3 36	2 763	2 660	2 434	2 347	2 283	2 234	2 195	2 164	2 38	2.097	2 053	2.007	1 9 78	1 358	T 9 5	1 993	1 882	1 870	1 846	
4	3 102	2 728	2 522	2 395	2 30 2	2 243	2 193	2 154	2 22	2 095	2 054	2.010	962	1 933	19-7	869	1 846	1 834	1 822	797	
5	3.073	∡ 695	2.490	2 36	2 2 2 3	2 208	2 168	2 119	2 086	2 059	2 017	1 972	924	1 894	1 43 3	858	1 805	1 793	1 78	1 755	
4	3 048	2 668	2 452	2 333	2 244	2 78	2 128	2 088	2 055	2 028	1 985	1 940	891	1 860	1 939	1.793	1 769	1 257	1 744	1 718	
7	3 026	2 645	2 437	2 708	22 B	2 52	2 102	2 06 t	2 028	2.001	1 958	1 912	962	1 83 1	1 800	+ 763	738	1 725	1 213	1 686	
8	3 00 7	2 624	2 416	2 286	2 96	2 30	2 0 7 9	2 038	2 005	7 977	1 933	887	83?	1 805	1 793	1 736	1 711	1 698	1 684	1.657	
9	2 990	2 606	2 397	2 266	2 176	2 109	2 D58	2010	984	1 956	1 912	B65	1 B 4	1.282	1 50	7 2	1 686	1 623	1 659	1 831	
0	2 9 7 5	2 589	2 380	2 249	2 158	2 09 -	2 040	1 909	965	7 937	1 892	1 845	754	761	1 738	1 690	164	1 650	1 836	1 607	
1	2 961	2 5 7 5	2 365	2 233	2 142	2 075	2 023	1.982	948	1 920	8 5	1 877	176	1 742	1 219	1670	1 644	1 630	1616	1 586	
2	2 949	2 561	2 351	229	2 1 28	2 060	2 008	1 967	1 933	7 904	1 859	B1.1	750	1 726	1 702	1 662	625	1 611	1 597	1.587	
13	2 937	2 549	2 339	2.207	21.5	2 04 1	1 995	1 953	919	T 890	1 845	*96	1 784	1 710	1 686	1 636	609	1 594	580	549	
14	2 927	2 538	2 327	2 95	2 103	2 035	1 983	1 34	906	817	1 832	783	730	1 696	167	1.627	1 603	1.579	1 564	1.533	
5	2 9 ° B	2 528	2 31 7	2 64	2 09 2	2 024	1.97	1 929	895	1 866	820	1 771	718	1 683	1 659	1 607	1 579	1 565	1 549	1 518	
0	2 881	2 489	2 276	2 42	2 049	1.980	1 927	1 384	849	219	1.773	т т22	867	1 632	1 606	1.552	1.523	1 607	1 49	456	
15	2 855	2 46*	2 247	2113	2019	† 950	1 896	952	B1	+ 7B7	1 739	688	632	1 595	1 569	1 513	1 482	1 465	1 448	1 417	
10	2 835	2 440	Z 226	2 091	1.997	1 927	. 273	829	1 793	1 763	715	1 662	1 605	1 568	1 541	1 483	1 451	1.434	146	377	
io	2 809	242	2 47	2 061	1 966	+ 895	1 840	1 796	760	7 729	1 580	* 627	† 568	1 529	1 502	1 441	1 40?	38B	1 369	1 327	
5	2 774	2 375	2 158	2 02	926	1 854	7 70g	. 754	3 716	1 685	635	580	1519	1 478	449	1 384	1 346	326	1 304	1 254	
0	2 756	2 356	2 39	2 002	906	1.834	1 776	1 732	696	663	617	1 557	1 494	1 453	1 423	1 355	1 315	293	1 270	124	
io	2 739	2 338	2 21	1 983	886	1 814	1 757	1 7 2	674	1.642	590	1 533	470	1 427	1 396	1 325	1 283	259	1 233	1 169	Ш
	2 706	2 303	2.084	1 945	1,847	1 774	1 717	1 670	1 632	1 599	546	1.487	1.421	1 375	342	1 253	1.214	185	1 151	1.0	

							q	0.95	$\alpha_1^R$	5%	α <sub>2</sub> = 1	0%	y = 90	8							
V <sub>1</sub>	1	2	3	4	5	6	7	8	9	10	12	15	20	25	30	50	75	100	150	50	ייעוע
1	161.4	199,5	215 7	224.6	230.2	234.0	236.8	238.9	240,5	241.9	243.9	245.9	248.0	249.3	250 1	251.8	252.6	253.0	253.5	254 3	1
2	18 51	19.00	19 16	19.25	19.30	19.33	19.35	19.37	19,38	19.40	19.41	19.43	19.45	19.46	19.46	19.48	19.48	19.49	19.49	19 50	2
3	10,13	9,552	B,277	9.117	9.013	8,941	8.887	8.845	8.812	8.786	8.745	8.703	8.660	8.634	8.617	8 581	8.563	8 554	8.545	8.526	3
4	7 709	6.944	6.591	6.388	6.256	6 163	6.094	6.041	5 999	5.964	5.912	5.858	5.803	5.769	5.746	5.699	5.676	5.664	5 652	5 628	4
5	6 808	5.786	5 409	5.192	5.050	4.950	4.876	4.B18	4.772	4.735	4,678	4,619	4.558	4.521	4.496	4.444	4.418	4.405	4.392	4 365	5
6	5 987	5.143	4.757	4 534	4.387	4.284	4.207	4.147	4.099	4.060	4.000	3.938	3,874	3.835	3.808	3 754	3.726	3.712	3.698	3 569	6
7	5 591	4 737	4,347	4 120	3.972	3.866	3.787	3.726	3.677	3,637	3.575	3.511	3,445	3.404	3.376	3.319	3.290	3.275	3.260	3 230	7
8	5 318	4 459	4.066	3.838	3.687	3 581	3 500	3 438	3.388	3.347	3.284	3.218	3 150	3.108	3.079	3.020	2.990	2.975	2 959	2 928	8
9	5.117	4.256	3.863	3.633	3 482	3.374	3.293	3.230	3.179	3,137	3,073	3.006	2 936	2.893	2.864	2.803	2 771	2 756	2.739	2 707	9
10	4 965	4.103	3 708	3.478	3.326	3.217	3 135	3.072	3.020	2.978	2.913	2.845	2.774	2 730	2 700	2.637	2.606	2.588	2.672	2 538	10
11	4.844	3.982	3.587	3.357	3.204	3.095	3.012	2.948	2.896	2.854	2 788	2.719	2.646	2.601	2.570	2 507	2,473	2.457	2,439	2 404	11
12	4.747	3.865	3,490	3,259	3 108	2.996	2,913	2,849	2.796	2.753	2.687	2.617	2.544	2.498	2.466	2.401	2,367	2.350	2.332	2 296	12
13	4 667	3.906	3.411	3 179	3.025	2915	2.832	2 767	2.714	2.671	2 604	2.533	2.459	2.412	2.380	2.314	2.279	2.261	2.243	2 208	13
14	4 600	3.739	3.344	3.112	2 958	2,848	2 764	2.699	2.646	2.602	2.534	2.463	2.388	2.341	2.308	2.241	2.205	2 187	2 169	2 131	14
15	4 543	3.682	3.287	3.056	2.901	2 790	2 707	2.641	2 588	2.544	2.475	2.403	2.328	2.280	2.247	2 178	2 142	2 123	2 105	2 066	15
16	4.494	3,634	3.239	3.007	2.852	2.741	2 657	2.591	2,538	2.494	2.425	2.352	2.276	2.227	2 194	2 124	2.087	2.068	2.049	2 010	16
17	4 451	3,592	3.197	2 965	2.810	2.699	2 614	2.548	2.494	2.450	2.381	2.308	2.230	2.181	2 148	2.077	2.040	2.020	2.001	1 960	17
18	4:414	3.555	3.160	2 928	2 773	2 661	2.577	2.510	2.456	2.412	2.342	2.269	2 191	2,141	2 107	2 035	1.998	1.978	1 958	1 917	16
19	4.381	3.522	3 127	2.895	2 740	2 628	2 544	2.477	2.423	2.376	2.308	2.234	2 155	2 106	2.071	1 999	1.960	1.940	1.920	1 878	19
20	4 351	3,493	3.098	2.886	2,711	2 599	2 514	2 447	2.393	2.348	2,278	2 203	2.124	2.074	2.039	1 966	1.927	1.907	1.886	1.843	20
21	4.326	3.467	3.072	2.840	2 685	2.573	2.488	2.420	2.366	2.321	2 250	2.178	2.096	2.045	2.010	1.936	1,897	1,876	1,855	1 812	21
22	4 301	3,443	3.049	2.817	2.661	2 549	2.464	2.397	2 342	2.297	2.226	2 151	2.071	2.020	1 984	1 909	1.869	1,849	1.827	1 783	22
23	4 279	3.422	3.028	2 796	2.640	2 528	2.442	2.375	2.320	2.275	2.204	2 128	2.048	1 996	1.961	1.885	1.844	1.823	1.802	1 757	23
24	4 260	3.403	3.009	2 776	2.621	2 508	2 423	2.355	2 300	2.256	2 183	2 108	2 027	1.976	1 939	1.863	1.822	1.800	1.779	1 733	24
25	4 242	3 385	2.991	2 759	2.603	2 490	2 405	2.337	2.282	2 236	2.165	2.089	2.007	1.956	1.919	1.842	1.801	1.779	1 757	1.711	25
30	4 171	3.316	2.922	2.690	2.534	2.421	2.334	2.266	2.211	2 165	2.092	2.015	1.932	1.878	1.841	1 761	1 718	1 695	1.672	1 622	30
35	4 121	3.267	2.874	2 641	2.485	2.372	2.285	2.217	2 161	2.114	2.041	1,963	1.878	1.824	1 788	1 703	1.658	1.635	1.610	↑ 558	35
40	4 085	3.232	2.839	2.606	2.449	2 338	2.249	2 180	2 124	2.077	2.003	1.924	1.839	1 783	1,744	1.660	1.614	1 589	1 564	1 509	40
60	4 034	3.183	2 790	2.557	2.400	2.286	2 199	2.130	2.073	2.026	1.952	1.871	1 784	1 727	1.887	1 599	1 551	1 525	1 498	1 438	50
75	3 968	3,119	2.727	2.494	2.337	5 555	2,134	2.064	2.007	1.959	1.884	1.802	1.712	1.653	1.611	1 510	1.466	1,437	1.407	1 339	76
100	3 936	3.087	2.696	2.463	2.305	2 191	2 103	2.032	1.975	1,927	1.850	1 768	1.678	1.616	1.573	1,477	1.422	1.392	1.359	1 283	100
150	3 904	3.056	2 665	2.432	2.274	2 160	2 071	2.001	1.943	1.894	1.817	1 734	1.641	1 580	1 535	1.438	1.377	1.345	1.309	1 223	150
DIO.	3.841	2 996	2 605	2 372	2 214	2 099	2 010	1 938	1 880	1 831	1 752	1 666	1 571	1 506	1 459	1 350	1 283	1 243	1 197	(10	ш

14	1	2	3	4	5	6	7	6	9	10	12	15	20	26	30	50	75	100	160	-00	11/
23	647.8	789.5	864.2	899.6	921.8	937.1	948.2	956.7	963.3	968.6	978.7	984.9	993.1	998 1	1001	1008	1011	1013	1015	1018	1
2	38.51	39.00	39.17	39 25	39.30	39.33	39 36	39.37	39 39	39.40	39.41	39.43		39 46	39 46	39 48	39.48	39 49	39 49	39 50	1
3	17.44	16.04	15.44	15 10	14.88	14 73		14 54	14 47			14.25		14 12		14.01		13.96	13.94	13 90	
4	12.22	10.65	9.978	9.605	9 364	9.197	9,074	B .980	8.905	8.844	8.751	8.657	8.560	8.501	8.461	8.381	8.340	8,319	8.299	8.257	6
5	10.01	8.434	7.784	7 388	7,146	6.978	6.853	6 757	6.681	6.619	6.525	6.428	6.329	6.268	6.227	6 144	6.101	6.080	6.059	6 0 1 5	5
6	8 813	7.260	6 699	6,227	5.988	5.820	5.695	5.600	5.523	5.461	5.366	5 269	5 168	5.107	5.065	4 980	4.937	4.915	4.893	4 849	
7	8.073	8.542	5,890	5.523	5.285	5.119	4 995	4.899	4.823	4.761	4 666	4.568	4 467	4.406	4.382	4 278	4.232	4,210	4 188	4 142	3
8	7.573	6.059	5.416	5.053	4.817	4.852	4.529	4.433	4.357	4.295	4.200	4.101	3,999	3 937	3.894	3.807	3.762	3,739	3.716	3.870	1
9		5,715		4 718	4.484		4 197	4 102	4.026	3 964	3.868	3 769	3.667	3 604	3 560	3.472	3.426		3.380	3 333	1
10	6 937	5.456	4.826	4.468	4.236	4.072	3 950	3.855	3.779	3.717	3.621	3.522	3.419	3.356	3.311	3 221	3.175	3 152	3.128	3 080	10
11	6 724	5,256	4.630	4.275	4.044	3.881	3 750	3.664	3 588	3.526	3,430	3.330	3,226	3,162	3,118	3,027	2.980	2.958	2.932	2 883	11
12	6 554	5.096	4.474	4 121	3.891	3 728	3 607	3.512	3.436	3.374	3,277	3,177	3.073	3.008	2,963	2.871	2.824	2,800	2,775	2 725	12
13		-	4,347	3.996	3.767	3.604	3.483	3.388	3.312	3 250	3.153	3.053	2 948	2.882		2 744	2 696		2.847	2 595	13
14			4.242		3.663	3.501	3,380	3 285	3.209	3,147	3.050	2.949		2 778		2 638	2 590		2.539	2 487	14
15	6.200	4.765	4 153	3.804	3.576	3.415	3,293	3.199	3.123	3.000	2.963	2.862	2 758	2.689	2.644	2.549	2.499	2.474	2.448	2 395	15
16		4.687	4,077	3.729	3.502	3.341	3.219	3,125	3.049	2.986	2.889	2 788	2.681	2.614			2.422	_	2,370	2 3 1 6	16
17		4.618	4.011	3.865	3 438	3.277	3 158	3.061	2.985	2.922	2.825	2 723	2.616	2.548		2.405	2.356		2,302	2 247	177
18		4.560	3,954	3,608	3.382	3.221	3.100	3.005	2.928	2.866	2 769	2.667		2.491		2.347	2.296		2,242	2 187	95
20		4,461	3.859	3.515			3,007		2.880	2.817		2.617		2.441		2.295	2.243	2.170	2 190	2 133	20
																					100
21	5.827	4.420	3.819	3.475	3.250	3.090	2.969		2.798	2.735		2.534		2.356			2.155		2 100	2 042	21
23		3,349	3.750		3.183	3.023	2.902	2.839	2.763	2.668	2.602	2.486	2.389	2.320	2.272	2.171	2.118		2.062	2 003 1 968	23
24			3,721	3.379		2 995	2.874			2.640		2.437		2.257		2.107	2.052		1.995	1 935	24
25		4,291	3.694	3.353		2.969	2.848		2.677				2.300			2.079	2.024		1.966	1 906	25
30	5 568	4 182	3.589	3.250	3.026	2.867	2 746	2 651	2,575	2.511	2.412		2.195	2 124		1.968	1.911		1.851	1 787	30
35		4.106	3.517		2 956	2 796	2.676	2 581		2.440	2.341		2.122	2.049		1.890	1.832		1.769	1 702	35
40		4.051	3,463	3.126		2 744	2.624	2.529	2.452			2 182			1.943	1.832	1,772		1 708	1 637	4
50		3.975	3.390	3.054		2.674	2.553	2.458	2.381		2.216			1,919		1,752		1.656	1.621	1 545	50
75	5 232	3.876	3.296	2.962	2 741	2.582	2.461	2.366	2.289	2.224	2.123	2.014	1,896	1,819	1.765		1.578		1.503	1 417	75
100	5 179	3.828	3.250	2.917	2.696	2 537	2.417	2.321	2.244	2.179	2.077	1.968	1,849	1.770	1.715	1.592	1.522	1.483	1.442	1 347	101
150		3 781	3.204	2.872	2.652	2 494	2.373	2.278	2,200					1,722		1.538	1.464		1,379	1.271	150
100	E 1124	7.000	3.116	2 700	2 507	0.400	2.288	D 400			1.945								1 239	(1.0)	95

							q =	0.99	αj ·	- 126	<u>a</u> 2 =	2%	$\gamma = 98$	12%						
1	1	2	3	4	5	6	7	- 8	9	10	12	15	20	25	30	50	75	100	150	50
1	4052	4999	5403	5625	5764	5859	5928	5981	6022	8056	8106	6157	6209	6240	6261	6303	6324	6334	6345	6366
2	98.50	99.00	99 17	99.25	99 30	99.33	99.36	99.37	99.39	99.40	99.42	99.43	99 45	99 46	99 47	99 48	99 49	99 49	99 49	99 50
3		30.82	29 46	28 71	28.24		27.67	27 49	27.35	27.23		26.87	26 69	26 58	26 50	26 35		26 24	26 20	26 13
4 5			16 69	15.98	15 52		14.98	14.80	14.66	14 55		14.20	14.02	13 91 9.449	13.84	9.238	9 166		9.094	9 020
-	15 20	13 27	12.06	11 39	10 97	10.67	10.46	10.29	10.16	10.05	9.888	9.722	9,553			-	_			+
6		10 92		9 148			8.260		7.976	7.874		7.559	7,396	7 296	7 229			6 98 7		6.880
7		9.547		7.847			6.993		6.719	6 620	6.469	6.314	6.155		5 992			5 756		5 650
8		8 649					6.178	6.029	5.911	5.814		5,515	5.359		5 198		4 998		4 929	4 859
9		8.022		6.422			5.613		5,351	5.257		4.962	4.808		4 649		4 449	4.014	4 380	3 909
0	10.04	7.559	0 002	2 204	6 636	5 386	5 200	1,007	4 942	4,849	4.700	4 558	4.405	4,311	4 24 /			-		
1 1			6 2 1 7	5.668	5 316			4.744	4.632	4 539	4.397	4.251	4 099		3 94 1			3 708		3 602
2		6 92 7		5 4 1 2	5 064	_	4 640		4 388	4.296		4.010	3.858	3 765	3 701			3 467		3.361
3		8.701		5.205	4.862		4 441			4.100		3.815		3.571				3 272		3 165
1		6 5 1 5		5 035	4.695		4 278		4.030	3.939		3.656	3 505	3.412			3 147		3 076 2 942	3 004
5	0.003	0.358	5.417	4 893	4 556	9318	4 142	4.004	3.895	3.805	3.000	3 522	3.372	3,278	3 2 14	3 00	3 012	2 311	2 342	2 868
6	8 531	6 226	5 292	4 773	4 437		4 026	3.890	3 780	3.691	3.553	3.409	3.259	3 165	3 101	2 967		2.863	2 827	2 753
7		6.112		4 669	4.336		3.927		3.682	3.593		3.312		3.068				2 764		2 653
8			5 092				3.841		3 597	3.508		3.227	3 077	2 983				2 678		2 566
8		5.926		4.500	4 171			3.631	3.523	3.434		3.153	3.003	3 909				2 602		2 489
o .	8.096	5.849	4 938	4 431	4 103	3 8 7 1	3 699	3 564	3.457	3.368	3.231	3.088	2 938	2.843	2 77B	2.643	2 572	2 535	2 498	2 421
1	8.017	5.780	4.874	4.369	4.042	3,812	3 640	3 506	3.398	3.310	3.173	3.030		2 785			2512		2 4 3 8	2 360
2			4.817			3 758	3 587	3.453	3.346	3.258		2.978		2 733			2 459		2 384	2 305
3			4 765				3 539	3.408	3.299	3.211	3.074			2.686			2411		2 3 3 5	2 256
	-,-		4 718			3 667	3 496	3,363	3.256	3.168		2.889	2 738	2 643			2 367		2 291	2211
5	7 770	5,568	4 675	4 177	3.855	3 627	3 457	3.324	3.217	3.129	2.993	2.850	2.699	2.604	2 538	2 400	2 327	2 289	2 250	2 169
3 .	7 562	5 390	4.510	4 018	3.699	3.473	3 304	3.173	3.067	2 979	2.843	2 700	2 549	2.453	2 386	2.245	2 170	2 131	2 091	2 006
5	7.419	5.268	4.396	3 908	3.592	3 368	3.200	3.069	2.963	2.876	2 740	2.597	2.445	2,348	2 281	2 137	2 060	2 020	1 9 7 9	1 891
9 ;		5 179		3.828	3.514	3.291	3 124	2 993	2.888	2,801		2.522	2 369	2.271		2 058		1 938	1.896	1.805
1		5 057		3 720	3 408		3 020	2.690	2.785	2.698		2,419	2 265		2 098	1 949		1 825	1 780	1 683
	6.985	4 900	4.054	3.580	3 272	3 052	2.887	2 758	2.653	2 567	2.431	2.287	2.132	2.031	1 960	1 806	1 720	1 674	1 626	15.6
3 1	6.895	4.824	3 964	3 513	3 206	2 988	2 823	2 694	2.590	2 503	2.368	2.223	2.067	1.965	1 893	1 735	1 646	1 598	1 546	1 427
ч.,	E 207	4 749	3 915	3 447	3 142	2 924	2 761	2 632	2 528	2.441	2 305	2.160	2.003	1 900	1 827	1 865	1 5 7 2	1 520	1 465	1 331
	0,007												3.070	1.772						
		4.606	3 782	3.319	3.017	2 802	2 639	2 511	2.407	2,321	2 185	2.039	1.076	1773	1 696	1 523	419	1 35B	1 288	11.01
		4.606	3 782	3.319	3.017	2 802		0 995	,	2,321	2 185		7 = 90	_	1 696	1 523	419	1 358	1 288	11 OF
		4.605	3 782	3.319	3.017			0 995	o <sup>R</sup>	2 3 dP	a <sub>1</sub> =	1%	γ = 90	%						11 Ox
	6 635	2	3	4	6	6	q	0 995	ġ <sup>R</sup>	: ,% 10	12	1%	7 = 90 20	25	30	50	75	100	150	80
	6 635	2 20000	3 21615	<b>4</b> 22500	<b>6</b> 23056	8 23437	7 23715	0 995 <b>8</b> 23925	o <sup>R</sup>	10 24224	12 24426	1% 15 24630	γ = 90 20 24836	<b>25</b> 24960	30 25044	<b>50</b> 25211	75	100 25337	<b>150</b> 25380	25464
	6 635 16211 198 5	2 20000 199 0	3	4 22500 199 2	6 23056 199.3	23437 199 3	7 23715 1994	0 995 8 23925 199,4	9 24091 199.4	10 24224 199.4	12 24426 199.4	1% ] 16 24630 199.4	7 = 99 20 24836 199.4	26 24960 199 5	30 25044 199 5	50 25211 199 5	<b>75</b> 26295	100	150	80
	6 635 18211 198 5 55 56	2 20000 199 0 49.80	3 21615 199 2 47 47	22500 199 2 46 19	23056 199.3 45.39	23437 199 3	23715 1994 4443	0 995 8 23925 199,4 44 13	9 24091 199.4 43.88	10 24224 199.4 43.69	12 24426 199.4 43.39	1% 15 24630 199.4 43.08	γ = 98  20  24836 199.4 42.78	26 24960 199 5 42 59	30 25044 199 5 42 47	25211 199 5 42 21	<b>75</b> 26295 199 5 42 09	100 25337 199 5	25380 199 5 41 96	25464 199 5
	6 635 16211 198 5 55 56 31 33	20000 199 0 49 80 26 28	3 21615 199 2 47 47	22500 199 2 46 19 23 15	23056 199.3 46.39 22.46	23437 199 3 44 84 21 97	23715 199 4 44 43 21 62	0 995 8 23925 199,4 44 13 21 36	9 24091 199.4 43.88	10 24224 199.4 43.69 20.97	12 24426 199.4 43.39 20.70	1% 16 24630 199.4 43 08 20 44	7 = 90 20 24836 199.4 42.78 20.17	26 24960 199 5 42 59	25044 199 5 42 47 19 89	25211 199 5 42 21 19 67	75 26295 199 5 42 09 19 55	100 25337 199 5 42.02	25380 199 5 41 96 19.44	25464 199 5 41 83
1 2 3 4 6	6 635 16211 198 5 55 56 31 33 22 78	2 20000 199 0 49 80 26 28 18 31	21615 199 2 47 47 24 26 16 53	22500 199 2 46 19 23 15 15.56	23056 199 3 45 39 22 46 14 94	23437 199 3 44 84 21 97 14 51	23715 199 4 44 43 21 62 14 20	0 995 23926 199,4 44 13 21 36 13 96	9 24091 199.4 43.88 21.14 13.77	10 24224 199.4 43.69 20.97 13.62	12 24426 199.4 43.39 20.70 13.38	1% 24630 199.4 43.08 20.44 13.16	γ = 90 20 24836 199.4 42.78 20.17 12.90	26 24960 199 5 42 59 20 00 12 76	25044 199 5 42 47 19 89 12 66	25211 199 5 42 21 19 67 12 45	25/295 199 5 42 09 19 55 12 35	100 26337 199 5 42 02 19 50 12 30	150 25380 199 5 41 96 19.44 12 25	25464 199 5 41 83 19 32 12 14
2 3 4 5	16211 198 5 55 56 31 33 22 78 18.63	2 20000 199 0 49.80 26 28 18.31 14.54	3 21615 199 2 47 47 24 26 16 53 12 92	22500 199 2 46 19 23 15 15.56	23056 199.3 45.39 22.46 14.94	23437 199 3 44 84 21 97 14 51	23715 199 4 44 43 21 62 14 20	0 995 23925 199,4 44 13 21 36 13 96 10.57	9 24091 199.4 43.88 21.14 13.77	10 24224 199.4 43.69 20.97 13.62	12 24426 199.4 43.39 20.70 13.38	1% 24630 199.4 43.08 20.44 13.15 9.814	7 = 90 20 24836 199.4 42.78 20.17 12.90 9.589	24960 1995 4259 2000 1276 9451	30 25044 199 5 42 47 19 89 12 66 9 358	26211 199.5 42.21 19.67 12.45	75 26295 199 5 42 09 19 55 12 35 9 074	100 25337 199 5 42.02 19 50 12 30 9 026	150 25380 199 5 41 96 19 44 12 25 8 977	25464 199 5 41 83 19 32 12 14 8 879
3 4 5	16211 198 5 55 56 31 33 22 78 18.63 16.24	200000 199 0 49 80 26 28 18 31 14 54 12 40	21615 199 2 47 47 24 26 16 53 12 92 10.88	22500 199.2 46.19 23.15 15.56 12.03 10.05	23056 199 3 46 39 22 46 14 94 11 46 9 522	23437 199 3 44 84 21 97 14 51 11 07 9 155	23715 199 4 44 43 21 62 14 20 10 79 8 885	0 995 23925 199,4 44 13 21 36 13 96 10.57 8 678	9 24091 199.4 43.88 21.14 13.77 10.39 8.514	10 24224 199.4 43.69 20.97 13.62 10.25 8.380	12 24426 199.4 43.39 20.70 13.38 10.03 8.176	1% 24630 199.4 43.08 20.44 13.16 9.814 7.968	7 = 90 20 24836 199.4 42.78 20.17 12.90 9.589 7.754	24960 1995 4259 2000 1276 9451 7.623	30 25044 199 5 42 47 19 89 12 66 9 358 7 534	26211 199 5 42 21 19 67 12 45 9 170 7 354	75 26295 1995 42 09 19 55 12 35 9 074 7 263	160 25337 199 5 42.02 19 50 12 30 9 026 7 217	150 25380 199 5 41 96 19 44 12 25 8 977 7 170	25464 199 5 41 83 19 32 12 14 8 879 7.076
1 2 3 4 6 7 9	16211 198 5 55 56 31 33 22 78 18.63 16.24 14.89	2 20000 199 0 49 80 26 28 18 31 14 54 12 40 11 04	21615 199 2 47 47 24 26 16 53 12 92 10.88 9 596	22500 199 2 46 19 23 15 15.56 12.03 10.05 8.805	23056 199 3 46 39 22 46 14 94 11 46 9 522 8.302	23437 199 3 44 84 21 97 14 51 11 07 9 155 7 952	23715 199 4 44 43 21 62 14 20 10 79 8.885 7 694	0 995 8 23925 199,4 44 13 21 36 13 96 10.57 8 678 7 496	9 24091 199.4 43.88 21.14 13.77 10.39 8.514 7.339	10 24224 199.4 43.69 20.97 13.62 10.25 8.380 7.211	12 24426 199.4 43.39 20.70 13.38 10.03 8.176 7.015	1% 24630 199.4 43.08 20.44 13.15 9.814 7.968 6.814	7 = 90 20 24836 199.4 42.78 20.17 12.90 9.589 7.754 8.608	26 24960 199 5 42 59 20 00 12 76 9 451 7.623 8.482	26044 199 5 42 47 19 89 12 66 9 358 7 534 6 396	26211 199 5 42 21 19 67 12 45 9 170 7 354 6 222	75 26795 199 6 42 09 19 55 12 35 9 074 7 263 6 133	100 25337 199 5 42.02 19 50 12 30 9 026 7 217 6 088	25380 199 5 41 96 19 44 12 25 8 977 7 170 6 042	25464 199 5 41 83 19 32 12 14 8 879 7.076 5 951
5 5 7 9	16211 198 5 55 56 31 33 22 78 18.63 16.24 14.89 13.61	20000 199 0 49 80 26 28 18 31 14 54 12 40 11 04 10 11	3 21615 199 2 47 47 24 26 16 53 12 92 10.88 9.596 8 717	22500 199 2 46 19 23 15 15.56 12.03 10.05 8.805 7.956	23056 199 3 46 39 22 46 14 94 11 46 9 522 8.302 7 471	23437 199 3 44 84 21 97 14 51 11 07 9 155 7 952 7 134	23715 199 4 44 43 21 62 14 20 10 79 8.885 7 694 6.885	0 995 23925 199,4 44 13 21 36 13 96 10.57 8 678 7 496 6 693	9 24091 199.4 43.88 21.14 13.77 10.39 8.514 7.339 6.541	10 24224 199.4 43.69 20.97 13.62 10.25 8.380 7.211 6.417	12 24426 199.4 43.38 20.70 13.38 10.03 8.176 7.015 6.227	1% 24630 199.4 43.08 20.44 13.16 9.814 7.968 6.814 6.032	7 = 90 20 24836 199.4 42.78 20.17 12.90 9.589 7.754 8.608 5.832	26 24960 199 5 42 59 20 00 12 76 9 451 7.623 8.482 5.708	26044 199 5 42 47 19 89 12 66 9 358 7 534 6 396 5 625	26211 199 5 42 21 19 67 12 45 9 170 7 354 6 222 5 454	75 26295 199 6 42 09 19 56 12 35 9 074 7 263 6 133 5 367	100 25337 199 5 42.02 19 50 12 30 9 026 7 217 6 088 5 322	25380 199 5 41 96 19 44 12 25 8 977 7 170 6 042 5 278	25464 199 5 41 83 19 32 12 14 8 879 7.076 5 951 5 188
3 4 5 6 7 8 8	16211 198 5 55 56 31 33 22 78 18.63 16.24 14.89 13.61 12.83	20000 199 0 49 80 26 28 18 31 14 54 12 40 11 04 10 11 9 427	21615 199 2 47 47 24 26 16 53 12 92 10.88 9.596 8 717 8.081	22500 199 2 46 19 23 15 15.56 12.03 10.05 8.805 7.966 7.343	23056 199 3 46 39 22 46 14 94 11 46 9 522 8 302 7 471 6 872	23437 199 3 44 84 21 97 14 51 11 07 9 155 7 952 7 134 6 545	23715 199 4 44 43 21 62 14 20 10 79 8.885 7 694 6.885 6 302	0 995 23925 199,4 44 13 21 36 13 96 10.57 8 678 7 496 6 693 8 116	9 24091 199.4 43.88 21.14 13.77 10.39 8.514 7.339 6.541 5.968	10 24224 199.4 43.69 20.97 13.62 10.25 8.380 7.211 6.417 5.847	12 24426 199.4 43 39 20 70 13 38 10.03 8.176 7.015 6.227 5.661	1% 24630 199.4 43.08 20.44 13.15 9.814 7.968 6.814 6.032 5.471	7 = 90 20 24836 199.4 42.78 20.17 12.90 9.589 7.754 8.608 5.832 6.274	26 24960 199 5 42 59 20 00 12 76 9 451 7.623 8.482 5.708 5.153	25044 199 5 42 47 19 89 12 66 9 358 7 534 6 396 5 625 5 071	26211 199 5 42 21 19 67 12 45 9 170 7 354 6 222 5 454 4 902	26295 199 5 42 09 19 55 12 35 9 074 7 263 6 133 5 367 4 816	100 25337 199 5 42.02 19 50 12 30 9 026 7 217 6 088 5 322 4 772	150 25380 199 5 41 96 19.44 12 25 8 977 7 170 6 042 5 278 4 728	25464 199 5 41 83 19 32 12 14 8 879 7.076 5 951 5 188 4 639
3 4 6 7 8 9 0 1	16211 198 5 55 56 31 33 22 78 18.63 16.24 14.89 13.61 12.83	20000 199 0 49.80 26 28 18.31 14.54 12.40 11.04 10.11 9.427 8.912	3 21615 199 2 47 47 24 26 16 53 12 92 10.88 9.596 8 717 8.081 7 600	22500 199 2 46 19 23 15 15.56 12.03 10.05 8.805 7.966 7.343 6.881	23056 199 3 46 39 22 46 14 94 11 46 9 522 8 302 7 471 6 872 6 422	23437 199 3 44 84 21 97 14 51 11 07 9 155 7 952 7 134 6 545 6 102	23716 199 4 44 43 21 62 14 20 10 79 8 885 7 694 6 885 6 302 5 865	0 995 23926 199,4 44 13 21 36 13 96 10.57 8 678 7 496 6 693 8 116 5 682	9 24091 199.4 43.88 21.14 13.77 10.39 8.514 7.339 6.541 5.968 5.537	24224 199.4 43.69 20.97 13.62 10.25 8.380 7.211 6.417 5.847	12 24426 199.4 43 38 20 70 13 38 10.03 8.176 7.015 6.227 5.661 5.236	1% 24630 199.4 43.08 20.44 13.15 9.814 7.968 6.814 6.032 5.471 5.049	20 24836 199.4 42.78 20.17 12.90 9.589 7.754 8.608 5.832 6.274 4.855	26 24960 199 5 42 59 20 00 12 76 9 451 7.623 8.482 5.708 5.153 4.736	26044 199 5 42 47 19 89 12 66 9 358 7 534 6 396 5 625 5 071 4 654	25211 199 5 42 21 19 67 12 45 9 170 7 354 6 222 5 454 4 902 4 488	26295 199 5 42 09 19 55 12 35 9 074 7 263 6 133 5 367 4 816 4 402	100 26337 199 5 42.02 19 50 12 30 9 026 7 217 6 088 5 322 4 772 4 358	25380 199 5 41 96 19 44 12 25 8 977 7 170 6 042 5 278 4 728 4 315	25464 199 5 41 83 19 32 12 14 8 879 7.076 5 951 5 188 4 639 4 226
3 4 6 7 8 8 0 1 2	16211 198 5 55 56 31 33 22 78 18.63 16.24 14.89 13.61 12.83 12.23 11 75	200000 199 0 49.80 26 28 18.31 14.54 12.40 11.04 10.11 9.427 8.912 8.510	3 21615 199 2 47 47 24 26 16 53 12 92 10.88 9.596 8 717 8.081 7 600 7.226	22500 199 2 46 19 23 15 15.56 12.03 10.05 8.805 7.966 7.343 6.881 6.521	23056 199.3 46.39 22.46 14.94 11.46 9.522 8.302 7.471 6.872 6.422 6.071	23437 199 3 44 84 21 97 14 51 11 07 9 165 7 952 7 134 6 545 6 102 5 757	23716 199 4 44 43 21 62 14 20 10 79 8 885 7 694 6 885 6 302 5 865 5,526	0 995 23925 199,4 44 13 21 36 13 96 10.57 8 678 7 496 6 693 8 116 5 682 5 345	9 24091 199.4 43.88 21.14 13.77 10.39 8.514 7.339 6.541 5.968 5.537 6.202	10 24224 199.4 43.69 20.97 13.62 10.25 8.380 7.211 8.417 5.847 5.418 5.085	24426 199.4 43.38 20.70 13.38 10.03 8.176 7.015 6.227 5.661 5.236 4.906	1% 24630 199.4 43.08 20.44 13.15 9.814 7.968 6.814 6.032 5.471 5.049 4.721	20 24836 199.4 42.78 20.17 12.90 9.589 7.754 8.608 5.832 6.274 4.855 4.530	26 24960 199 5 42 59 20 00 12 76 9 451 7.623 8.482 5.708 5.153 4.736 4.412	26044 199 5 42 47 19.89 12.66 9.358 7.534 6.396 5.625 5.071 4.654 4.331	25211 199 5 42 21 19 67 12 45 9 170 7 354 6 222 5 454 4 907 4 488 4 165	75 26295 199 6 42 09 19 55 12 35 8 074 7 263 6 133 5 367 4 816 4 402 4 080	100 26337 199 5 42.02 19 50 12 30 9 026 7 217 6 088 5 322 4 772 4 358 4 037	150 25380 199 5 41 96 19 44 12 25 8 977 7 170 6 042 5 278 4 728 4 315 3 993	25464 199 5 41 83 19 32 12 14 8 879 7.076 5 951 5 188 4 639 4 226 3 904
3 4 5 6 7 8 9 0 1 2 3	16211 198 5 55 55 31 33 22 78 18.63 16.24 14.89 13.61 12.83 12.23 11.75 11.37	20000 199 0 49 80 26 28 18 31 14 54 12 40 11 04 10 11 9 427 8 912 8 510 8 186	3 21615 199 2 47 47 24 26 16 53 12 92 10.88 9.596 8 717 8.081 7 600 7 226 6 926	22500 199 2 46 19 23 15 15.56 12.03 10.05 8.805 7 966 7.343 6.881 6.521 6.233	23056 199.3 46.39 22.46 14.94 11.46 9.522 8.302 7.471 6.872 6.422 6.071 5.791	23437 199 3 44 84 21 97 14 51 11 07 9 155 7 952 7 134 6 545 6 102 5 757 5 482	23715 199 4 44 43 21 62 14 20 10 79 8.885 7 694 6.885 6 302 5 865 5.525 5 253	0 995  23925 199.4 44 13 21 36 13 96 10.57 8 678 7 496 6 693 8 116 5 682 5 345 5 076	9 24091 199.4 43.88 21.14 13.77 10.39 8.514 7.339 6.541 5.968 5.537 6.202 4.935	10 24224 199.4 43.69 20.97 13.62 10.25 8.380 7.211 6.417 5.847 5.418 5.085 4.820	12 24426 199.4 43.39 20.70 13.38 10.03 8.176 7.015 6.227 5.661 5.236 4.906 4.643	1% 15 24630 199.4 43.08 20.44 13.15 9.814 7.968 6.814 8.032 5.471 5.049 4.727 4.460	7 = 90  20  24836 199.4 42.78 20.17 12.90 9.589 7.754 8.608 5.832 6.274 4.855 4.530 4.270	26 24960 199 5 42 59 20 00 12 76 9 451 7.623 8.482 5.708 5.153 4.736 4.412 4 153	25044 199 5 42 47 19 89 12 66 9 358 7 534 6 396 5 625 5 071 4 654 4 331 4 073	\$0 25211 199.5 42.21 19.67 12.45 9170 7.354 6.222 5.454 4.902 4.488 4.165 3.908	76 26295 1995 42 09 19 56 12 35 9 074 7 263 6 133 5 367 4 816 4 402 4 080 3 823	100 25337 1995 42.02 19 50 12 30 9 026 7 217 6 088 5 322 4 772 4 359 4 037 3 780	150 25380 199 5 41 96 19 44 12 25 8 977 7 170 6 042 5 278 4 728 4 315 3 993 3 736	25464 199 5 41 83 19 32 12 14 8 879 7.076 5 951 5 188 4 639 4 226 3 904 3 647
3 4 6 7 8 8 1 2 2 4	16211 198 5 55 55 31 33 22 78 18.63 16.24 14.89 13.61 12.83 12.23 11.75 11.37 11.06	200000 199 0 49 80 26 28 18 31 14 54 12 40 11 04 10 11 9 427 8 912 8 510 8 186 7 922	3 21615 199 2 47 47 24 26 16 53 12 92 10.88 9.596 8 717 8.081 7 600 7 226 6 926 6 680	22500 199 2 46 19 23 15 15.56 12.03 10.05 8.805 7.966 7.343 6.881 6.521 6.233 5.998	23056 199.3 46.39 22.46 14.94 11.46 9.522 8.302 7.471 6.872 6.422 6.071 5.791 5.562	6 23437 199 3 44 84 21 97 14 51 11 07 9 155 7 952 7 134 6 545 6 102 5 757 5 482 5 257	23715 199 4 44 43 21 62 14 20 10 79 8 885 7 694 6 885 6 302 5 865 5 253 5 031	0 995  23925 199.4 44 13 21 36 13 96 10.57 8 678 7 496 6 693 8 116 5 682 5 345 5 076 4 857	9 24091 199.4 43.88 21.14 13.77 10.39 8.514 7.339 6.541 8.968 5.537 6.202 4.935 4.717	10 24224 199.4 43.69 20.97 13.62 10.25 8.380 7.211 6.417 5.847 5.418 5.085 4.820 4.603	12 24426 199.4 43.39 20.70 13.38 10.03 8.176 7.015 6.227 5.661 5.236 4.906 4.643 4.428	1% 156 24630 199.4 43.08 20.44 13.15 9.814 7.968 6.814 8.032 5.471 5.049 4.721 4.460 4.247	7 = 90  20  24836 199.4 42.78 20.17 12.90  9.589 7.754 8.608 5.832 6.274  4.855 4.530 4.270 4.059	24960 199 5 42 59 20 00 12 76 9 451 7.623 8.482 5.708 5.153 4.736 4.412 4 153 3 942	25044 199 5 42 47 19.89 12 66 9 358 7 534 6 396 5 625 5 071 4 654 4 331 4 073 3 862	\$0 25211 199 5 42 21 19 67 12 45 9 170 7 354 6 222 5 454 4 902 4 488 4 165 3 908 3 698	76 26295 1995 42 09 19 56 12 35 9 074 7 263 6 133 5 367 4 816 4 402 4 080 3 823 3 612	100 25337 1995 42.02 19 50 12 30 9 026 7 217 6 088 5 322 4 772 4 358 4 037 3 780 3 569	25380 199 5 41 96 19 44 12 25 8 977 7 170 6 042 5 278 4 728 4 315 3 993 3 736 3 525	25464 199 5 41 83 19 32 12 14 8 879 7.076 5 951 5 188 4 639 4 226 3 904 3 647 3 436
2 3 4 6 7 8 9 0 1 2 2 4 6	16211 198 5 55 56 31 33 22 78 18.63 16.24 14.89 13.61 12.83 11 75 11.37 11.06 10.80	20000 199 0 49.80 26 28 18.31 14.54 10.11 9.427 8.912 8.510 8.186 7.922 7.701	3 21615 199 2 47 47 24 26 16 53 12 92 10.88 9.596 8 717 8 081 7 600 7 226 6 926 6 680 6 476	22500 199 2 46 19 23 15 15.56 12.03 10.05 8.805 7.966 7.343 6.881 6.521 6.233 5.998 5.803	23056 199.3 46.39 22.46 14.94 11.46 9.522 8.302 7.471 6.872 6.422 6.071 5.791 5.562 6.372	23437 199 3 44 84 21 97 14 51 11 07 9 155 7 952 7 134 6 545 6 102 5 757 5 482 5 257 6 071	23715 199 4 44 43 21 62 14 20 10 79 8.885 7 694 6.885 6.302 5.965 5.526 5.525 5.031 4.847	0 995 23925 199.4 44 13 21 36 13 96 10.57 8 678 7 496 6 693 8 116 5 682 5 345 5 076 4 .957 4 .674	24091 199.4 43.88 21.14 13.77 10.39 8.514 7.339 6.541 5.968 5.537 6.202 4.935 4.717 4.536	10 24224 199.4 43.69 20.97 13.62 10.25 8.380 7.211 6.417 5.847 5.418 5.085 4.820 4.603 4.424	24426 199.4 43.38 20.70 13.38 10.03 8.176 7.015 6.227 5.661 5.236 4.906 4.643 4.428 4.250	1% 24630 199.4 43.08 20.44 13.15 9.814 7.968 6.814 6.032 5.471 5.049 4.721 4.460 4.247 4.070	7 = 90  20  24836 199.4 42.78 20.17 12.90 9.569 7.754 8.608 5.832 6.274 4.855 4.530 4.270 4.059 3.883	24960 199 5 42 59 20 00 12 76 9 451 7.623 8.482 5.708 5.153 4.736 4.412 4 153 3 942 3.766	25044 199 5 42 47 19 89 12 66 9 358 7 534 6 396 5 625 5 071 4 654 4 331 4 073 3 862 3 687	25211 199 5 42 21 19 67 12 45 9 170 7 354 6 222 5 454 4 902 4 488 4 165 3 908 3 698 3 523	75 26295 199 5 42 09 19 55 12 35 9 074 7 263 6 133 5 367 4 816 4 402 4 080 3 823 3 612 3 437	100 25337 199 5 42.02 19 50 12 30 9 026 7 217 6 088 5 322 4 772 4 359 4 037 3 569 3 394	25380 199 5 41 96 19 44 12 25 8 977 7 170 6 042 5 278 4 728 4 315 3 993 3 736 3 525 3 350	25464 199 5 41 83 19 32 12 14 8 879 7.076 5 951 5 188 4 639 4 226 3 904 3 647 3 436 3 260
1 2 3 4 5 6 7 8 9 0 1 2 2 3 4 5 6	16211 198 5 55 56 31 33 22 78 18.63 16.24 14.89 13.61 12.83 12.23 11 75 11.37 11.06 10.80	20000 198 0 49 80 26 28 18 31 14 54 12 40 11 04 10 11 9 427 8 912 8 510 8 186 7 922 7 701 7 514	3 21615 199 2 47 47 24 26 16 53 12 92 10.88 9.596 8 717 8.081 7 600 7 226 6 926 6 880 6 476 6 303	22500 199 2 46 19 23 15 15.56 12.03 10.05 8.805 7 966 7.343 6.881 6.521 6.233 5.998 5.803	\$ 23056 199.3 46.39 22.46 14.94 11.46 9.522 8.302 7.471 6.872 6.422 6.071 5.791 5.562 6.372 5.212	23437 199 3 44 84 21 97 14 51 11 07 9 165 7 952 7 134 6 545 6 102 5 757 5 482 5 257 6 071 4 913	23715 199 4 44 43 21 62 14 20 10 79 8.885 7 694 6.885 6 302 5.865 5.525 5 253 5.031 4.847 4 692	0 995  23925 199,4 44 13 21 36 13 96 10.57 8 678 7 496 6 693 8 116 5 682 5 345 5 076 4 957 4 674 4,521	24091 199.4 43.88 21.14 13.77 10.39 8.514 7.339 6.541 5.968 5.537 6.202 4.935 4.717 4.536 4.384	10 24224 199.4 43.69 20.97 13.62 10.25 8.380 7.211 6.417 5.847 5.418 5.085 4.820 4.803 4.424 4.272	24426 199.4 43.38 20.70 13.38 10.03 8.176 7.015 6.227 5.661 5.236 4.906 4.643 4.428 4.250	1% 24630 199.4 43.08 20.44 13.15 9.814 7.968 6.814 6.032 5.471 5.049 4.721 4.460 4.247 4.070 3.920	7 = 90 20 24836 199.4 42.78 20.17 12.90 9.589 7.754 8.608 5.832 6.274 4.855 4.530 4.270 4.059 3.863 3.734	24960 199 5 42 59 20 00 12 76 9 451 7.623 8.482 5.708 5.153 4.736 4.412 4 153 3 942 3.766 3.618	25044 199 5 42 47 19 89 12 66 9 358 7 534 6 396 5 625 5 071 4 654 4 331 4 073 3 862 3 687 3 539	90 25211 199 5 42 21 19 67 12 45 9 170 7 354 6 222 5 454 4 907 4 488 4 165 3 908 3 698 3 523 3 376	76 26295 199 5 42 09 19 56 12 35 9 074 7 263 6 133 5 367 4 816 4 402 4 080 3 823 3 612 3 437 3 290	100 25337 199 5 42 02 19 50 12 30 9 026 7 217 6 088 5 322 4 772 4 359 4 037 3 780 3 569 3 394 3 246	25380 199 5 41 96 19 44 12 25 8 977 7 170 6 042 5 278 4 728 4 315 3 993 3 736 3 525 3 350 3 202	25464 199 5 41 83 19 32 12 14 8 879 7.076 5 951 5 188 4 639 4 226 3 904 3 647 3 436 3 260 3 112
1 2 3 4 5 6 7 8 9 0 1 2 2 9 6 5 6 7	16211 198 5 55 55 31 33 22 78 18.63 16.24 14.89 13.61 12.83 11.75 11.37 11.06 10.80 10.58	2 20000 199 0 49 80 26 28 18 31 14 54 10 11 04 10 11 9 427 8 912 8.510 8 186 7 922 7 701 7 514 7 354	3 21615 199 2 47 47 24 26 16 53 12 92 10.88 9.596 8 717 8.081 7 600 7 226 6 880 6 476 6 303 6 156	22500 199 2 46 19 23 15 15.56 12.03 10.05 8.805 7 966 7.343 6.881 6.521 6.233 5.998 5.803 5.638 5.497	\$ 23056 199.3 46.39 22.46 14.94 11.46 9.522 8.302 7.471 6.872 6.422 6.071 5.791 5.562 6.372 5.212 5.075	6 23437 199 3 44 84 21 97 14 51 11 07 9 155 7 952 7 134 6 545 6 102 5 757 5 482 5 257 6.071 4 913 4 779	23715 199 4 44 43 21 62 14 20 10 79 8 885 7 694 6 885 6 302 5 865 5 253 5 031 4 847 4 692 4 569	0 995  23925 199,4 44 13 21 36 13 96 10.57 8 678 7 496 6 693 8 116 5 682 5 345 5 076 4 857 4 874 4,521 4 389	9 24091 199.4 43.88 21.14 13.77 10.39 8.514 7.339 6.541 5.968 5.537 6.202 4.935 4.717 4.536 4.384 4.254	10 24224 199.4 43.69 20.97 13.62 10.25 8.380 7.211 6.417 5.847 5.418 5.085 4.820 4.803 4.424 4.272 4.142	12 24426 199.4 43.39 20.70 13.38 10.03 8.176 7.015 6.227 5.661 5.236 4.906 4.643 4.428 4.250 4.099 3.971	1% 156 24630 199.4 43.08 20.44 13.15 9.814 7.968 6.814 8.032 5.471 5.049 4.721 4.460 4.247 4.070 3.920 3.793	7 = 90  20  24836 199.4 42.78 20.17 12.90 9.589 7.754 8.608 5.832 6.274 4.855 4.530 4.270 4.059 3.863 3.734 3.607	24960 199 5 42 59 20 00 12 76 9 451 7.623 8.482 5.708 5.153 4.736 4.412 4 153 3 942 3.766 3.618 3.492	25044 199 5 42 47 19 89 12 66 9 358 7 534 6 396 5 625 5 071 4 654 4 331 4 073 3 862 3 687 3 539 3 412	\$0 25211 199 5 42 21 19 67 12 45 9 170 7 354 6 222 5 454 4 907 4 488 4 165 3 908 3 698 3 523 3 375 3 248	76 26295 1995 42 09 19 56 12 35 9 074 7 263 6 133 5 367 4 816 4 402 4 080 3 823 3 612 3 437 3 290 3 163	100 25337 1995 42.02 19 50 12 30 9 026 7 217 6 088 5 322 4 772 4 359 4 037 3 780 3 569 3 394 3 246 3 119	150 25380 199 5 41 96 19 44 12 25 8 977 7 170 6 042 5 278 4 728 4 315 3 993 3 736 3 525 3 350 3 202 3 075	25464 199 5 41 83 19 32 12 14 8 879 7.076 5 951 5 188 4 639 4 226 3 904 3 647 3 436 3 260 3 112 2 984
1 2 3 4 5 6 7 8 6 7 8	16211 198 5 55 55 31 33 22 78 18.63 16.24 14.89 13.61 12.83 11.75 11.37 11.06 10.80 10.58 10.38 10.22	2 20000 199 0 49.80 26 28 18.31 14.54 12.40 11 04 10.11 9.427 8.912 8.510 8.186 7.922 7.701 7.514 7.354 7.215	3 21615 199 2 47 47 24 26 16 53 12 92 10.88 9.596 8 717 8.081 7 600 7 226 6 880 6 476 6 303 8 156 6.028	22500 199 2 46 19 23 15 15.56 12.03 10.05 8.805 7.966 7.343 6.881 6.521 6.233 5.998 5.803 5.638 5.497 5.375	6 23056 199.3 46.39 22.46 14.94 11.46 9.522 8.302 7.471 6.872 6.422 6.071 5.791 5.562 6.372 5.212 5.075 4.956	6 23437 199 3 44 84 21 97 14 51 11 07 9 155 7 952 7 134 6 545 6 102 5 757 5 482 5 257 6 071 4 913 4 779 4 663	23715 199 4 44 43 21 62 14 20 10 79 8 885 7 694 6 885 6 302 5 865 5 253 5 031 4 847 4 692 4 4559 4 445	0 995  23925 199.4 44 13 21 36 13 96 10.57 8 678 7 496 6 693 8 116 5 682 5 345 5 076 4 857 4 874 4,521 4 389 4 276	9 24091 199.4 43.88 21.14 13.77 10.39 8.514 7.339 6.541 5.968 5.537 6.202 4.935 4.717 4.536 4.384 4.254 4.141	10 24224 199.4 43.69 20.97 13.62 10.25 8.380 7.211 6.417 5.847 5.418 5.085 4.820 4.803 4.424 4.272 4.142 4.030	12 24426 199.4 43.39 20.70 13.38 10.03 8.176 7.015 6.227 5.661 5.236 4.906 4.643 4.428 4.250 4.099 3.971 3.860	1% 24630 199.4 43.08 20.44 13.15 9.814 7.968 6.814 6.032 5.471 5.049 4.721 4.460 4.247 4.070 3.920 3.793 3.683	7 = 90  24836 199.4 42.78 20.17 12.90 9.589 7.754 8.608 5.832 6.274 4.855 4.530 4.270 4.059 3.883 3.734 3.607 3.498	24960 199 5 42 59 20 00 12 76 9 451 7.623 8.482 5.708 5.153 4.736 4.412 4 153 3 942 3.766 3.618 3.492 3.382	25044 199 5 42 47 19.89 12 66 9 358 7 534 6 396 5 625 5 071 4 654 4 331 4 073 3 862 3 687 3 539 3 412 3 303	\$0 25211 199 5 42 21 19 67 12 45 9 170 7 354 6 222 5 454 4 902 4 488 4 165 3 908 3 523 3 375 3 248 3 139	76 26295 199 56 42 09 19 56 12 35 8 074 7 263 6 133 5 367 4 816 4 402 4 080 3 823 3 612 3 437 3 290 3 163 3 053	100 25337 1995 42.02 19 50 12 30 9 026 7 217 6 088 5 322 4 772 4 358 4 037 3 780 3 569 3 394 3 246 3 119 3 009	25380 199 5 41 96 19 44 12 25 8 977 7 170 6 042 5 278 4 728 4 315 3 993 3 736 3 525 3 350 3 202 3 075 2 985	25464 199 5 41 83 19 32 12 14 8 879 7.076 5 951 5 188 4 639 4 226 3 904 3 647 3 436 3 260 3 112 2 984 2 873
1 2 3 4 5 6 7 8 8 7 8 8	16211 198 5 55 56 31 33 22 78 18.63 16.24 14.89 12.83 12.23 11.37 11.06 10.80 10.58 10.38 10.22 10.07	2 20000 199 0 49.80 26 28 18.31 14.54 12.40 11.04 10.11 9.427 8.912 8.510 8.186 7.922 7.701 7.514 7.354 7.215 7.093	3 21615 199 2 47 47 24 26 16 53 12 92 10.88 9.596 8 717 8 081 7 600 7 226 6 926 6 680 6 476 6 303 8 156 6 028 5 916	22500 199 2 46 19 23 15 15.56 12.03 10.05 8.805 7.966 7.343 6.881 6.521 6.233 5.998 5.803 5.638 5.497 5.375 5.268	6 23056 199.3 46.39 22.46 14.94 11.46 9.522 8.302 7.471 6.872 6.422 6.071 5.791 5.562 5.372 5.212 5.075 4.956 4.853	6 23437 199 3 44 84 21 97 14 51 11 07 9 155 7 952 7 134 6 545 6 102 5 757 5 482 5 257 6.071 4 913 4 779 4 663 4 561	23715 199 4 44 43 21 62 14 20 10 79 8 885 6 302 5 865 5 253 5 031 4 847 4 692 4 559 4 445 4 345	0 995  23925 199.4 44 13 21 36 13 96 10.57 8 678 7 496 6 693 8 116 5 682 5 345 5 076 4 857 4 874 4 521 4 389 4 276 4.177	9 24091 199.4 43.88 21.14 13.77 10.39 6.541 5.968 5.537 6.202 4.935 4.717 4.536 4.384 4.254 4.141 4.043	10 24224 199.4 43.69 20.97 13.62 10.25 8.380 7.211 6.417 5.847 5.418 5.085 4.820 4.603 4.424 4.272 4.142 4.030 3.933	12 24426 199,4 43 38 20 70 13 38 10 03 8.176 7.015 6.227 5.661 5.236 4.906 4.643 4.428 4.250 4.098 3.971 3.860 3.763	1% 24630 199.4 43.08 20.44 13.15 9.814 9.814 6.814 6.032 5.471 5.049 4.721 4.460 4.247 4.070 3.920 3.793 3.683 3.587	7 = 90  24836 199.4 42.78 20.17 12.90 9.589 7.754 8.608 5.832 6.274 4.855 4.530 4.270 4.059 3.883 3.734 3.607 3.498 3.402	24960 1995 4259 2000 1276 9 451 7.623 8.482 5.708 5.153 4.736 4.412 4 153 3 942 3.766 3.618 3.492 3.382 3.287	25044 199 5 42 47 19.89 12 66 9 358 7 534 6 396 5 625 5 071 4 654 4 073 3.862 3 687 3 539 3 412 3 303 3 208	\$0 25211 199 5 42 21 19 67 12 45 9 170 7 354 6 222 5 454 4 902 4 488 4 165 3 908 3 598 3 523 3 375 3 248 3 139 3 043	76 26295 1995 4209 1956 1235 9074 7263 6133 5367 4816 4402 4080 3.823 3.612 3.437 3.290 3.163 3.053 2.957	100 25337 1995 42.02 19 50 12 30 9 026 7 217 6 088 5 322 4 772 4 359 4 037 3 780 3 569 3 394 3 246 3 119 3 009 2 913	25380 199 6 41 96 19 44 12 25 8 977 7 170 6 042 5 278 4 728 4 315 3 993 3 736 3 525 3 350 3 202 3 075 2 965 2 868	25464 199 5 41 83 19 32 12 14 8 879 7.076 5 951 5 188 4 639 4 226 3 904 3 647 3 436 3 260 3 112 2 984 2.873 2 776
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	16211 198 5 55 56 31 33 22 78 18.63 16.24 14.89 13.61 12.83 11.37 11.06 10.80 10.58 10.22 10.07 9.944 9.630 9.727 9.635	2 20000 199 0 49.80 26 28 18.31 14.54 12.40 11 04 10.11 9.427 8.912 8.510 8.186 7.922 7.701 7.514 7.215 7.093 6.986 6.891 6.891 6.891 6.891 6.730	3 21615 199 2 47 47 24 26 16 53 12 92 10.88 9 596 8 717 8 081 7 600 7 226 6 680 6 476 6 303 6 156 6 028 5 916 5 818 5 730 5 652 5 582	6 22500 199 2 46 19 23 15 15.56 12.03 10.05 8.805 7.966 7.343 6.881 6.521 6.233 5.998 5.803 5.497 5.375 5.268 5.174 5.017 4.950	6 23056 199.3 46.39 22.46 14.94 11.46 9.522 8.302 7.471 6.872 6.422 6.071 5.791 5.562 6.372 5.212 5.075 4.956 4.953 4.762 4.681 4.609 4.544	6 23437 199 3 44 84 21 97 14 51 11 07 9 155 7 952 7 134 6 545 6 102 5 757 5 482 5 257 6.071 4 913 4 779 4 663 4 561 4 472 4.393 4 322	23715 199 4 44 43 21 62 14 20 10 79 8 885 6 302 5 865 5 253 5 031 4 847 4 692 4 454 4 257 4 179 4 109 4 047	0 995  23925 199.4 44 13 21 36 13 96 10.57 8 678 7 496 6 693 8 116 5 682 5 345 5 076 4 .857 4 .874 4 .521 4 .389 4 .276 4 .177 4 .090 4 013 3 944 3 882	9 24091 199.4 43.88 21.14 13.77 10.39 8.514 7.339 6.541 5.968 5.537 6.202 4.935 4.717 4.536 4.384 4.254 4.141 4.043 3.956 3.880 3.812 3.750	10 24224 199.4 43.69 20.97 13.62 10.25 8.380 7.211 6.417 5.847 5.418 5.085 4.820 4.603 4.424 4.272 4.142 4.030 3.933 3.847 3.771 3.703 3.642	12 24426 199,4 43 39 20 70 13 38 10 03 8.176 7.015 6.227 5.661 5.236 4.906 4.643 4.428 4.250 4.099 3.971 3.860 3.763 3.678 3.678 3.678	1% 24630 199.4 43.08 20.44 13.15 9.814 9.814 6.814 6.032 5.471 5.049 4.721 4.460 4.247 4.070 3.920 3.793 3.683 3.587 3.502 3.427 3.360 3.300	7 = 90  24836 199.4 42.78 20.17 12.90 9.589 7.754 8.608 5.832 6.274 4.855 4.530 4.270 4.059 3.883 3.734 3.607 3.498 3.402 3.318 3.243 3.176 3.116	24960 1995 4259 2000 1276 9 451 7.623 8.482 5.708 5.153 4.736 4.412 4 153 3 942 3.766 3.618 3.492 3.382 3.287 3.203 3 128 3.061 3.001	25044 199 5 42 47 19.89 12 66 9 358 7 534 8 396 5 625 5 071 4 654 4 331 4 073 3.862 3 687 3 539 3 412 3 303 3 208 3 123 3 049 2 982 2 922	\$0 25211 199 5 42 21 19 67 12 45 9 170 7 354 6 222 5 454 4 902 4 488 4 165 3 908 3 598 3 523 3 375 3 248 3 139 3 043 2 959 2 884 2 817 2 756	76 26295 1995 4209 1955 1235 9074 7263 6133 5367 4816 4402 4080 3.823 3.612 3437 3290 3163 3053 2957 2872 2797 2730 2669	100 25337 1995 42.02 19 50 12 30 9 026 7 217 6 088 5 322 4 772 4 358 4 037 3 780 3 569 3 394 3 246 3 119 3 009 2 913 2 828 2 753 2 686 2 624	25380 199 6 41 96 19 44 12 25 8 977 7 170 6 042 5 278 4 728 4 728 4 315 3 393 3 736 3 525 3 350 3 202 3 075 2 965 2 868 2 783 2 707 2 640 2 579	25464 199 5 41 83 19 32 12 14 8 879 7.076 5 951 5 188 4 639 4 226 3 904 3 647 3 436 3 260 3 112 2 984 2.873 2 776 2 690 2 614 2 545 2 484

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8 118 5.490 4 453 3 878 3.508

7 879 5.298 4.279 3.715 3.350

4 150 3 939 3.776 3.645 3.537

3 949 3 742 3 580 3.450 3.344

3.812 3.607 3 447 3.318 3.212

3 713 3 509 3 350 3.222 3.117

3,579 3 376 3.219 3.092 2.988

3.325 3.127 2.972 2.847 2.744

3.091 2.897 2 744 2.621 2.519

3.407 3.208 3.052 2.927

3.245 3 048 2 894 2.770

7	0 999	aR = 014	a; 0.2%	າ 99.8%
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The values for it, 1 should be multiplied by 10

27	1 1	2	3	4	5	6	7		9	10	12	15	20	25	30	50	75	100	15ù	. Ans	DI.
1	40528	50000	54038	56250	57640	58594	59287	59814	60228	60562	61067	61576	62091	62402	62610	63029	63239	63344	63450	63662	
2	998.5	999.0	999.2	999.3	999.3	999.3	999.4	999.4	999.4	999.4	999.4	999 4	999.4	999.5	999 5		999 5		999.5	999 5	2
3	167.0	148.5	141.1	137 1	134.6	132.8	131.6	130.6	129.9	129.2	128.3	127.4	126.4	125.6	125.4	124.7	124 3	124.1	123 9	123.5	3
4	74.14	61.25	56.18	53.44	61.71	50 53	49.66	49.00	48.47	48.05	47.41	46,76	46.10	45 70	45.43	44.88	44.61	44.47	44.33	44 05	4
5	47 18	37 12	33.20	31 08	29.75	28.83	28.16	27.65	27 24	26.92	26.42	25.91	25.39	25.08	24 87	24 44	24.22	24.12	24.01	23.79	5
6	35.51	27.00	23.70	21.92	20.80	20,03	19.46	19.03	18.69	18.41	17.99	17.56	17.12	16.85	16.67	16.31	16 12	16.03	15.93	15 75	6
7	29 25	21 69	18.77	17.20	16.21	15.52	15.02	14 63	14.33	14.08	13.71	13.32	12 93	12.69	12 53	12.20	12.04	11 95	11.87	11 2D	7
8	25.41	18.49	15.83	14.39	13.48	12.86	12.40	12.05	11.77	11.54	11.19	10.84	10.48	10.28	10.11	9.804	9.650	0.571	9.493	8 3 14	8
9	22 86	16.39	13.90	12.56	11.71	11 13	10 70	10.37	10.11	9.894	9.570	9.238	8.898	8.689	8.548	8.260	0.113	8.039	7 964	7 813	9
10	21.04	14.91	12.66	11.28	10.48	9.926	P.517	9.204	8.966	8.754	8.445	8.129	7.804	7.604	7.469	7 193	7 052	6.980	6.908	6 762	10
21	19.69	13,81	11.56	10.35	9.578	9.047	8.655	8.355	B.116	7.922	7 626	7 321	7.008	6.815	6.684	6.416	6.280	6.210	6,140	5 998	11
12	18 64	12 97	10.80	9 633	8 892	8379	8 00 1	7 710	7.480	7.292	7 005	6 709	6 405	6.217	6 090	5 829	5 695	5 627	5 559	5.420	12
13	17.82	12.31	10.21	9.073	8,354	7.856	7.489	7.206	6.962	6.799	6.519	6.231	5.934	5.751	5.626	5.370	5.239	5.172	5.104	4.967	13
14	17.14	11.78	9.729	8.622	7.922	7.436	7.077	6.802	6.583	5.404	6.130	5,848	5.557	5.377	5.254	5.002	4.873	4.807	4.740	4 604	14
15	16 59	11.34	9.335	8.253	7.567	7 092	6.741	8.471	6.258	6.061	5.812	5.535	6.248	5.071	4.950	4 702	4.573	4.508	4.442	4 30 2	15
16	16.12	10.97	9.006	7.944	7.272	6.805	6.460	6.195	5.984	5.612	5.547	5,274	4.892	4.817	4 697	4.461	4 324	4 259	4 193	4 059	16
17	15.72	10.66	8.727	7.683	7.022	8.562	6.223	5.962	5.754	5.584	5 324	5.054	4.775	4.602	4.484	4.239	4.113	4,048	3.983	3 850	17
18	15,38	10.39	9.487	7.459	6.808	6.355	6.021	5.763	5.558	5.390	5 132	4.866	4.500	4,418	4.301	4 058	3.933	3.868	3.803	1670	8
19	15 08	10.16	8.280	7.205	6.622	6.175	5.845	5.590	5.388	5.222	4 967	4.704	4.430	4.259	4,143	3.902	3.777	3.713	3.647	3.514	19
20	14.82	9.963	890.8	7.096	6.461	6.019	5.692	5.440	5.239	5.075	4.823	4,562	4.290	4.121	4.005	3.785	3.640	3.576	3.511	3 378	20
21	14.59	9.772	7 93B	6.847	6.318	5.881	5.557	5.308	5.109	4.948	4 696	4 437	4.167	3 999	3.884	3.645	3 520	3.456	3 391	3.257	21
22	14.38	9.612	7 798	6.814	6.191	5.758	6.438	5.190	4 993	4.832	4 583	4.326	4.058	3.891	3.776	3.538	3,413	3.349	3 284	3 151	22
23	14.20	9.469	7.669	6.696	6.078	5.649	6.331	5.085	4.890	4.730	4 483	4.227	3.961	3.794	3.680	3.442	3.318	3,254	3.189	3.055	20
24	14.03	9.339	7 554	6.589	5.977	5.550	5.235	4.991	4.797	4.638	4 393	4.139	3.873	3.707	3.593	3 356	3.232	3.168	3.103	2 960	24
26	13 88	9.223	7.451	6.493	5.885	6.462	5.148	4.905	4.713	4 555	4 312	4.059	3.794	3.629	3.515	3.279	3.154	3.001	3.025	2 890	25
30	13.29	8,773	7.054	6.125	5.534	5.122	4.817	4 581	4.393	4.239	4 001	3.753	3.493	3.330	3.217	2 981	2.857	2 782	2 726	2 589	30
35	12 90	8.470	6.787	5.876	5.298	4.894	4 595	4.363	4.178	4.027	3 792	3.547	3.290	3.128	3.018	2.781	2.655	2 590	2.523	2 383	35
40	12.61	8.251	6.595	5,698	5.128	4.731	4 436	4.207	4.024	3.874	3.642	3.400	3.145	2.984	2.872	2.638	2 510	2.444	2.376	2 232	40
50	12.22	7.956	0.336	5.459	4.901	4.512	4.222	3.998	3.818	3.671	3.443	3.204	2 951	2.790	2 679	2.441	2.313	2.246	2.176	2 26	50
75	11.73	7 585	6.01	5 159	4 617	4 237	3 955	3 736	3 561	1416	3 192	2 957	2 707		2 435	2 194	2 062		197	1.754	75
100	11.50	7.408	5.857	5.017	4 482	4 107	3.829	3.612	3.439	3.296	3 074	2.840	2 501	2.431	2 319	2.076	1 940	1.867	1 790	815	200
150	11.27	7.236	6.707	4.879	4.361	3.981	3 706	3 493	3.321	3.179	2 959	2.727	2.479		2 206		1 820	1.744	1.882	46	150
00	10.83	6 908	5 422	4 617	4 103	3 743	3 4 7 5	3 266	3.097	2 959	2 742	2 513	2.266	2 105	1 990	1 /33	1 581	1 494	1 395	(1.0	ex.
														7-7	***		-3.0			1.0	

4 09999 a. 001% a 002 y = 9998

The values for x 1 should be multiplied by 1000

100	1	5	3	4	6	0	7	8	9	10	12	15	20	25	30	50	75	100	150	ort	V3 /
1	40528	20000	54038	56250	57640	58594	59287	59814	60228	60562	6 Ob.7	615 0	(12091	62402	62610	6 50 29	ь3239	63344	6.1450	ь .	7
2	9999	9999	9999	9999	9999	9999	2000	9999	9999	9494	3289	90.99	9999	9099	9999	9999	9999	9999	9999	B99r	
3	784.0	694.7	659.3	640.2	62B.2	6199	613.9	609 3	605 7	602.8	598.3	593.8	589 3	686 5	584.7	581.0	579 1	578.1	577.2	525 ,	ш
4	241.B	198.0	181.0	171 9	166.1	162 2	1593	157.1	155 4	154.0	151.9	149 7	147.5	146.2	145.3	143 5	142 6	142.1	741.7	140 8	ш
6	124.9	97 03	86 29	80 53	76.93	74.43	72.61	71 23	70.13	89 25	67.91	66 54	65 16	84 31	63 76	62 60	62 02	61 73	61 43	60 84	
В	82 49	61 63	53 68	49 42	46 75	44.91	43 57	42.54	41.73	41.08	40.08	39 07	38 04	37.41	36 98	36.13	35 69	35.47	35 25	34 8	
7	62 17	45.13	38 68	35 22	33 06	31 57	30.48	29 64	28 99	28 45	27 64	26 82	25 98	25 48	25.12	24 42	24 06	23 88	23 70	23.34	Ш
8	50.69	38 00	30 46	27 49	25.63	24 36	23 42	22 71	22 14	21 68	20.98	20 27	19 55	19 10	18.80	18 19	17 89	17.73	17.57	7.26	ш
9	43 48	30 34	25 40	22 77	21 11	19 97	19 14	18 50	18 00	17 59	16 97	16 33	15.68	15 28	15 01	14.47	14 19	14 05	13.91	3 62	ш
10	38 58	26 55	22 04	19.63	18.12	17 08	16 32	15.74	15 27	14 90	14 33	13.75	13 15	12.78	12.54	12 03	11.77	11 66	11 51	11 25	1
11	35.06	23.85	19,86	17.42	16.02	15.05	14.34	13.80	13.37	13.02	12.49	11 95	11.39	11.05	10.81	10.34	10.10	9.977	9 854	8 605	П
12	32 43	21.86	17.90	15.79	14.47	13 56	12.89	12 38	11.96	11 65	11.14	10.63	10.10	9.777	9.557	9 108	8.878	8 762	8.644	8 406	Ш
13	30 39	20.31	16 55	14 55	13.29	12.42	11 79	11:30	10 92	10.60	10.12	9.632	9.127	0.816	8.606	8 175	7 954	7 842	7 729	7 500	Ш
14	2B.77		15.49	13 57	12 37	11.53	10.92	10.46	10 09	B 785	9.326	8.853	8.366	8.067	7.864	7 448	7 234	7 126	7 016	6 793	Ш
15	27 45	18 11	14 64	12.78	11 62	10.82	10 23	9 780	9 4 2 2	9 1 3 1	8 686	8 229	2.758	7 468	7.271	6 866	6 658	6 553	6 446	6 229	Ш
16	26.38	17 30	13.93	12 14	11.01	10.23	B.663	9.226	8 878	8 596	8.164	7 720	7 262	6 979	6.787	6 392	6 169	6 086	5.981	5 768	ш
17	25 44	16.82	13.34	11.60	10 50	9 747	9.191	8.765	8.427	8 152	7 730	7 297	6 850	6 573	6 385	5 999	5.799	5.69B	5.595	5 385	ш
18	24 66	6 04	12 85	11 14	10 07	9 335		B 376		7.777	7 365	6 94 1	5 503	6 232	6 047	5 66 7	5 \$ 7 5	5.371	6.270	5 QR	ш
19	23.99	15.55	12.42	10.75	9 706			8.044	7 720	7 457	7 053	6.637	6 207	5.941	5.759	5 385	5.191	5.093	4 993	4 788	ш
20	23 40	15.12	12 05	10.41	9 388	8 679	8.158	7 757	7 439	7 181	6.784	6.375	5.952	5.689	5.510	5 141	4.950	4 852	4 753	4 550	Ш
21	22.89	14.74	11 73	10.12	9.111	8.414	7 901	7 507	7 195	6.940	6.549	6.147	5.729	5.471	5.294	4 929	4 740	4 643	4 545	4 344	П
22		14.41	11.44	9 860	8.867	8 180	7.676	7 288	6 980	6.729	6.343	5.946	5.534	5.279	5.104	4 743	4 555	4 459	4 362	4 162	Ш
23		14.12	11 19	9 630	8 651		7 476		6 789	6 542	6 161	5 769	5 362	5 109	4 936	4 578	4 392	4 29 7	4 200	4 000	Ш
24		13.85	10 96	9 425	9.458		7 298		6.620	6.375	5 999	5.611	5.208	4 958	4 787	4 432	4.247	4 152	4 055	3 857	ш
25	21 34	13 62	10 76	9 240	8 285	7 624	7 138	6 765	6 468	8 226	5.854	5 4 7 0	5 071	4 823	4 653	4 300	4 116	4 022	3 926	3 728	
30		12 72	9 994	B.544	7.632	7 002	6.537	6.180	5.896	5.664	5.308	4 939	4 554	4 314	4 149	3 806	3.625	3 532	3 437	3 240	1
35		12 12	9.487	8.084	7 202	6.592	6.143	5.796	5.521	5.296	4 950	4 591	4.216	3.981	3.819	3.481	3 303	3.210	3.115	2 918	1
10	1000	11 70	9 128	7 759	6.899	6.303	5.864		5.256	5.036	4.697	4.346	3.977	3.746	3.587	3 252	3.074	2 982	2.887	2 686	1
50		11.14	8.652	7 330	6.498		5.497		4 909	4.695	4 368	4.024	3.664	3.438	3 281	2 950	2.773	2 680	2 584	2 380	2
75	16 RB	10 44	8.066	6.802	8.006	5.455	5.048	4 734	4.483	4.278	3 961	3.630	3 281	3.060	2 907	2 578	2 399	2.304	2 205	1 988	Ш
00				6 555	6.777	5.237			4.285	4.084	3.773	3.448	3.104		2 732	2 404	2.223	2 126	2 024	1.730	10
50	15 98	9 800	7 528	6.319	5.558	5 030	4 640	4 338	4.097	3 900	3.594	3.274	2 934	2718	2 566	2 236	2 052	1 953	1 846	1 4 9 7	95
70	15.14	9.210	7.036	5.878	5.149	4 643	4 268	3.978	3.747	3.556	3.261	2 951	2.619	2.406	2.254	1 919	1 724	1.613	487	1.0	. 0

## Critical values for the Kolmogorov-Smirnov goodness-of-fit test (for completely specified distributions)

01	5%	21-9%	1%	-,4
or <sub>3</sub>	10%	5%	2%	1%
17				
1	0.9500	0.9750	0 9900	0 9950
2	0 7784	0 8419	0.9000	0 9293
3	0 6360	0 7076	0 7846	0 8290
4	0.5652	0 6239	0 6889	0 7342
5	0 5094	0 5633	0 6272	0 6685
6	0 4680	0 5193	0 5774	0 6166
7	0.4361	0 4834	0 5384	0 5758
8	0 4096	0 4543	0 5065	0.5418
9	0 3875	0.4300	0 4796	0.5133
10	0 3687	0 4092	0 4566	0 4889
11	0 3524	0.3912	0.4367	0 4677
12	0.3382	0.3754	0.4192	0 4490
13	0 3255	0.3614	0.4036	0.4325
14	0.3142	0.3489	0.3897	0 41 76
15	0 3040	0 3376	0.3771	0 4042
16	0 2947	0 3273	0 3657	0 3920
17	0 2863	0.3180	0 3553	0 3809
18	0 2785	0 3094	0.3457	0 3706
19	0 2714	0 3014	0 3369	0 3612
20	0 2647	0 2941	0 3287	0 3524

22         0 2528         0 2809         0 3139         0 336           23         0 2475         0 2749         0 3073         0 3291           24         0 2424         0 2693         0 3010         0 3221           25         0 2377         0 2640         0 2952         0 3164           26         0 2332         0 2591         0 2896         0 3104           27         0 2290         0 2544         0 2844         0 3054           28         0 2250         0 2499         0 2794         0 299           29         0 2212         0 2457         0 2747         0 294           30         0 2176         0 2417         0 2702         0 289           31         0 2176         0 2417         0 2702         0 289           32         0 2108         0 2342         0 2619         0 280           32         0 2108         0 2342         0 2619         0 280           33         0 2077         0 2308         0 2580         0 276           34         0 2047         0 2242         0 2507         0 269           36         0 1991         0 2212         0 2473         0 265           37					
7 21 0 2586 0 2872 0 3210 0 344; 22 0 2528 0 2809 0 3139 0 336; 23 0 2475 0 2749 0 3073 0 329; 24 0 2424 0 2693 0 3010 0 322; 25 0 2377 0 2640 0 2952 0 3164; 26 0 2332 0 2591 0 2896 0 310; 27 0 2290 0 2544 0 2844 0 305; 28 0 2250 0 2499 0 2794 0 299; 29 0 2212 0 2457 0 2747 0 294; 30 0 2176 0 2417 0 2702 0 289; 31 0 2141 0 2379 0 2660 0 285; 32 0 2108 0 2342 0 2619 0 280; 33 0 2077 0 2308 0 2580 0 276; 34 0 2047 0 2274 0 2543 0 272; 35 0 2018 0 2242 0 2507 0 269; 36 0 1991 0 2212 0 2473 0 265; 37 0 1965 0 2183 0 2440 0 261; 38 0 1939 0 2154 0 2409 0 258; 39 0 1916 0 2127 0 2379 0 255;	α1	5%	2 -5	1%	* , D*.
21         0 2586         0 2872         0 3210         0 344           22         0 2528         0 2809         0 3139         0 336           23         0 2475         0 2749         0 3073         0 3291           24         0 2424         0 2693         0 3010         0 3221           25         0 2377         0 2640         0 2952         0 3164           26         0 2332         0 2591         0 2896         0 3104           27         0 2290         0 2544         0 2844         0 3054           28         0 2250         0 2499         0 2794         0 299           29         0 2212         0 2457         0 2747         0 294           30         0 2176         0 2417         0 2702         0 289           31         0 2141         0 2379         0 2660         0 285           32         0 2108         0 2342         0 2619         0 285           33         0 2077         0 2308         0 2580         0 276           34         0 2047         0 2274         0 2543         0 272           36         0 1991         0 2212         0 2473         0 266           37	02	10%	5%	2%	1%
22         0 2528         0 2809         0 3139         0 336           23         0 2475         0 2749         0 3073         0 3291           24         0 2424         0 2693         0 3010         0 3221           25         0 2377         0 2640         0 2952         0 3166           26         0 2332         0 2591         0 2896         0 3106           27         0 2290         0 2544         0 2844         0 3056           28         0 2250         0 2499         0 2794         0 299           29         0 2212         0 2457         0 2747         0 294           30         0 2176         0 2417         0 2702         0 289           31         0 2146         0 2379         0 2660         0 285           32         0 2108         0 2342         0 2619         0 280           33         0 2077         0 2308         0 2580         0 276           34         0 2047         0 2274         0 2543         0 272           35         0 2018         0 2242         0 2507         0 269           36         0 1991         0 2212         0 2473         0 265           37	n				
23         0 2475         0 2749         0 3073         0 3295           24         0 2424         0 2693         0 3010         0 3225           25         0 2377         0 2640         0 2952         0 3166           26         0 2332         0 2591         0 2896         0 3106           27         0 2290         0 2544         0 2844         0 3056           28         0 2250         0 2499         0 2794         0 299           29         0 2212         0 2457         0 2747         0 2947           30         0 2176         0 2417         0 2702         0 2891           31         0 2141         0 2379         0 2660         0 2851           32         0 2108         0 2342         0 2619         0 2800           33         0 2077         0 2308         0 2580         0 2760           34         0 2047         0 2274         0 2543         0 2720           36         0 1991         0 2242         0 2507         0 2690           36         0 1991         0 2212         0 2473         0 2650           37         0 1965         0 2183         0 2440         0 2409         0 2580 </th <td>21</td> <td>0.2586</td> <td>0 2872</td> <td>0.3210</td> <td>0 3443</td>	21	0.2586	0 2872	0.3210	0 3443
24         0 2424         0 2693         0 3010         0 322           25         0 2377         0 2640         0 2952         0 3164           26         0 2332         0 2591         0 2896         0 3104           27         0 2290         0 2544         0 2844         0 3054           28         0 2250         0 2499         0 2794         0 2994           29         0 2212         0 2457         0 2747         0 294           30         0 2176         0 2417         0 2702         0 289           31         0 2141         0 2379         0 2660         0 285           32         0 2108         0 2342         0 2619         0 2800           33         0 2077         0 2308         0 2580         0 2760           34         0 2047         0 2274         0 2543         0 2720           35         0 2018         0 2242         0 2507         0 2690           36         0 1991         0 2212         0 2473         0 2650           37         0 1965         0 2183         0 2440         0 2613           38         0 1939         0 2154         0 2409         0 2580           39	22	0 2528	0 2809	0 3139	0 3367
26         0 2377         0 2640         0 2952         0 3164           26         0 2332         0 2591         0 2896         0 3104           27         0 2290         0 2544         0 2844         0 3056           28         0 2250         0 2499         0 2794         0 299           29         0 2212         0 2457         0 2747         0 294           30         0 2176         0 2417         0 2702         0 2893           31         0 2141         0 2379         0 2660         0 2853           32         0 2108         0 2342         0 2619         0 2803           33         0 2077         0 2308         0 2580         0 2761           34         0 2047         0 2274         0 2543         0 2721           36         0 1991         0 2242         0 2507         0 2693           36         0 1991         0 2212         0 2473         0 2651           37         0 1965         0 2183         0 2440         0 2611           38         0 1939         0 2154         0 2409         0 2582           39         0 1916         0 2127         0 2379         0 2379         0 2555 <td>23</td> <td>0 2475</td> <td>0 2749</td> <td>0.3073</td> <td>0 3295</td>	23	0 2475	0 2749	0.3073	0 3295
26 0 2332 0 2591 0 2896 0 3104 27 0 2290 0 2544 0 2844 0 3054 28 0 2250 0 2499 0 2794 0 299 29 0 2212 0 2457 0 2702 0 2893 30 0 2176 0 2417 0 2702 0 2893 31 0 2141 0 2379 0 2660 0 2853 32 0 2108 0 2342 0 2619 0 2803 33 0 2077 0 2308 0 2580 0 2761 34 0 2047 0 2274 0 2543 0 2721 35 0 2018 0 2242 0 2507 0 2693 36 0 1991 0 2212 0 2473 0 2653 37 0 1965 0 2183 0 2440 0 2611 38 0 1939 0 2154 0 2409 0 2583 39 0 1916 0 2127 0 2379 0 2555	24	0 2424	0 2693	0.3010	0 3229
27         0 2290         0 2544         0 2844         0 3054           28         0 2250         0 2499         0 2794         0 299           29         0 2212         0 2457         0 2747         0 294           30         0 2176         0 2417         0 2702         0 289           31         0 2141         0 2179         0 2660         0 285           32         0 2108         0 2342         0 2619         0 280           33         0 2077         0 2308         0 2580         0 276           34         0 2047         0 2274         0 2543         0 272           36         0 2018         0 2242         0 2507         0 269           36         0 1991         0 2212         0 2473         0 265           37         0 1965         0 2183         0 2440         0 2613           38         0 1939         0 2154         0 2409         0 258           39         0 1916         0 2127         0 2379         0 2379         0 255	25	0.2377	0 2640	0 2952	0.3166
28 0 2250 0 2499 0 2794 0 299 29 0 2212 0 2457 0 2747 0 294 30 0 2176 0 2417 0 2702 0 289 31 0 2141 0 2179 0 2660 0 285 32 0 2108 0 2342 0 2619 0 280 33 0 2077 0 2308 0 2580 0 276 34 0 2047 0 2274 0 2543 0 272 35 0 2018 0 2242 0 2507 0 269 36 0 1991 0 2212 0 2473 0 265 37 0 1965 0 2183 0 2440 0 2613 38 0 1939 0 2154 0 2409 0 258 39 0 1916 0 2127 0 2379 0 255	26	0 2332	0 2591	0 2896	0 3106
29 0 2212 0 2457 0 2747 0 2947 30 0 2176 0 2417 0 2702 0 2899 31 0 2141 0 2379 0 2660 0 2859 32 0 2108 0 2242 0 2619 0 2800 33 0 2077 0 2308 0 2580 0 2760 34 0 2047 0 2274 0 2543 0 2720 35 0 2018 0 2242 0 2507 0 2690 36 0 1991 0 2212 0 2473 0 2650 37 0 1965 0 2183 0 2440 0 2611 38 0 1939 0 2154 0 2409 0 2580 39 0 1916 0 2127 0 2379 0 2555	27	0 2290	0 2544	0 2844	0.3050
30 0 2176 0 2417 0 2702 0 2899 31 0 2141 0 2379 0 2660 0 2853 32 0 2108 0 2342 0 2619 0 2803 33 0 2077 0 2308 0 2580 0 2761 34 0 2047 0 2274 0 2543 0 2721 35 0 2018 0 2242 0 2507 0 2690 36 0 1991 0 2212 0 2473 0 2651 37 0 1965 0 2183 0 2440 0 2611 38 0 1939 0 2154 0 2409 0 2582 39 0 1915 0 2127 0 2379 0 2555	28	0 2250	0 2499	0 2794	0 2997
31 0.2141 0.2379 0.2660 0.285; 32 0.2108 0.2342 0.2619 0.280; 33 0.2077 0.2308 0.2580 0.276; 34 0.2047 0.2274 0.2543 0.272; 35 0.2018 0.2242 0.2507 0.269; 36 0.1991 0.2212 0.2473 0.265; 37 0.1965 0.2183 0.2440 0.261; 38 0.1939 0.2154 0.2409 0.258; 39 0.1915 0.2127 0.2379 0.255;	29	0 2212	0 2457	0 2747	0 2947
32         0.2108         0.2342         0.2619         0.2801           33         0.2077         0.2308         0.2580         0.2761           34         0.2047         0.2274         0.2543         0.2721           35         0.2018         0.2242         0.2507         0.2691           36         0.1991         0.2212         0.2473         0.2651           37         0.1965         0.2183         0.2440         0.2611           38         0.1939         0.2154         0.2409         0.2581           39         0.1916         0.2127         0.2379         0.2552	30	0 2176	D 2417	0 2702	0 2899
33 0.2077 0.2308 0.2580 0.2761 34 0.2047 0.2274 0.2543 0.2721 35 0.2018 0.2242 0.2507 0.2691 36 0.1991 0.2212 0.2473 0.2651 37 0.1965 0.2183 0.2440 0.2611 38 0.1939 0.2154 0.2409 0.2581 39 0.1915 0.2127 0.2379 0.2551	31	0.2141	0 2379	0 2660	0 2853
34         0.2047         0.2274         0.2543         0.2721           35         0.2018         0.2242         0.2507         0.2690           36         0.1991         0.2212         0.2473         0.2650           37         0.1965         0.2183         0.2440         0.2650           38         0.1939         0.2154         0.2409         0.2580           39         0.1915         0.2127         0.2379         0.2550	32	0 2108	0 2342	0.2619	0.2809
35         0 2018         0 2242         0 2507         0 2690           36         0 1991         0 2212         0 2473         0 2650           37         0 1965         0 2183         0 2440         0 2610           38         0 1939         0 2154         0 2409         0 2580           39         0 1915         0 2127         0 2379         0 2550	33	0 2077	0 2308	0 2580	0 2766
36         0 1991         0 2212         0 2473         0 265           37         0 1965         0 2183         0 2440         0 261           38         0 1939         0 2154         0 2409         0 258           39         0 1915         0 2127         0 2379         0 255	34	0 2047	0 2274	0 2543	0 2728
37 01965 02183 02440 02613 38 01939 02154 02409 0258 39 01915 02127 02379 0255	35	0 2018	0 2242	0 2507	0 2690
38 0 1939 0 2154 0 2409 0 258 39 0 1915 0 2127 0 2379 0 255	36	0 1991	0 2212	0 2473	0 2653
39 0 1915 0 2127 0 2379 0 255	37	0 1965	0.2183	0 2440	0 2618
0.0.0	38	0 1939	0 2154	0 2409	0 2584
40 0 1891 0 2101 0 2349 0 252	39	0 1915	0.2127	0 2379	0 2552
	40	0 1891	0 2101	0 2349	0.2521

a	5%	2 5%	1%	2%
α,	10%	5%	2%	1%
n				
41	0 1869	0 2076	0.2321	0.2490
42	0.1847	0.2052	0.2294	0 2461
43	0 1826	0.2028	0 2268	0.2433
44	0 1805	0 2006	0 2243	0 2406
45	0 1786	0 1984	0 2218	0 2380
46	0 1767	0 1963	0.2194	0 2354
47	0 1748	0 1942	0.2171	0 23 30
48	0 1730	0 1922	0 2149	0.2306
49	0.1713	0 1903	0 2128	0 2283
50	0 1696	0 1884	0 2107	0.2260
55	0 1619	0 1798	0 2011	0.2157
60	0 1551	0 1723	0 1927	0 2067
65	0 1491	0 1657	0 1853	0 1988
70	0 1438	0 1597	0.1786	0 1917
75	0 1390	0.1544	0 1727	0 1853
80	0 1347	0 1498	0 1673	0 1796
85	0 1307	0 1452	0 1624	0 1742
90	0.1271	0.1412	0 1579	0 1694
95	0 1238	0.1375	0 1537	0 1649
100	0 1207	0 1340	0 1499	0 1608

Goodness-of-fit tests are designed to test a null hypothesis that some given data are a random sample from a specified probability distribution. The Kolmogorov-Smirnov tests are based on the maximum absolute difference  $D_n$  between the c.d.f. (cumulative distribution function)  $F_0(x)$  of the hypothesised distribution and the c.d.f. of the sample (sometimes called the empirical c.d.f.)  $F_n(x)$ . This sample c.d.f. is the step-function which starts at 0 and rises by 1/n at each observed value, where n is the sample size, i.e.  $F_n(x)$  is equal to the proportion of the sample values which are less than or equal to x.

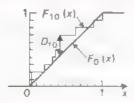
Critical regions for rejecting  $H_0$  are of the form  $D_n \ge tabulated$  value, and in most cases the general alternative hypothesis is appropriate, i.e. the  $\alpha_2$  significance levels should be used. One-sided alternative hypotheses can be dealt with by only considering differences in one direction between the c.d.f.s. For example, suppose  $H_1$  says that the actual values being sampled are mainly less than those expected from  $F_0(x)$  if this is the case  $F_n(x)$  will tend to rise earlier than  $F_0(x)$ , and so instead of  $D_n$  we should then use the statistic  $D_n^* = \max{\{F_n(x) - F_0(x)\}}$ . In the opposite case, where  $H_1$  says that the values sampled are mainly greater than those expected from  $F_0(x)$ , we should use  $D_n^* = \max{\{F_0(x) - F_n(x)\}}$ . Critical regions are  $D_n^*$  (or  $D_n^*$ )  $\ge tabulated$  value, and in these one-sided tests the  $\alpha_1$  significance levels should be used

For illustration, let us test the null hypothesis  $H_0$  that the following ten observations (derived in fact from part of the top row of the table of random digits on page 42) are a random sample from the uniform distribution over (0:1), having c.d.f.  $F_0(x) = 0$  for x < 0,  $F_0(x) = x$  for  $0 \le x \le 1$ , and  $F_0(x) = 1$  for x > 1:

0.02484 0.88139 0.31788 0.35873 0.63259 0.99886 0.20644 0.41853 0.41916 0.02944

Sorting the data into ascending order, we have

0.02484 0.02944 0.20644 0.31788 0.35873 0.41853 0.41915 0.63269 0.88139 0.39886



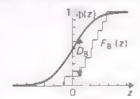
It is then easy to draw the sample c d.f.,  $F_{10}(x)$ , and from the diagram we find that the maximum vertical distance between the two c.d.f.s, which occurs at x = 0.41915, is  $D_{10} = 0.7 - 0.41915 = 0.28085$ . But the critical region for rejection of  $H_0$  even at the  $\alpha_2 = 16\%$  significance level is  $D_{10} \ge 0.3687$ , and so we have no reason here to doubt the null hypothesis.

The Kolmogorov-Smirnov test may be used both when  $F_0(x)$  is

continuous and discrete. In the continuous case critical values are exact; in the discrete case they may be conservative (i.e. true  $\alpha < n_{\rm cominal}(\alpha)$ ).

A particularly useful application of the test is to test data for normality. In this case use may be made of the graph on page 27 of the c.d.f of the standard normal distribution by first standardising the data, i.e. subtracting the mean and dividing by the standard deviation. The resulting sample c.d.f. may be drawn on page 27 and the Kolmogorov-Smirnov test performed as usual. For example to test the hypothesis that the following data come from the normal distribution with mean 5 and standard deviation 2, we transform each observation X into  $Z = \frac{1}{2}(X - 5)$ .





Then we sort the transformed data into ascending order and draw the sample c.d.f. on the graph on page 27 (step-heights are 1/8 since the sample size n is 8 here). The maximum vertical distance between the two c.d f.s is seen to be about 0.556, and this shows strong evidence that the data do not come from the hypothesised distribution, since the  $\alpha_2 = 1\%$  critical region is  $D_6 \ge 0.5418$ .

Perhaps it is more commonly necessary to test for normality without the mean and standard deviation being specified. To perform the test in these circumstances, first estimate the mean by  $\bar{X} = \sum X/n$  and the standard deviation by  $s = \{\sum (X - \bar{X})^2/(n-1)\}^{1/2}$ . Standardise the data using these estimates, and then proceed as before except that the critical values on page 27 should be used. For the above eight observations  $\bar{\lambda} = 6.940$  and s = 1.484. The transformed data are now

1213 -1927 0923 0.579 0371 0182 0074 06	1 213	-1927	0 923	0.579	0.371	0 182	0 074	0 674
---	-------	-------	-------	-------	-------	-------	-------	-------

he maximum difference now found between the c d f. of this sample and that of the standard normal distribution is  $D_8 = 0.155$ , and this is certainly not significantly large, for even at the  $\alpha_2 = 10\%$  level the critical region is  $D_8 \ge 0.2652$ . We conclude therefore that although there was strong evidence that the data do not come from the originally specified normal distribution, they could quite easily have come from some other normal distribution. The originator of this type of test was W. H. Lilliefors.

Critical values for larger sample sizes than covered in the tables are discussed on page 35.

## Critical values for the Kolmogorov-Smirnov test for normality

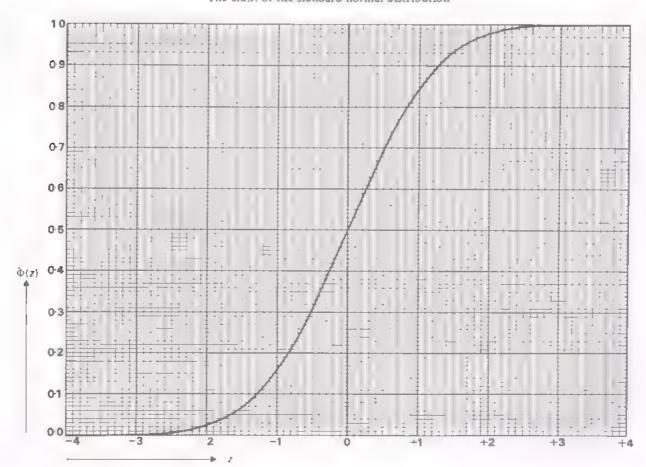
$\alpha_1$	5%	2. a.	1%	205
a <sub>2</sub>	10%	5%	2º%	1%
0				
1				
2	-			
3	0 3666	0 3758	0.3812	0.3830
4	0.3453	0.3753	0.4007	0.4131
5	0 3189	0 3431	0.3755	0 3970
6	0 2972	0 3234	0 3523	0.3708
7	0 2802	0 3043	0.3321	0 3509
8	0 2652	0 2880	0 3150	0.3332
9	0 2523	0.2741	0 2999	0.3174
10	0 2411	0.2619	0 2869	0 3037
17	0 2312	0.2514	0 2754	0 2916
12	0 2225	0 2420	0 2651	0.2810
13	0.2148	0.2336	0 2559	0.2714
14	0.2077	0.2261	0 2476	0.2627
15	0 2013	0.2192	0.2401	0 2549
16	0 1954	0.2129	0 2332	0 2476
17	0 1901	0.2071	0 2270	0 2410
18	0.1852	0.2017	0 2212	0 2349
19	0 1807	0 1968	0.2158	0 2292
20	0 1765	0 1921	0.2107	0 2238

σι	5%	2350	1%	1.8
α2	10%	5%	2%	1%
n				
21	0 1725	0 1878	0 2060	0.2188
22	0 1688	0 1838	0.2015	0 2141
23	0 1653	0.1800	0.1974	0.2097
. 24	0 1620	0.1764	0 1936	0 2056
25	0 1589	0.1730	0.1899	0.2018
26	0 1560	0 1699	0 1865	0 1981
27	0 1533	0.1670	0.1833	0.1947
28	0 1507	0 1642	0.1802	0 1915
29	0 1483	0.1615	0 1773	0 1884
30	0 1460	0 1589	0 1746	0 1855
31	0 1437	0.1565	0 1719	0 1827
32	0.14)6	0.1542	0 1693	0.1800
33	0 1395	0 1519	0 1669	0.1774
34	0 1375	0.1498	0 1645	0.1749
35	0 ⊺356	0 1478	0 1622	0.1725
36	0 1338	0 1458	0 1601	0.1702
37	0 1321	0 1439	0 1580	0 1680
38	0 1304	0 1421	0 1560	0 1659
39	0 1288	0 1403	0.1540	0 1638
40	0 1272	0.1386	0 1522	0 1518

0:1	5%	2 %	1%	1, 9%
- a <sub>2</sub>	10 -	5%	2 hb	1%
л				
41	0 1257	0.1370	0 1504	0 1599
42	0 1 2 4 3	0.1354	0.1487	0.1581
43	0 1229	0 1339	0 1470	0 1563
44	0 1216	0 1325	0 1454	0 1546
45	0 1203	0.1311	0 1438	0.1530
46	0.1190	0 1297	0 1423	0 1514
47	0 1178	0 1284	0 1409	0 149B
48	0 1166	0.1271	0.1394	0.1483
49	0.1155	0 1258	0.1380	0 1468
50	0 1144	0 1246	0.1367	0 1454
55	0 1092	0 1190	0 1306	0 1389
60	0 1048	0.1142	0.1253	0.1332
65	0 1008	0.1098	0 1205	0.1281
70	0.0972	0 1060	0.1163	0 1236
75	0 0940	0 1025	0.1125	0.1195
80	0 0911	0.0993	0 1090	0.1158
85	0 0885	0.0964	0 1059	0 1125
90	0.0861	0.0938	0.1030	0 1094
95	0 0838	0.0913	0.1003	0 1065
100	0.0817	0 0890	0 097B	0 1039

For description see page 26; for larger sample sizes, see page 35.

The c.d.f. of the standard normal distribution



#### Nonparametric tests

Pages 29-34 give critical values for six nonparametric tests. The sign test and the Wilcoxon signed-rank test are one-sample tests and can also be applied to matched-pairs data, the Mann Whitney and Kolmogorov Smirnov tests are two-sample tests, and the Kruskal Wallis and Friedman tests are nonparametric alternatives to the standard one-way and two-way analyses-of-variance. Critical values for larger sample sizes than those included in these tables are covered on page 35.

The sign test (page 29) Suppose that the national average mark in an English examination is 60%. (In nonparametric work, the average is usually taken to be the median rather than the mean.) Test whether the following marks, obtained by twelve students from a particular school, are consistent with this average

												_
70	65	75	58	56	60	80	75	71	69	58	75	
+	+	+	_	_	0	+	+	+	+	_	+	

We have printed + or - under each mark to indicate whether it is greater or less than the hypothesised 60. There is one mark of exactly 60 which is completely ignored for the purposes of the test, reducing the sample size n to 11. The sign test statistic S is the number of + signs or the number of - signs, whichever is smaller, here S=3. Critical regions are of the form  $S \le tabulated\ value$ . As the  $\alpha_2=10\%$  critical region for n=11 is  $S \le 2$ , we cannot reject the null hypothesis  $H_0$  that these marks are consistent with an average of 60%

For a one-sided test, count either the number of + or - signs, whichever the alternative hypothesis  $H_1$  suggests should be the smaller. For example if  $H_1$  says that the average mark is less than 60%, S would be defined as the number of + signs since if  $H_1$  is true there will generally be fewer marks exceeding 60%. Critical regions are of the same form as previously, but the  $\alpha_1$  significance levels should be used

The Wilcoxon signed-rank test (page 29) This test is more powerful than the sign test as it takes into account the sizes of the differences from the hypothesised average, rather than just their signs. In the above example, first subtract 60 from each mark, and then rank the resulting differences, irrespective of their signs. Again ignore the mark of exactly 60, and also average the ranks of tied observations.

differences	+ 10	+ 5	+ 15	-2	-4	(0)	+ 20	+ 15	+11	+9	- 2	+ 15
tankı	6	4	9	1}	3		11	9	7	.5	11	9

The Wilcoxon statistic T is the sum of the ranks of either the + ve or —ve differences, whichever is smaller. Here  $T=1\frac{1}{2}+3+1\frac{1}{2}=6$ . Critical regions are of the form  $T \le tabulated$  value, and the test thus shows evidence at better than the  $\alpha_2 = 2\%$  significance level that these marks are inconsistent with the national average, since the 2% critical region for n=11 is  $T \le 7$ .

For a one-sided test, let T be the sum of the ranks of either the  $\pm$ ve or the  $\pm$ ve differences, whichever the one-sided  $H_1$  suggests should be the smaller  $\pm$ 1 will be the same choice as in the sign test  $\pm$ 2 and use the  $\alpha_1$  significance levels.

Matched-pairs data. Matched-pairs data arise in such examples as the following. One member of each of eight pairs of identical twins is taught mathematics by programmed learning, the other by a standard teaching method. Do the test results imply any difference in the effectiveness of the two teaching methods?

twins	a	ь	c	d	e	. 1	9	h
programmed learning	70	80	62	50	70	30	49	60
standard method	75	82	65	58	68	41	55	67
differences	+5	+2	+3	+8	-2	$\pm 11$	+6	+7

Such data may be analysed by either of the above tests, comparing the twin-by-twin differences in the final row with a hypothesised average of 0. The reader may confirm that S=1 and  $T=1\frac{1}{2}$ , so that the null hypothesis of no difference is rejected at the  $\alpha_2=10\%$  level in the sign test and at near to the  $\alpha_2=2\%$  level in Wilcoxon's test.

The Mann-Whitney U test (page 30). Six students from another school take the same English examination as mentioned above. Their marks are, 53, 65, 63, 67, 68 and 56. We want to check whether the two sets of students are of different average standards.

We order the two samples of marks together and indicate by A or B whether a mark comes from the first or second school

		53 B	56 A	56 8	57 8	58 A	58 .4	60 A	63 B	65 A	65 <i>B</i>	68 £	69 A	70 .4	71 .A	76 A	75 A	75 A	A
I	yanda	1	24	21	4	5	В	7	8	95	91	11	12	13	14	15	16	17	18

The observations are given ranks as shown, the ranks being averaged in the case of ties (unnecessary if a tie only involves members of one sample). Then either form the sum  $R_A$  of the ranks of observations from sample A, and calculate  $U_A = R_A - \frac{1}{2}n_A(n_A+1)$ , or the sum  $R_B$  of the ranks of observations from sample B, and calculate  $U_B = R_B - \frac{1}{2}n_B(n_B+1)$ , where  $n_A$  and  $n_B$  are the sizes of samples A and B. Finally obtain U as the smaller of  $U_A$  or  $n_A n_B - U_A$ , or equivalently the smaller of  $U_B$  or  $n_A n_B - U_B$ . Critical regions have the form  $U \le tabulated value$ . In the above example,  $R_A = 135$  so that  $U_A = 135 - \frac{1}{2}(12)(13) = 57$ , or  $R_B = 36$  and  $U_B = 36 - \frac{1}{2}(6)(7) = 15$ . In either case U is found to be 15, and this provides a little evidence for a difference between the two sets of students since the  $\alpha_2 = 10\%$  critical region is  $U \le 17$  and the 5% region is  $U \le 14$ . (In the table, sample sizes are denoted by  $n_1$  and  $n_2$  with  $n_1 \le n_2$ .)

For a one-sided test, calculate whichever of  $U_A$  and  $U_B$  is more likely to be small if the one-sided  $H_1$  is true, use this in place of  $U_c$  and refer to the  $\alpha_1$  significance levels

The Kolmogorov-Smirnov two-sample test (page 31), Whereas the Mann-Whitney test is designed specifically to detect differences in average, the Kolmogorov-Smirnov test is used when other types of difference may also be of interest. To calculate the test statistic D, draw the sample c.d.f.s (see page 26) for both sample A and sample Bon the same graph, D is then the maximum vertical distance between these two c.d.f.s. To use the table on page 31, form  $D^{\bullet} = n_A n_B D$ , and critical regions are of the form D° > tabulated value, using the a2 significance levels. A one-sided version of the test is also available, but is not often used since the alternative hypothesis is then essentially concerned not with general differences but a difference in average, for which the Mann-Whitney test is more powerful. Applied to the above example on the two sets of English results, D = 7/12 and  $D^* = 12 \times 10^{-6}$  $6 \times 7/12 = 42$ . This is not even significant at the  $\alpha_2 = 10\%$  level, as that critical region is  $D^* \ge 48$ . This supports the above remark that the Mann-Whitney test (which gave significance at better than the 10% level) is more powerful as a test for differences in average

The Kruskal-Wallis test (pages 32-34) The Kruskal-Wallis test is also designed to detect differences in average, but now when we have three or more samples to compare. Again, as in the Mann-Whitney test, we rank all of the data together (averaging the ranks of tied observations) and form the sum of the ranks in each sample. The test statistic is

$$H = \frac{12}{N(N+1)} \sum_{i=1}^{k} \frac{R^2}{n_i} - 3(N+1)$$

where k is the number of samples,  $n_1, n_2, \ldots, n_k$  are their sizes,  $N = \sum n_i$  and  $R_1, R_2, \ldots, R_k$  are the rank sums. Critical regions are of the form  $H \ge tabulated$  value. Tables are given on page 32 for k = 3 and  $N \le 19$ , on page 33 for k = 4 ( $N \le 14$ ), k = 5 ( $N \le 13$ ) and k = 6 ( $N \le 13$ ), and on page 34 for  $3 \le k \le 6$  and equal sample sizes  $n_1 = n_2 = \ldots = n_k = n$  for  $2 \le n \le 25$ 

To illustrate the Kruskal-Wallis test, we show samples of mileages per gallon for three different engine designs

derign		mileage	per geller			770	nica		canic aumo
	19.8	20.5	20.8	19.7	-4	6	7	21/2	20
b	21.7	20.8	21.2		10	71	9		264
c	19.7	19.4	10.9		21	1	8		89

Then
$$H = \frac{12}{10 \times 11} \left( \frac{20^2}{4} + \frac{(26\frac{1}{2})^2}{3} + \frac{(8\frac{1}{2})^2}{3} \right) - 3 \times 11$$

$$= 0.1091 \times (358.167) - 33 = 6.073.$$

This is significant of a difference between average mileages at better than the 5% level, the  $\alpha = 5\%$  critical region being  $H \geqslant 5.791$  (In such cases where there is no meaningful one-sided version of the test,  $\alpha_2$  is written as  $\alpha$  with no subscript )

Friedman's test (page 34) Friedman's test applies when the observations in three or more samples are related or 'blocked' (similarly as with matched-pairs data). If there are k samples and n blocks, the observations in each block are ranked from 1 to k, the rank sums  $R_1, R_2, \ldots, R_k$  for each sample obtained, and Friedman's test statistic is then

$$M = \frac{12}{nk(k+1)} \sum_{i=1}^{k} B^{2} \quad 3n(k+1)$$

To illustrate the test, suppose that in a mileages survey we use cars of five different ages and obtain the following data:

			age of a								
design	1	2	3	4	5			ranks			rank sume
	21.3	21,6	21.2	20.7	20.1	2	2	2)	2	2	10
ь	216	21.7	21.2	20.8	20.6	3	3	21	3	3	144
6	20 0	20.1	19.9	19.5	19,0	1	T	1	-1	-1	5

Then  $M = 12 (15 \times 4) \{(10\frac{1}{2})^2 + (14\frac{1}{2})^2 + 5^2 + (15 \times 4) + 0.2 \times 345.5 + 60 = 9.1$ , which is strongly significant since the  $\alpha = 1\%$  critical region is  $M \ge 8.400$ 

Note: All of the nonparametric tests described above have discrete-valued statistics, so that the exact nominal  $\alpha$ -levels are not usually obtainable. The tables give best conservative critical regions, i.e. the largest regions with significance levels less than or equal to  $\alpha$ 

### Critical values for the sign test

a,	5%	2 5%	1%	14.0½	$\alpha_1$	5%	21 9	1%	44	$\alpha_1$	5%	2 %	1%	c <sub>/č</sub>	01	5%	2 0	1%	,0;
α,	10%	5%	2%	1%	a	10%	5%	2%	1%	Δ2	10%	5%	2%	1%	a <sub>2</sub>	10-	5%	29,	1%
n					/5					n					2				
3	-	-		-	26	8	7	6	6	51	19	18	16	15	76	30	28	27	26
2			-		27	В	7	7	6	52	19	16	1.7	16	77	30	29	27	26
3	-				28	9	8	7	6	53	20	16	1.7	16	78	3↑	29	28	27
4		-		-	29	9	В	7	7	54	20	19	18	1.7	79	31	30	28	27
5	0				30	10	9	8	7	55	20	19	18	17	80	32	30	29	28
6	0	0	-		31	10	9	8	7	56	21	20	18	17	81	32	31	29	28
7	0	0	0		32	10	9	8	8	57	21	20	19	18	82	33	31	30	28
8	1	0	0	0	3.3	1.1	10	9	8	58	22	21	19	18	83	33	32	30	29
9	1	1	0	0	34	12	10	9	9	59	22	21	20	19	84	33	32	30	29
10	1	1	Ö	0	35	12	1 1	10	9	50	23	21	20	19	85	34	32	31	30
11	2	1	1	0	36	12	11	10	9	61	23	22	20	20	86	34	33	31	30
12	2	2	1	1	37	13	12	10	10	62	24	22	21	20	87	35	33	32	31
13	3	2	1	1	38	13	12	11	10	63	24	23	21	20	88	35	34	32	31
14	3	2	2	1	39	13	12	11	11	64	24	23	22	21	89	36	34	33	31
15	3	3	2	2	40	14	13	12	11	65	25	24	22	21	90	36	35	3.3	32
16	4	3	2	2	41	14	13	12	11	66	25	24	23	22	91	37	35	33	32
17	4	4	3	2	42	15	14	13	12	6.7	26	25	23	22	92	37	36	34	33
18	5	4	3	3	43	15	14	13	12	68	26	25	23	22	9.3	38	36	34	33
19	5	4	4	3	44	16	15	13	13	69	27	25	24	23	94	38	37	35	34
20	5	5	4	3	45	16	15	14	13	70	27	26	24	23	95	38	37	35	34
2t	6	5	4	4	46	16	15	14	13	71	28	26	25	24	96	39	37	36	34
22	6	5	5	4	47	17	16	15	14	72	28	27	25	24	97	39	38	36	35
23	7	6	5	4	48	17	18	15	14	73	28	27	26	25	98	40	38	37	35
24	7	6	5	5	49	18	17	15	15	74	29	28	26	25	99	40	39	37	35
25	7	7	6	5	50	18	17	16	15	75	29	28	26	25	100	41	39	37	36

For description, see page 28; for larger sample sizes, see page 35.

## Critical values for the Wilcoxon signed-rank test

a <sub>1</sub>	6%	2 5	1%	-5%	a <sub>1</sub>	5%	2,1	1%	٩	or <sub>1</sub>	5%	2 %	1%	TO <sub>Str.</sub>	æ,	5%	21 %	1%	1 %
or <sub>a</sub>	109	5%	2%	1%	dr <sub>3</sub>	10%	5%	2	1%	a:1	10%	5%	29.	1%	o <sub>z</sub>	10%	5%	2%	1%
n					n					12					17				
1	-			-	26	110	98	84	75	51	486	453	416	390	76	1144	1084	1015	968
2			-		27	119	107	92	83	52	507	473	434	408	77	1176	1115	1044	997
3		-		-	28	130	116	101	91	5.3	529	494	454	427	78	1209	1147	1075	1026
4			-		29	140	126	110	100	54	550	514	473	445	79	1242	1179	1105	1056
5	0	-			30	151	137	120	109	65	573	536	493	465	80	1276	1211	1136	1086
6	2	0		- ]	31	163	147	130	118	56	595	557	514	484	81	1310	1244	1168	1116
7	3	2	0		32	175	159	140	128	67	618	579	535	504	82	1345	1277	1200	1147
8	5	3	1	0	33	187	1.70	151	13B	58	642	602	556	525	63	1380	1311	1232	1178
9	8	5	3	1	34	200	182	162	148	59	666	625	578	546	84	1415	1345	1265	1210
10	10	8	5	3	35	213	195	173	159	60	690	648	600	567	85	1451	1380	1298	1242
11	13	10	7	5	36	227	208	185	171	61	715	672	623	589	86	1487	1415	1332	1275
12	1.7	1.3	9	7	37	241	221	198	182	62	741	697	646	611	87	1524	1451	1366	130B
13	21	1.7	12	9	38	256	235	211	194	63	767	721	669	634	88	1561	1487	1400	1342
14	25	21	15	12	39	271	249	224	207	64	793	74.7	693	857	89	1599	1523	1435	1376
15	30	25	19	15	40	286	264	238	220	65	820	772	718	681	90	1638	1560	1471	1410
16	35	29	23	19	41	302	279	252	233	66	847	798	742	705	91	1676	1597	1507	1445
17	41	34	27	23	42	319	294	266	247	67	875	825	768	729	92	1715	1635	1543	1480
18	47	40	32	27	43	336	310	281	261	68	903	852	793	754	93	1755	1674	1580	1516
19	53	46	37	32	44	353	327	296	276	69	931	879	819	779	94	1795	1772	1617	1552
20	60	52	43	37	45	371	343	312	291	70	960	907	846	B05	95	1836	1752	1655	1589
21	67	58	49	42	46	389	361	328	307	71	990	936	873	831	96	1877	1791	1693	1626
22	75	65	55	48	47	407	378	345	322	72	1020	964	901	858	97	1918	1832	1731	1664
23	83	73	62	54	48	426	396	362	339	73	1050	994	928	BB4	98	1960	1872	1770	1702
24	91	81	69	61	49	446	415	379	355	74	1081	1023	957	912	99	2003	1913	1810	1740
25	100	89	76	68	50	466	434	397	373	75	1112	1053	986	940	100	2045	1955	1850	1779

For description, see page 28; for larger sample sizes, see page 35.

## Critical values for the Mann-Whitney U test

01 02	5% 2 ° 1% ° ° ° ° ° ° ° ° ° ° ° ° ° ° ° ° °	α <sub>1</sub> α <sub>2</sub>	5% 2 4 1% -% 10 5% 2 1%	a <sub>1</sub>		1% _% 2 1%		α <sub>1</sub>	10	2 º		.ºŧ		α <sub>1</sub> α <sub>2</sub>	<b>5%</b>	21/2°.	1% 2%	5% 1%
$n_1$ $n_2$		n, n2		Fi n2		-	17:	n <sub>3</sub>				$\neg$	n	n2				
2 2		8 5	4 2 1 0	8 16	36 31	26 22	12	21	B1	73	64	58	18	23	143	132	118	109
2 3		5 6	5 3 2 1	8 17	39 34	28 24	12	22	85	77	67	61	18	24	150	138	124	115
2 4		5 7	6 5 3 1	8 18		30 26	12	23	90	81	71	64	18	25	157	145	130	121
2 5	0 -	5 8	8 6 4 2	8 19	44 38 47 41	32 28 34 30	12	24	94 98	85 89	75 78	68 71	19	19	123	113	101	93
2 6	0 -	5 9	9 7 5 3	8 20		36 32	14		30	10.5	,,,		19	20	130		107	99:
2 8	1 0 -	5 11	12 9 7 5	8 22		38 34	13	13	51	45	39	34	19	21	138	126	113	106
2 9	1 0 -	5 12	13 11 8 6	B 23		40 35	13	14	56	50	43	38	19	22	145	133	120	111
2 10	1 0	5 13	15 12 9 7 16 13 10 7	8 24 8 25	57 50 60 53	42 37 45 39	13	16	61 65	54 59	47 51	42	19	23	152 160	140	126 133	117
2 11 2 12	2 1	5 15	18 14 11 8	- 20	00 A	4, 50	13	17	70	63	55	49	19	25	167		139	129
2 13	2 1 0	5 16	19 15 12 9	9 9	21 17	14 11	13	18	75	67	59	53	-					-
2 14	3 1 0 -	5 17	20 17 13 10	9 10	24 20	16 13	13	19	80	72 76	63 67	571	20	20	138	127	114	105
2 16	3 1 0 -	5 18	22 18 14 11 23 19 15 12	9 11	27 23 30 26	18 16	13	20	84 89	80	71	64	20	22	154	141	127	118
2 17	3 2 0	5 20	25 20 16 13	9 13	33 28	23 20	13	22	94	85	75	68	20	23	161	149	134	125
2 18	4 2 0 -	5 21	26 22 17 14	9 14	36 31	26 22	13	23	98	89	79	72	20	24	169	156	141	131
2 19	4 2 1 0	5 22	28 23 18 14	9 15	39 34	28 24	13	24	103 108	94	83 87	75 79	20	25	177	163	148	138
2 20	4 2 1 0 5 3 1 0	5 23	29 24 19 15 30 25 20 16	9 16 9 17	42 37 45 39	31 27 33 29	13	20	108	30	07	, 3	21	21	154	142	128	118
2 22	5 3 1 0	5 25	32 27 21 17	9 18	48 42	36 31	14	14	61	55	47	42	21	22	162	150	135	125
2 23	5 3 1 0	-		9 19	51 45	38 33	14	15	66	59	51	46	21	23	170	167	142	132
2 24	6 3 1 0	6 6	7 5 3 2 8 6 4 3	9 20	54 48 57 50	40 36 43 38	14	16	71	64 69	56 60	50	21	24	179 187	165	150	139
2 25	6 3 1 0	6 8	8 6 4 3	9 22	60 53	45 40	14	18	82	74	65	58					1 47	
3 3	0	6 9	12 10 7 5	9 23	63 56	48 43	14	19	87	78	69	63	22	22	171	158	143	133
3 4	0	6 10	14 11 8 6	9 24	66 59	50 45	14	20	92	83	73	67	22	23	179	166	150	140
3 5	1 0	6 11	16 13 9 7 17 14 11 9	9 26	69 62	53 47	14	21	97	93	78 62	71	22	24	188	174	158 166	147 155
3 6	2 1 2 1	6 12	19 16 12 10	10 10	27 23	19 16	14	23	107	98	87	79						
3 8	3 2 0 -	6 14	21 17 13 11	10 11	31 26	22 18	14	24	113	102	91	83	23	23	189	175	158	148
3 9	4 2 1 0	6 15	23 19 15 12	10 12	34 29	24 21	14	25	118	107	95	87	23	24 25	198	183	167	166
3 10	4 3 1 0	6 16	25 21 16 13 26 22 18 15	10 13	37 33 41 36	27 24 30 26	15	15	72	64	56	51	23	23	207	. 62	170	100
3 12	5 4 2 1	6 18	28 24 19 16	10 15	44 39	33 29	15	16	7.7	70	61	55	24	24	207	192	175	164
3 13	6 4 2 1	6 19	30 25 20 17	10 16	48 42	36 31	15	17	83	75	66	60	24	25	217	201	184	172
3 14	7 5 2 1	6 20	32 27 22 18	10 17	51 45	38 34 41 37	15	18	98 94	80 85	70 75	69	25	25	227	211	182	180
3 15	7 5 3 2 B 6 3 2	6 21	34 29 23 19 36 30 24 21	10 18	55 48 58 52	44 39	15	20	100	90	80	73	2.0		**/		184	1437
3 17	9 6 4 2	6 23	37 32 26 22	10 20	62 55	47 42	15	21	105	96	85	78						
3 18	9 7 4 2	6 24	39 33 27 23	10 21	65 58	50 44	16	22	111	101	90	82	26	26	247	230	211	198
3 19		6 25	41 35 29 24	10 22	68 61 72 64	53 47	15	23	178	10 <del>6</del>	94	97 91	27	27 28	268	250 272	230	216
3 20	11 8 5 3	7 7	11 8 6 4	10 28	75 67	58 52	15			117		96	29	29	314	294	271	255
3 22		7 8	13 10 7 6	10 25	79 71	61 56	_		-			-	30	30	338	317	293	276
3 23	13 9 6 4	7 9	15 12 9 7	11 14	24 20	25 24	16	16	83 89	75 81	56 71	60						
3 24	13 10 6 4	7 10	17 14 11 9 19 18 12 10	11 11	34 30 38 33	25 21 28 24	16	18	95	86	76	70	31	31	363	341	316	298
- 23	, ,	7 12	21 18 14 12	11 13	42 37	31 27	16	19	101	92	82	74	32	32	388	365	339	321
4 4		7 13	24 20 16 13	- 51 - 16	46 40	34 30	16	20	107	98	87	79	33	33	415 443	391 418	363 368	344
4 5		7 14	26 22 17 15 28 24 19 16	11 16	50 44 54 47	37 33 41 36	18	21	113	103	92	84	34	34	471	445	414	384
4 6		7 16	30 26 21 18	11 17	57 51	44 39	16	23	125	115	102	94						
4 8	5 4 2 1	7 17	33 28 23 19	11 18	61 55	47 42	18	24	131		108	99	36	38	501	473	441	420
4 9		7 18		11 19	65 58	50 45	16	25	137	126	113	104	37	37 38	531 563	503 533	469 498	447
4 10	7 5 3 2	7 19		11 20	69 62 73 65	53 48 57 51	17	17	96	67	77	70	39	39	595	564	528	504
4 12		7 21		11 22	77 69	60 54	17	18	102	93	82	75	40	40	628	596	658	633
4 13	10 8 5 3	7 22		11 23	81 73	63 57	17	19	109	99	88	81			-			
4 14	11 9 6 4	7 23		11 26	85 76	66 60 70 63	17	20	115	105	93	91	41	41	662	628	590	564
4 15		7 26	1				17	22	128	117	105	96	42	42	697	662	622	595
4 17	15 11 8 6		-	12 12		31 27	17	23	134			102	43	43	733	697	655	627
4 18		8 8	1	12 13	47 41	35 31 38 34	17		141		116	107	44	45	770 808	732 769	689 724	660
4 19		8 9		12 16		38 34 42 37	17	40	147	. 25	122	,,,	40	40	0.00	. 03	7.7	
4 21	19 15 11 B	8 11		12 16	1	46 41	18	18	109	99	88	81	46	46	846	806	760	729
4 22		8 12		12 17	3	49 44	18		116	106	94	87	47	47	886	845	797	765
4 23		8 14		12 18	9	53 47 56 51	18		123	112	100	92 98	48	4B 49	926 968	884 924	835 873	802 839
4 24		8 15		12 20	2	60 54	18			125		104	50	50		965		
4 23	23 10 13 10	4 10	20 27 20												_			

## Critical values for the Kolmogorov - Smirnov two-sample test

$\alpha_t$	5%	Z 24	1%	96		۵,	5%	2 n.	1%	ok.	α	5%	2 20	1%	a <sub>F</sub>		α1	5%	2 %	1%	95		Ot 1	5%	2 %	1%	, P'a
0.5	10%	5%	2%	1%		σ1	-0%	5%	25	1%	0.	10%	5%	2%	1%		02	10%	5%	24	1%		α2	10%	5%	23,	1%
n1 n2					$n_{\rm L}$						n, n2	-				m <sub>1</sub>						113					
2 2 2 3	-				5	6	20	25 24	25 30	30	B 16	72 68	80 77	88 85	88 88	12		108	120	132 138	141	-	8 23	162	170	189	204
2 4	1				5	7	25	28	30	35	8 18	72	80	88	94		23	113	125	138	149	-	B 25	162	180	202	216
2 5	10			-	6	8	27	30	35	35	8 19	74	82	93	98	12		132	144	156	168	Н					
2 6	12	**			5	10	30	35 40	36 40	40	8 20	80	88	102	104	12	25	120	138	153	165	-	9 19	152	160	190	190
2 8	16	16	_		5	11	36	39	44	45	8 22	84	94	106	112	13	13	91	91	104	117	-	9 21	147	163	184	199
2 9	18	18			5	12	36	43	48	50	8 23	89	98	107	115	13	14	78	89	102	104	1	9 22	152	169	190	204
2 10	18	20		1	5	13	40	45 46	50	52 56	8 24 8 26	96 95	104	120	128	13		87 91	96	107	115	-	9 23	159	177	197 204	209
2 12	22	24			6	15	50	55	60	60	B 23	85	104	0	123	13		96	105	118	127	-	9 25	168	187	211	224
2 13	24	26	26	-	6	16	48	54	59	64	9 9	54	54	63	63	13		99	110	123	131	H					
2 14 2 15	24 26	26 28	28 30		5	17	50	55 60	63 65	68 70	9 10	50 52	53 59	61	63 70	13		104	114	130	138	- 1111	0 20	160	180	193	199
2 16	28	30	32		5	19	56	61	70	71	9 12	57	63	69	75	13		113	126	140	150	1110	0 22	160	176	196	212
2 17	30	32	34		5	20	60	65	75	80	9 13	59	65	73	78	13		117	136	143	156		0 23	164	184	205	219
2 18	32	34 36	36	38	5	21	60	69 70	75 78	80	9 14	63 69	70 75	B0 B4	90	13	23	120	135	152	166		0 24	172	192	212	228
2 20	34	38	40	40	5	23	85	72	02	87	9 16	69	78	87	94		25	131	145	160	172	-	- 20	-00	200	820	200
2 21	36	38	42	42		24	67	76	85	90	9 17	74	82	92	99							-	1 21	168	189	210	231
2 22 23	36	40	44	44	5	25	75	80	90	95	9 18 9 19	81	90	99	108	14	14	98	112	112	126	-	1 22	163	183	205	223
2 24	40	44	46	48	6	6	30	30	36	36	9 20	84	93	104	111	14		96	106	120	126	- 1	1 24	177	198	222	237
2 25	42	46	48	50	6	7	28	30	35	36	9 21	90	99	111	117	14	17	100	111	125	134	2	1 25	182	202	225	244
3 3	9				6	B 9	30	34	40	40	9 22	91 94	101	113	122	14		104	116	130	140	2	2 22	198	198	242	242
3 4	12			-	6	10	36	40	44	4B	9 24	99	111	123	132		20	114	126	142	152	110	2 23	173	194	217	237
3 5	15	15			6	11	38	43	49	54	9 25	101	114	125	135	100	21	126	140	154	161		2 24	182	204	228	242
3 6	15 18	18	21	-	6	12	48 46	48 52	54 54	60 60	10 10	60	70	70	80	-	22	124	138	152 159	164	- 2.	2 25	189	209	234	250
3 8	21	21	24	-		14	48	54	60	64	10 11	57	60	69	77		24	132	146	164	176	2	3 23	207	230	253	253
3 9	21	24	27	27		15	51	57	63	69	10 12	60	66	74	80	14	25	136	150	169	182	-	3 24	183	205	228	249
3 11	24	27 30	30	30	1100	16	54 56	60 62	66 68	72	10 13	68	70	7B 84	90	15	15	105	120	135	135	2.	3 25	195	216	243	262
3 12	27	30	33	36	6	18	56	72	78	84	10 15	75	80	90	100		16		114	120	133	24	1 24	216	240	264	288
3 13 3 14	30	33	36	39 42	-	19	64	70	77	83	10 16	76	84	94	100		17		116	131	142	24	1 25	204	225	254	262
3 15	33	36 36	39 42	42		21	66 69	72 75	80	90	10 17	79 82	93	99 104	106 108		18	111	123	138	147	25	25	225	250	275	300
3 16	36	39	45	45		22	70	78	88	92	10 19	85	94	104	113	15	20	125	135	150	160						
3 17	36 39	42	45	48 51		23	73 78	90	91 96	97	10 20	100	110	120	130		21	126	138	156	168	20	3 26	234	260	286	312
3 19	42	45	51	54	1100	25	78	88	96	107	10 22	30	108	120	130		23		149	165	179	-	7 27	243	270	324	324
3 20	42	48	54	57							10 23	101	114	127	137		24	141	156	174	186	-	3 28	580	308	3 36	364
3 21 3 22	45 48	51 51	54	57 60	7	7	35 34	42	42	42	10 24	106	118	130	140	15	25	145	160	180	195	-	30	290 300	319	348 360	377
3 23	48	54	60	63	7	9	36	42	47	49		1	- 4 -	- 10		16	16	112	128	144	160			500	200	300	,,,,,
3 24	51	57 en	63	66		10	40	46	50	53	11 11	66	77	88	88	16	_		124	139	143			D 4 D		0.7.2	,,,,
3 25	54	60	66	69		11	44	48 53	55 58	59 60	11 12	64	72 75	77 86	86 91		18		128	142	154	-	31	310	341	416	403
4 4	16	16			7	13	50	56	63	65	11 14	73	82	90	96	16	20		140	156	168		33	330	396	429	462
4 5	16 18	20	20 24	24		14	56 56	63	70	77   75	11 15	76	84	95	102		21		145	162	173		34	374	408	442	476
4 7	21	24	28	28		16	59	62 64	70 73	77	11 17	80	93	104	106		22		150	168	180	3	35	385	420	455	490
4 8	24	28	32	32	7	17	61	68	77	84	11 18	88	97	108	118	16	24	152	168	184	200	-	36	396	432	468	504
4 9 4 to	27	30	32 36	36 36	7	18	65 69	72 76	83	91	11 19	92	102	114	122	16	26	149	167	186	199	-	37	407	444	518	518
4 11	29	33	40	40		20	72	79	86 91	93	11 21	96 †01	112	124	134	17	17	136	136	153	170		38	418	456 468	532 546	570
4 12	36	36	40	44	7	21	7.7	91	98	105	11 22	110	121	143	143	17	18	118	133	150	164		40	440	520	560	600
4 13	35 38	39 42	44	48 48		22 23	77 80	84	97	103	11 23	108	119	132	142		19		147	158	166						
4 15	40	44	48	52		24	84		101 105	108	11 25	111		143	150 154		20		146 151	163 168	175 180	42	41	492	533	574	615
4 16	44	48	52	56		25	86			115		-		-		17	22	142	157	176	187	-	42	504	546	588	630
4 17	44	48	56 56	60 60	8	9	40	49	AD	66	12 12	72	84	96 92	96		23		163	181	196		43	516 528	559	645 660	688
4 19	46 49	50 53	57	60 64	8	8	40	48 46	48 54	56 55	12 13	71 78	81 86	94	95 104		24		168	187 196	203		44	528 540	572 585	660 675	704
4 20	52	60	64	68	8	10	44	48	56	60	12 15	84	93	102	108							-		-	_		
4 21	52	59	64	72	8	11	48	53	61	64	12 16	88	96	108	116		18		162	180	180		46		644	690	736
4 22	56 57	62 64	66 69	72 76	8	12 :	52 54	60 62	64 67	68 72	12 17	96	100	112	119		19		142	150	176		47	564 576	658 672	705 720	752 768
4 24	60	68	76	80	8	14	58	64	72	76	12 19	99	108	121	130		21		159	177	189		49	637	686	735	833
4 25	63	68	75	84	8	15	60	67	75	81	12 20	104	116	128	140	18	22	148	164	1B4	196	50	50	650	700	800	850
																						444					

## Critical values for the Kruskal-Wallis test (small sample sizes)

$$H = \frac{12}{N(N+1)} \sum_{i=1}^{k} \frac{R_i^2}{n_i} - 3(N+1)$$

4 3 samples (N ≤ 19)

	1620:		a 0%	5%	2%	1%
1	1	1				
2	1	1	1			
2	2	1	1			
2	2	2	4 5 7 1			
3	1	1	İ			
3	2	1	4 286			
3	2	2	4 500	4 714		
3	3	7	4 577	5 143		
3	3	2	4 556	5 361	6 250	
3	3	3	4 622	5 600	6 489	7 200
4	1	1				
4	2	1	4 500			
4	2	2	4 458	5 333	6 000	
4	3	1	4 056	5 208	0.344	
4	3	3	4.511	5 444	6 564	6 745
4	4	1	4 167	4 967	6 667	6 667
4	4	2	4 555	6 465	6 600	7 076
4	4	3	4 545	5 598	6 712	7 44
4	4	4	4 654	5 692	6 962	7 654
5	1	7				
5	2	1	4 200	5 000		
5	2	2	4 373	5 160	6 000	6 533
8	3	1	4 018	4 960	6 044	0.000
5	3	3	4 533	5 251	6 533	6 909 7 079
5	4	1	3.987	4 985	6 4 3 7	6 955
5	4	2	4 541	5 2 7 3	6 505	7 205
S	4	3	4 549	5 656	8 6 7 6	7 445
5	4	4	4 668	5 667	6 953	7 760
6	5	1	4 109	5 127	6 146	7 309
5	5	2	4 623	5 338	6 446	7 338
5	5	3	4 545 4 523	5 705 5 666	6 866 7 000	7 5 7 8 2 3
5	5	5	4 560	5 780	7 220	8 000
6	1	1	-			
6	2	1	4 200	4 B22		
6	2	2	4 545	5 346	6 182	6 655
б	3	1	3 909	4 855	6 2 3 6	6873
6	3	2	4 682	5 348	6 227	6 9 70
6	3	3	4 590	5 615	6 590	7 410
6	4	2	4 038	4 947 5 340	6 5 7 1	7 106
	4	3	4 604	5 610	6 725	7 500
6			4 004		0 123	
	4	4	4 595	5 681	6 900	7 795
6				5 681 4 990		7 795 7 182
6 6 6	4 5 5	1 2	4 595 4 128 4 596	4 990 5 338	6 900 6 38 6 586	7 795 7 182 7 376
6 6 8	4 5 5 5	1 2 3	4 595 4 128 4 596 4 535	4 990 5 338 5 602	6 900 6 38 6 586 5 829	7 795 7 182 7 376 7 590
6 6 6 6	4 5 5 5 5	4 1 2 3 4	4 595 4 128 4 596 4 535 4 522	4 990 5 338 5 602 5 661	6 900 6 38 6 586 5 829 7 0 8	7 795 7 182 7 376 7 590 7 936
6 6 6 6 6 6	4 5 5 5 5 5	4 2 3 4 5	4 595 4 128 4 596 4 535 4 522 4 547	4 990 5 338 5 602	6 900 6 38 6 586 5 829 7 0 8 7 110	7 795 7 182 7 376 7 590 7 936 8 028
6 6 6 6	4 5 5 5 5	4 1 2 3 4	4 595 4 128 4 596 4 535 4 522	4 990 5 338 5 602 5 661 5 729	6 900 6 38 6 586 5 829 7 0 8	7 795 7 182 7 376 7 590 7 936
6 6 6 6 6 6	4 5 5 5 5 5 6	4 1 2 3 4 5 1	4 595 4 128 4 596 4 535 4 522 4 547 4 000	4 990 5 338 5 602 5 661 5 729 4 945	6 900 6 38 6 586 6 829 7 0 8 7 110 6 286	7 795 7 182 7 376 7 590 7 936 8 028 7 121
6 6 8 6 6 6 6	4 5 5 5 5 6 6 6 6	4 1 2 3 4 5 7 2 3 4	4 595 4 128 4 596 4 535 4 522 4 547 4 000 4 438 4 568 4 548	4 990 5 338 5 602 5 661 5 729 4 945 5 410 5 625 5 724	6 900 6 38 6 586 6 829 7 0 8 7 110 6 286 6 667 6 900 7 107	7 795 7 182 7 376 7 590 7 936 8 028 7 121 7 467
6 6 6 6 6 6 6 6	4 5 5 5 5 6 6 6 6	4 1 2 3 4 5 7 2 3 4 6	4 595 4 128 4 596 4 535 4 522 4 547 4 000 4 438 4 568 4 548 4 548	4 990 5 338 5 602 5 661 5 729 4 945 5 410 5 625 5 724 5 765	6 900 6 38 6 586 5 829 7 0 8 7 110 6 286 6 667 6 900 7 107 7 152	7 795 7 182 7 376 7 590 7 936 8 028 7 121 7 467 7 725 8 000 8 124
6 6 6 6 6 6 6 6 6	4 5 5 5 5 6 6 6 6	4 1 2 3 4 5 7 2 3 4	4 595 4 128 4 596 4 535 4 522 4 547 4 000 4 438 4 568 4 548	4 990 5 338 5 602 5 661 5 729 4 945 5 410 5 625 5 724	6 900 6 38 6 586 6 829 7 0 8 7 110 6 286 6 667 6 900 7 107	7 795 7 182 7 376 7 590 7 936 8 028 7 121 7 467 7 725 8 000
6 6 6 6 6 6 6 6 6 6 7	4 5 5 5 5 5 6 6 6 6 6	4 1 2 3 4 5 7 2 3 4 6	4 595 4 128 4 596 4 535 4 522 4 547 4 000 4 438 4 568 4 548 4 548 4 643	4 990 5 338 5 602 5 661 5 729 4 945 5 410 5 625 5 724 5 765 5 801	6 900 6 38 6 585 5 829 7 0 8 7 110 6 286 6 667 6 900 7 107 7 152 7 240	7 795 7 182 7 376 7 590 7 936 8 028 7 121 7 467 7 725 8 000 8 124 8 222
6 6 6 6 6 6 6 6 6 7 7	4 5 5 5 5 5 6 6 6 6 6 6 6 1 2	4 1 2 3 4 5 7 2 3 4 5 6	4 595 4 128 4 596 4 535 4 522 4 547 4 000 4 438 4 568 4 548 4 548 4 542 4 643	4 990 6 338 5 602 5 661 5 729 4 945 5 410 5 625 5 724 5 765 5 801	6 900 6 38 6 586 5 829 7 0 8 7 110 6 286 6 667 6 900 7 107 7 152 7 240	7 795 7 182 7 376 7 590 7 936 8 028 7 121 7 467 7 725 8 000 8 124 8 222
6 6 6 6 6 6 6 6 7 7 7	4 5 5 5 5 5 6 6 6 6 6 6 6 6	4 1 2 3 4 5 7 2 3 4 6 6	4 595 4 128 4 596 4 535 4 522 4 547 4 000 4 438 4 568 4 548 4 542 4 643 4 267 4 200 4 526	4 990 5 338 5 602 5 661 5 729 4 945 5 410 5 625 5 724 5 765 5 801	6 900 6 38 6 586 5 829 7 0 8 7 110 6 286 6 667 6 900 7 107 7 152 7 240 5 891 6 058	7 795 7 182 7 376 7 590 7 936 8 028 7 121 7 467 7 725 8 000 8 124 8 222
6 6 6 6 6 6 6 6 6 7 7 7 7 7 7	4 5 5 5 5 5 6 6 6 6 6 6 6 6 6	1 2 3 4 5 7 2 3 4 6 6 6	4 595 4 128 4 596 4 535 4 522 4 547 4 000 4 438 4 568 4 548 4 542 4 643 4 267 4 200 4 526 4 173	4 990 5 338 5 602 5 661 5 729 4 945 5 410 5 625 5 724 5 765 5 801 4 706 5 143 4 952	6 900 6 38 6 586 5 829 7 0 8 7 110 6 286 6 667 6 900 7 107 7 152 7 240 5 891 6 058 6 043	7 795 7 182 7 376 7 590 7 936 8 028 7 121 7 467 7 725 8 000 8 124 8 222 7 000 7 030
6 6 6 6 6 6 6 6 6 7 7 7 7 7	4 5 5 5 5 5 6 6 6 6 6 8 1 2 2 3 3	4 1 2 3 4 5 7 2 3 4 6 6	4 595 4 128 4 596 4 535 4 522 4 547 4 000 4 438 4 568 4 548 4 542 4 643 4 267 4 200 4 528 4 173 4 582	4 990 5 338 5 602 5 661 5 729 4 945 5 410 5 625 5 724 5 765 5 801 4 706 5 143 4 952 5 357	6 900 6 38 6 586 5 829 7 0 8 7 110 6 286 6 667 6 900 7 107 7 152 7 240 5 891 6 058 6 043 6 339	7 795 7 182 7 376 7 590 7 936 8 028 7 121 7 467 7 725 8 000 8 124 8 222 7 000 7 030 6 839
6 6 6 6 6 6 6 6 6 7 7 7 7 7 7	4 5 5 5 5 5 6 6 6 6 6 6 6 6 6	1 2 3 4 5 6 6 1 1 2 1 2	4 595 4 128 4 596 4 535 4 522 4 547 4 000 4 438 4 568 4 548 4 542 4 643 4 267 4 200 4 526 4 173	4 990 5 338 5 602 5 661 5 729 4 945 5 410 5 625 5 724 5 765 5 801 4 706 5 143 4 952	6 900 6 38 6 586 5 829 7 0 8 7 110 6 286 6 667 6 900 7 107 7 152 7 240 5 891 6 058 6 043	7 795 7 182 7 376 7 590 7 936 8 028 7 121 7 467 7 725 8 000 8 124 8 222 7 000 7 030
6 6 6 6 6 6 6 6 6 7 7 7 7 7 7 7 7 7 7 7	4 5 5 5 5 5 6 6 6 6 6 6 6 6 7 2 2 3 3 3	1 2 3 4 5 5 6 6 1 1 2 1 2 1 2 3	4 595 4 128 4 596 4 535 4 522 4 547 4 000 4 438 4 548 4 548 4 542 4 643 4 267 4 200 4 528 4 173 4 582 4 603	4 990 5 338 5 602 5 661 5 729 4 945 5 410 5 625 5 724 5 765 5 801 4 706 5 143 4 952 5 367 5 620	6 900 6 38 6 586 5 829 7 0 8 7 110 6 286 6 667 6 900 7 107 7 152 7 240 5 891 6 058 6 043 6 339 6 666	7 795 7 182 7 376 7 590 7 936 8 028 7 121 7 467 7 725 8 000 8 124 8 222 7 000 7 030 6 839 7 228
6 6 6 6 6 6 6 6 6 6 7 7 7 7 7 7 7 7 7 7	4 5 5 5 5 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6	1 2 3 4 5 6 1 1 2 1 2 3 1 2 3	4 595 4 128 4 596 4 535 4 522 4 547 4 000 4 438 4 568 4 548 4 542 4 643 4 267 4 200 4 528 4 173 4 582 4 603 4 121 4 549 4 527	4 990 5 338 5 602 5 661 5 729 4 945 5 410 5 625 5 724 5 765 5 801 4 706 5 143 4 952 5 320 4 986 5 376 5 623	6 900 6 38 6 586 6 829 7 0 8 7 110 6 286 6 667 6 900 7 107 7 152 7 240 5 891 6 058 6 043 6 339 6 666 6 319 6 447 6 780	7 795 7 182 7 376 7 590 7 936 8 028 8 028 8 121 7 467 7 725 8 000 8 124 8 222 7 000 7 030 6 839 7 228 6 986 7 321 7 550
6 6 6 6 6 6 6 6 6 6 7 7 7 7 7 7 7 7 7 7	4 5 5 5 5 5 6 6 6 6 6 6 6 6 6 6	1 2 3 4 5 6 1 1 2 1 2 3 1 2	4 595 4 128 4 596 4 535 4 522 4 547 4 000 4 438 4 548 4 548 4 542 4 643 4 267 4 200 4 526 4 173 4 582 4 603 4 121 4 549	4 990 5 338 5 602 5 667 5 729 4 945 5 410 5 625 5 724 5 765 5 801 4 706 5 143 4 952 5 357 5 620 4 986 5 376	6 900 6 38 6 586 6 829 7 0 8 7 110 6 286 6 667 6 900 7 107 7 152 7 240 5 891 6 058 6 058 6 043 6 339 6 656 6 319 6 447	7 795 7 182 7 376 7 590 7 936 8 028 8 1 21 7 467 7 725 8 000 8 124 8 222 7 000 7 030 6 839 7 228 6 986 7 321

	SPITT	ple	g	10%	5%	2%	1%
	5:2	BE .	1	70.0	338		
7	5	3	1	4 535	5 607		7 69 7
7	5	4	1	4 542	5 733		
7	5	5	1	4 571	5 708		8 108
7	6	1		4 0 3 3			7 254
7	6	3		4 500 4 550	5 357 5 689		7 756
7	6	4		4 562	5 706		8 039
7	6	5		4 560	5 770		8 157
7	6	6		4 530	5 730		
7	7	1		3 986	4 986		7 157
7	7	2		4 491			7.491
7	7	3		4 613	5 688		7 810
7	7	4		4 563	5 766	7 145	8 142
7	7	6		4 546	5 746	7 247	8 257
8	4	2		4 4 1 8			
8	2	2		4011	4 909	6 000	
8	2	2		4 587	5 356		6 663
8	3	ŧ		4 0 1 0	4 881		6 804
8	3	2	1	4 451	5 3 1 6	6 371	7.022
8	3	3		4 543	5 617		7 350
8	4	1		4 038	5 044	6 140	6.973
8	4	2		4 500	5 393	6 5 3 6	7 350
В	4	3		4 529	5 623	6 854	7 585
В	4	4		4 561	5 779	7 0 7 5	7 853
B	5	1		3 967	4 869	6 257	7 1 1 0
В	5	2		4 466	5 4 1 5	6 5 7 1	
В	5	3		4 5 1 4	5614		7 706
8	5	-4		4 549	5 718	7 051	-
В	5	5		4 555	5 769	7 159	8 116
₿	6	1		4 015	5.015		
8	6	2		4 463	5 404		
В	6	3		4 575			
8	6	4		4 563	5 743		
8	6	5		4 550	5 750		
8	7	2		4 045	5 041		7 308
8	7	3		4 451	5 403		
8	7	4		4 556 4 548	5 698		7 827
8	8	1		4 044	5 0 19		
В	8	2		4 509	5 408		7 654
B	8	3		4 555		7.021	889
9	3	1		A CAE			
9	2	1		4 545 3 906	4 842	5 662	6 744
9	2	Z		4 484	5 4 60		
9	3	9		4 073	4.952		
9	3	2		4 492	5 440		7.006
9	3	3		4 633	5 5 8 9		
8	4	٩		3971	5		
8	4	2		1 489	5 400	6518	7 364
9	4	3		4 526	5 452		
9	6	4		4 5 16	5 104	4 390	7.910
9	5	4		4 066	5 740		
9	5	2		\$ 465	5 396		
9	5	3		4 58 7	5 6 0		
9	5	-5		\$ 53.	5 7 7 3		
9	5	5		3 557	5 ''0		
9	6	1		1 953	5 349		
9	6	2		3 481	5 392		
9	6	3		4 548	5 6 745		
9	7	1		g = 1	5 745		
9	7	2		4 480	5 429		
8	7	3		1547	5 656		
9	8	1		3 986	4 985		
9	8	2		492	5 420		
9	9	1		1 007	4 961		
+		_		_			
0	1 2	1		1 654	4 654 4 840		6 470
0	44			- 114			6 429
		2		1434	13 3 7 1		
10 10	2	2		1 434 3 9 <del>9</del> 6	5 120		6 537

9	amp		a 10%	5%	2%	1%
10	3128	3	4 529	5 588	6 784	7 372
10	4	1	4 042	5.018	6.158	7 105
10	4	z	4 462	5.345	6.492	7 357
10	4	3	4 588	5 661	6.905	7.617
10	4	4	4 565	5.716	7 085	7 907
10	5	1	3 988	4 954	6.318	7 178
10	5	2	4 455	5.420	6.612	7 514
10	5	3	4 552	5.638	6.938	7 752
10	5	4	4 557	5.744	7 135	8.048
10	6	1	3 967	5 D42	6.383	7,316
10	6	2	4 480	5 406	6.669	7 588
10	6	3	4 551	5 658	7.002	7 882
10	7	1	3 981	4 986	6.370	7 252
10	7	2	4 492	5.377	6.652	7 841
10	8	1	3 964	5 038	6.414	7 359
			-		0,7,7	- 557
11	7	1	4 028	4 747	_	-
11	2	1	4 044	4 816	5.834	6 600
11	2	2	4 414	5.164	6.050	Ø 765
11	3	1	3 985	5 030	5.030	818
11	3	3	4 487	5 374	6.370	7.094
111	3	3	4 589	5 583	6.776	7.418
11	4	1	3.991	4 988	6,111	7 090
11	4	7	4 484	5 365	6 553	7.396
11	4	3	4 538	5 880	6.881	7 679
11	4	4	4 550	5 740	7.036	7 945
11	5	1	4 028	5 020	6.284	7 130
3.1	5	2	4 490	5 374	6 648	7 507
11	5	3	4 550	5.646	6.962	7.807
11	6	1	4 029	5.062	6.304	7 261
11	6	2	4 463	5 408	8.693	7 564
11	7	1	4 045	4 985	6 409	7 330
12	)	1	4 148	4 829	-	-
12	2	1	4 092	4 875	5 550	6 229
12	2	2	4 379	5 173	5 967	6 761
12	3	1	3 930	4 930	6.018	6.812
37	3	2	4 477	5 350	6.412	7 134
12	3	3	4 579	5 5 7 6	6.746	7,471
12	d	1	4 003	4 931	6 225	7 108
12	4	2	4 500	5.442	6 547	7 389
12	4	3 .	4 524	5.661	6.903	7,703
12	5	1	3 985	4 977	6.326	7.215
12	5	2	4 486	6 398	6.649	7 512
12	6	1	4 050	5.006	8.371	7 297
1,3	1	1	4 254	4 900		
13	2	1	3 989	4.819	5 727	6.312
13	2	2	4 385	5 199	6 134	6.792
13	3	1	4 095	5.024	6 081	6.846
13	3	2	4 485	5 371	6 407	7 138
13	3	3	4 539	5.613	6 755	7,449
13	4	1	4 045	4 963	6 325	7 052
13	4	2	4 484	5 368	6 587	7 434
13	5	7	4 043	4 993	6 288	7 238
14	7	1	3 728	4 963	-	
14	2	7	4 070	4.863	5 737	6 356
14	2	2	4 441	5.193	6 045	6.812
14	3	3	4 075	4 977	6 029	6 811
14	3	2	4 515	5.383	6.413	7,218
14	3	3	4 020	4 991	6 265	7 176
15	1	3	3.843	5,020		
15	Z	1	4 032	4.827	5 599	6 053
15	2	2	4.461	5.184	6 044	6 760
15	3	7	4 055	5 019	6 139	6.813
16	2	1	3 886	4.511	5 070	
16	2	1	4 044	4.849	5 670	6.189
-	-					
17	1	7		4 581		
p.c	carp	dia .	4 606	5.991	7 824	9,210

		3	4 Jampies NS 14		
sample 5)2RS	a 10% 5% 2° 1%	sample sizes	α 3° 5% 2 3%	sizer 6 5 2 1	a 10% \$% 2% 1%
2 1 1 1		5 2 1 1	536 5960 6600 5542 6109 632 2.6	6 6 1 1	5 589 5 541 7 598 8 389 5 219 5 133 7 275 8 181
2 2 1 1	5 357 5 679	5 2 2 2 5 5 3 1 1	5 60 6 604 6 964 1 300	7 1 1	5 9 5 845 5 09 6 No 6 186 2 3
3 1 1 1	5 667 5 167 6 661 6 66	5 3 2 . 5 3 2 2 5 3 3 1	55 P ( 164   185   58 5 12 8 8 6 4 1 6 2 6 8 8 9 9 5 6 6 4 1 6 5 6 8 2 6	7 2 2 1 7 2 2 2 7 1 1 1	5 4 6 7 5 6 5 6 8 6 5 7 5 7 5 7 5 7 5 7 5 7 5 7 5 7 5 7 5
3 2 1 1 3 3 2 7 1	5 4.7 5 556 5 833 6 500	5 3 3 2 6 1 3 3	5 86t + 8 1 2 8 to 60.1 10 # 8 24 8 448	7 3 2 1 7 3 2 2	4 h E 6 466 3B 4 005
3 2 2 2	5 644 6 33 6 9 8 33 5 333 6 313	5 4 7 1	\$755 AG4 1.3. 305 \$501 649 4 8 3	7 3 3 7 4 t	the francis
3 1 2 1 3 3 2 2 3 3 3 1	5 689 6 244 6 684 200 5 145 6 52 81 6 20 6 655 6 660 7 00 4 10	5 4 2 7	6 82 34 49 82 6 64 6 4 6 4 10 6 70 4 49 82	7 4 2	5 611 5 9 40
3 3 3 3	589 677 1536 80 5 6026 100 87 8 38	5 6 8 1	4 - 3 - 6 P	B 1 1 1 B 2 1 1	3 25 F 18
4 1 1 7	5 260 5.833	6	58 1 P 2 1 1 (1)	8 2 2 2 3 8 3 1	1 44 1 10 14 14 14 14 14 14 14 14 14 14 14 14 14
4 2 2 2	5595 , 32 666 1000 515 5545 06 79	6 1 1 1	56 - 644	8 4 4 1	5 6 ALA 05 8 A
4 1 2 1	5 061 8 78 6 1 16 5 693 6 309 1 0 8 95 5 750 6 62 7 63 6	6 2 7 1	4 2 At 4 5 C A 15	g 1 1	99 V 9
4 3 3 1	5 689 6 545 464 74A	6 7 ,		9 2 2 1	
4 3 3 3	60 8 6946 7 445 9 3 5 82 5 945 (8) 7 466	6 3 7 4 6 >		10 1 1	4.4
4 4 2 2	5 668 6 386 7 364 955 5 808 6 3 15 6 3 5 672 956 7 660 81	6 4 7	4 × 4 × × × × × × × × × × × × × × × × ×	10 7	4 4 4
6 4 1 2	590 684 79 gA, 60 % 878 84	6 4 7 2			6 251 7 815 9 437 11 34
4 4 4 2	5644 645 E 4 F HB	651)	6 × - 9		
Silve	e FON: 8% 2 1%	z cu) ctrodkyń	5% . 1%	strance	9 5% 1%
1 1 1 1		4 7 2 1	* 1 * * * * * * * * * * * * * * * * * *	5 1 1	6 388 7 154 8 235 ···· 6 679 7 520 8 492 k
2 1 + 1 2 2 1 1	5 86 5 250 F 50	4 7 5 4	E +	6	6 356 7776 8 334
7 2 2 2 1	6 98 14 8 8 1 H,	4 2 2 2	6 k	6 /	6 286 6 009 7 682 8 00 6 5 7 7 3 08 8 05 1 8 62 5 6 60 2 7 5 9 3 8 5 4 9 9 0 7
2 1 1 1	619 6583	# S 2 1	prr u .	6	1 6 602 7 593 8 549 9 07 1 6 423 7 051 8 064 8 59 1 6 648 7 505 8 407 9 00
2 2 1 1 2 2 2 1 2 2 2	6 055 682 6302 654	4 4 2 2	2 4 387	G 4	f-396 7187 8286 903
3 1 1 1 3 2 3 1	6 11 7 4 6 600 70K 7A 0	5 1 1 1		7 1	6 187 6.831 7.455 6 368 6 984 7.763 8.73 1 6 593 7.356 8 143 8 68
3 2 2 1	6 786 51 R 25P 4 F F	5 7 1 1 1 5 2 2 1 1	F + 1 ps .	7 3 1	6 367 7 152 8 119 B 779
3 3 1 T 3 3 2 T 3 3 2 2	6 188 75 6 dail death 6 9 0 7 84 859 775 121 8 044 9 1 9 51	5 7 2 7 2	F 100 Fac -> 1	9 . ,	100
3 3 3 1	אָבֶּ אָאָ אָרָה דיָטָי מוח אָ דיָטָי	6 3 2 7 1	6 864 14 8 7 7 8 54 5 864 14 8 7 7 8 7 5	9 - 1 1	5 095 6 755 7 458 8 044
2 1 1 1	6 167 — 6 200 8 733 7 267 —	5 3 3 1 1	6 15 684 Bt5 9 A	Bb 74. X 3	7 779 9 488 11 67 13 28
			Euroe Acti		
1 701	0 10 5% 1 1%	tample 1781		sample	
1 1 1 1		3 5 7 7 3 1 1 1 3 2 1 7 1	8 1 d 2 9 714 10 15 9, 474 9 205 9 564 5 3 4 8 9 3 9 670 10 08	5 7 2 7	
7 1 1 7 2 2 1 1 7	6 8 3 3 26 7 600 800	4 1 5	- 1	5 4 . 5 6 1 1	7 701 8 495 9 371 9
2 2 1 1 2 2 2 1 2	52 0 8 8455 5 F A 905 4 455 7 367 3 8 F4 8 8 8 6 7 3 H + 2 4	4 2 7 7 4 2 7 1 4 2 7 1 1		6 1	
1 1 1		4 2 2 2 2 4	P 33 99 19 193	6 7 1	7 7 7 626 8 374 9 165 9
1 1 1 1 2 2 2 1 1	7 133 7461 4 8 1945 8 345 6 500	4 2 2 1 1 1	24844, 0	7	7 198 7 791 8 846 8
2 2 2 1 1 2 2 2 2	7 .7 8 148 8 7190 + F 98 8 , 9 .46 4 17 A 98 9 0 33 9 8 2 40 ,	4 4 1 3 7	4 4 9 · · · · · · · · · · · · · · · · ·	8 1	7 194 7 788 8 712 9
2 1 1 1 2 2 3 1	1400 000 R Sed 8 164 1697 8 301 8 801 1 045	5 1 , 1	25 672		
2 2 3 1	8 2 8 5 4 4 4 36 ] + 8	5 2 1 1 1 1	7 345 7891 8 4*3 8 682		

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## Critical values for the Kruskal-Wallis test (equal sample sizes)

$$H = \frac{12}{n^2k(nk+1)} \sum_{i=1}^{11} R_i^2 - 3(nk+1)$$

		k 3			
10	10%	5%	2%	1%	1
2	4 571				5
3	4 622	5 600	6 489	7 200	6
4	4 654	5 692	6 962	7 654	6
5	4 560	5 780	7 220	8 000	6
6	4 643	5 801	7 240	8 222	6
7	4 594	5 819	7 332	8 3 7 8	6
8	4 595	5 805	7 355	B 465	6
9	4 586	5 831	7.418	8 529	6
10	4 581	5.853	7 453	8 60 7	6
11	4 587	5 885	7 489	8 648	6
12	4 578	5 8 7 2	7 523	8 712	6
13	4 601	5 90 1	7 551	8 735	6
14	4 592	5 896	7 566	8 754	6
15	4 591	5 902	7 582	8 821	6
16	4 595	5 909	7 596	8 822	6
17	4 593	5 915	7 609	8 856	6
18	4 596	5 932	7 522	8 865	6
19	4 598	5 923	7 634	8 887	6
20	4 594	5 928	7 641	8 905	- 6
21	4 59 7	5 930	7 652	8918	6
22	4 597	5 932	7 657	8 928	6
23	4 598	5 9 3 7	7 664	8 94 7	6
24	4 598	5 936	7 670	8 964	6
25	4 599	5 942	7 682	8 976	6
00	4.605	5,991	7.824	9.210	6

	k =	4	
10%	5%	2%	1%
5 667	6 167	6 667	6 667
6 026	7 000	7872	B 538
880 6	7 235	8 5 1 5	9 287
6 120	7 377	8 863	9 789
6 127	7 453	9 027	10.09
6 141	7.501	9 152	10.25
6 t4B	7 534	9 250	10 42
6 161	7 55 7	9 3 1 6	10.53
6 67	7 586	9 376	10.62
6 163	7 623	9 422	10 69
6 185	7 629	9 458	10.75
6 191	7 645	9 481	10.80
6 198	7 658	9 508	10 84
6 201	7 676	9 531	10.87
6 205	7 6 7 8	9 550	10 90
6 206	7 682	9 568	10 92
6 212	7 698	9 583	10.95
6 212	7.701	9 595	10 98
5 216	7 703	9 606	10 98
6 218	7 709	9 623	11.01
6 215	7.714	9 629	11 03
6 220	7 719	9 640	11 03
6 221	7 724	9 652	11 06
6 222	7 727	9 659	11 07
6.251	7.815	9.837	11:34

	k :	- 5	
10%	5%	2%	1%
6 982	7.418	8 073	8 291
2 333	8 333	9 467	10.20
7 457	8 685	10.13	11.07
7 532	8 8 7 6	10 47	11.57
7 557	9 002	10 72	11.91
7 600	9 080	10.87	12 14
7 624	9 126	10 99	12 29
7 637	9 166	11.06	12 41
7 650	9 200	11 13	12 50
7 660	9 242	11 19	12 58
7 675	9 274	11 22	12 63
7 685	9 303	11.27	12 69
7 695	9 307	11 29	12 74
7 701	9 302	11.32	12 77
7 705	9 313	11.34	12 79
7 709	9 325	11.36	12 83
7.714	9 334	11.38	12.85
7.717	9 342	11 40	12 B7
7.719	9 353	11.41	12.91
7 723	9 356	11 43	12 92
7 724	9 362	11.43	12 92
7 727	9 368	11.44	12 94
7 729	9 375	11 45	12 96
7 730	9 377	11 46	12.96
7 779	9,488	11.07	13.28

	Г	k 6		
10%	5%	2%	1%	9/
8 154	8 846	9 538	9 846	2
8 620	9 789	11 03	11.82	3
8 800	10 14	11.71	12 72	4
8 902	10 36	12 07	13 26	5
8 958	10.50	12 33	13 60	6
8 992	10 59	12 50	13 84	7
9 0 3 7	10 66	12 62	13 99	8
9 057	10.71	12.71	14.13	9
9 0 7 8	10.75	12.78	14 24	10
9 093	10.76	12 84	14 32	11
9 105	10.79	12 90	14 38	12
9 1 1 5	10.83	12 93	14 44	13
9 1 2 5	10.84	12 98	14 49	14
9 133	10 86	13 01	14 53	15
9 140	10.88	1303	14 56	16
9 144	10.08	13 04	14 60	1.7
9 149	10.89	13 06	14 63	18
9 156	10.90	13 07	14 64	19
9 159	10 92	13.09	14 67	20
9 164	10.93	13 11	14.70	21
9 168	10.94	13 12	14.72	22
9 171	10 93	13 13	14.74	23
9 1 70	10 93	13 14	14.74	24
9 1 2 7	10.94	13.15	14.77	25
9.236	11.07	13.39	15.09	cuD

For description, see page 28.

### Critical values for Friedman's test

$$M = \frac{12}{nk(k+1)} \sum_{i=1}^{k} R_i^2 - 3n(k+1)$$

		k 3		
10	10%	5%	2%	1%
2	-		_	
3	6 000	6 000		
4	6 000	6 500	8 000	8 000
5	5 200	6 400	B 400	8 400
6	5 333	7 000	8 333	9 000
7	5 429	7 143	8 000	8 857
В	5 250	6 250	7 750	9 000
9	5 556	6 222	8 000	9 556
10	5 000	6 200	7 800	9 600
11	5 091	6 545	7 8 1 8	9 455
12	5 167	6 500	8 000	9 500
13	4 769	6 6 1 5	000 B	9 385
14	5 143	6 143	8.143	9 143
15	4 933	6 400	8 133	8 933
16	4 875	6 500	7 875	9 3 7 5
17	5 059	6 1 18	7 529	9 294
18	4 778	6 333	8 111	9 000
39	5 053	6 421	7 895	9 5 7 9
20	4 900	6 300	7 900	9 300
21	4 952	6 095	7 714	9 238
22	4 727	6 091	8 273	9 091
23	4 957	6 348	8 087	9 391
24	5 083	6 250	7 750	9 250
25	4 880	6 080	7 760	8 960
402	4.605	5.991	7.824	9.210

		"	
10%	5%	23	1%
6 000	6 000		
6 600	7 400	8 200	9.000
6.300	7 800	8 400	9 600
6 360	7 800	9 000	9 960
6 400	7 600	9 400	10 20
6 4 2 9	7 800	9 171	10 54
6 300	7 650	9 450	10 50
6 200	7 66 7	9 400	10.73
6 360	7 680	9 480	10.68
6 273	7 691	9 655	10.75
6 300	7 700	9 500	10.80
6 138	7 800	9 646	10.85
6 343	7.714	9 600	10.89
6 280	7 720	9 640	10 92
6 300	7 800	9 600	10 95
6 3 1 8	7 800	9 635	11.05
6 333	7 733	9 667	10 93
5 347	7 863	9 632	11.02
6 240	7 800	9 600	11.10
6 314	7 800	9 686	11 06
6 327	7.800	9 709	11.07
6 287	7 800	9 678	11 09
6 250	7 750	9 700	11 15
6 264	7 800	9 6 7 2	11 16
6.251	7 815	9.837	11 34

		5	
101	5%	29	1%
7 200	7 600	8 000	8 000
7 467	8 533	9 600	10 13
7 600	8 800	10.20	11.20
7 680	8 960	10.56	11.68
7 733	9 067	10.80	11.87
7 771	9 143	10 97	12.11
7.700	9 200	11 00	12.30
7 733	9 244	11.11	12 44
7 760	9 280	11.20	12 48
7 782	9 309	71.20	1258
7 733	9.333	11.27	12 60
7 754	9 354	11 32	12.68
7.771	9 371	11 37	12.74
7 787	9 38 7	11 36	12.80
7 750	9 400	11.40	12 80
7.765	9 412	11.44	12.85
7 778	9 422	11.47	12 89
7 789	9 432	21.45	12 88
7 760	9 400	11 48	12 92
7 771	9 448	11 50	12 91
7 782	9 4 1 8	11 49	12 95
7 791	9 426	1151	12 97
7 767	9 433	11.50	13.00
7 776	9 440	11.52	12 99
7 779	9.488	11 67	13.28

		k = 6		
10%	5%	2%	1%	9,
8 286	9 143	9 429	9 714	2
8 714	9 857	11.00	11 76	3
9 000	10.29	11 71	12.71	4
9 000	10 49	12 09	13 23	5
9 048	10 57	12 38	13 62	8
9 122	10 67	12 55	13 86	7
9 0 7 1	10.71	12 64	14 00	В
9 127	10.78	12.75	14 14	9
9 143	10 80	12 BO	14 23	10
9 130	10 84	12 92	14 32	11
9 143	10 86	12 95	14 38	12
9 176	10 89	13.00	14 45	13
9 184	10.90	13 02	14 49	14
9 2 1 0	10 92	13 00	14 54	15
9 214	10 96	13 07	14.57	16
9 202	10 95	13 10	14 61	17
9 206	10 95	13 11	14 63	18
9 196	11 00	13 14	14 67	19
9 200	11.00	13 11	14 66	20
9 218	10 99	13 14	14 69	21
9 221	10 96	13 14	14.73	22
9 236	11.00	1319	14 73	23
9 238	10 95	13 19	14 74	24
9 229	10.99	13.21	14 74	25
9.236	11 07	13.39	15.09	CHO.

### Critical values for nonparametric tests with large samples

For all the eight tests dealt with on pages 26-34 there are approximate methods for finding critical values when sample sizes exceed those covered in the tables

Approximate critical values for the sign test, Wilcoxon signed-rank test and Mann—Whitney U test may be found from the table of percentage points of the standard normal distribution on page 20. Denote by a the appropriate percentage point of the standard normal distribution, e.g. 1 9600 for an  $\alpha_1=5\%$  two-sided test or 1 6449 for an  $\alpha_1=5\%$  one-sided test. Then calculate  $\mu$  and  $\sigma$  from the table below. The required critical value is  $[\mu=2\sigma-\frac{1}{2}]$ , the square brackets denoting the integer part.

	ш	0
sign tust	§n	1vn
Wilcoxon signed rank test	4n(n + 1)	$\{\frac{1}{2}(n(n+1)(2n+1)\}^{1/2}$
Mann - Whitney U lest	4n1n2	$\{(2n_1n_2(n_1+n_2+1))^{1/2}$

For example in the sign test with sample size n=144,  $\mu=\frac{1}{2}(144)=72$  and  $\alpha=\frac{1}{2}\sqrt{144}=6$ , so that the  $\alpha_2=5\%$  critical value is  $[72-1.96\times 6-\frac{1}{2}]=[59.74]=59$ , i.e. the  $\alpha_2=5\%$  critical region is  $S\leqslant 59$ . The reader may verify similarly that (i) for the signed-rank test with n=144.  $\mu=5220$ ,  $\sigma=501.428$ , and the  $\alpha_2=5\%$  critical region is  $T\leqslant 42.36$ , and (ii) in the Mann. Whitney test with sample sizes 25 and 30.  $\mu=375$ ,  $\sigma=59.161$ , and the  $\alpha_2=5\%$  critical region is  $U\leqslant 258$ .

For the Kolmogorov-Smirnov goodness-of fit test, approximate critical values are simply found by dividing the constants b in the following table by  $\sqrt{n}$ 

0	5%	210	1%	10
۵,	10%	5%	2%	1%
b	1 2238	1 3581	1.5174	1.6276
c	0 8255	0 8993	0 9885	1.0500

So with a sample of size n=144, the  $\alpha_3=5\%$  critical value is 1.3581,  $\sqrt{144}=0.1132$ , i.e. the critical region is  $D_{144}\geqslant 0.1132$ . The same constants b are used to obtain approximate critical regions for the Kolmogorov-Smirnov two-sample test. In this case b is multiplied by  $\{1/n_1+1/n_2\}^{1/2}$  to give critical values for D (not  $D^n$ ). So with sample sizes 25 and 30,  $\{1/n_1+1/n_2\}^{1/2}=\{1/25+1/30\}^{1/2}=0.2708$  and the  $\alpha_2=5\%$  critical region is  $D\geqslant 1.3581 \times 0.2708=0.3678$ . For the Kolmogorov-Smirnov test for normality (with unspecified mean and standard deviation), the critical values are found as in the goodness-of-fit test except that the second row of constants c is used instead of b. In this case the  $\alpha_2=5\%$  critical region with n=144 is  $D_{144}\geqslant 0.8993/\sqrt{144}=0.0749$ .

Finally the Kruskal-Wallis and Friedman test statistics are, for large sample sizes, both distributed approximately as the  $\chi^2$  distribution with  $\nu=k-1$  degrees of freedom. The appropriate values have been inserted at the ends of the tables on pages 32–34,  $\alpha_1^R$  values from the  $\chi^3$  table (page 21) are appropriate

### Linear and rank correlation

When data consist of pairs (X,Y) of related measurements it is often important to study whether there is at least an approximate linear relationship between X and Y. The strength of such a relationship is measured by the linear correlation coefficient  $\rho$  (tho), which always lies between -1 and +1  $\rho=0$  indicates no linear relationship,  $\rho=+1$  and  $\rho=-1$  indicate exact linear relationships of + ve and - ve slopes respectively. More generally, values of  $\rho$  near 0 indicate little linear relationship, and values near +1 or -1 indicate strong linear relationships.

Tests etc concerning  $\rho$  are formulated using the sample linear correlation coefficient  $r=\Sigma(X-\bar{X})(Y-\bar{Y})/\{\Sigma(X-\bar{X})^2\Sigma(Y-\bar{Y})^2\}^2/\chi$ ,  $\bar{X}$  and  $\bar{Y}$  being the sample mean values of X and Y. The first table on page 36 is for testing the null hypothesis  $H_0$  that  $\rho=0$ . Critical regions are  $|r| \ge tabulated$  value if  $H_1$  is the two-sided alternative hypothesis  $\rho \ne 0$  (using significance levels  $\alpha_2$ ) or  $r \ge tabulated$  value or  $r \le -(tabulated value)$  if  $H_1$  is  $\rho > 0$  or  $\rho \le 0$  respectively (using levels  $\alpha_3^R$ )

The following data show the market value (in units of £10 000) of eight houses four years ago (X) and currently (Y)

X	0.8	1.7	2 4	09	12	16	1.7	29
Y	1.3	33	3.8	1.1	2.4	3 1	35	39

Here is found to be 0.89. 8. This is very strong evidence in favour of

the one-sided  $H_1$  p>0, since the  $\alpha_1^n=\frac{1}{2}\%$  critical region with sample size n=8 is  $r\geqslant 0.8343$ . Had  $\alpha_1^L$  critical values been required, they would have been given by the  $\alpha_1^R$  values prefixed with a minus sign

The construction of confidence intervals for  $\rho$  and the testing of values of  $\rho$  other than  $\rho=0$  may be accomplished using Pisher's z-transformation. For any value of r or  $\rho$ , this gives a 'z-value' z(r) or  $z(\rho)$ , computed from

$$\varepsilon(r) = \frac{1}{2}\log_{e}\left(\frac{1+r}{1-r}\right) = 1.1513\log_{10}\left(\frac{1+r}{1-r}\right)$$

and z(r) is known to have an approximate normal distribution with mean  $z(\rho)$  and standard deviation  $1/\sqrt{n-3}$ . A table giving z(r) is provided on page 36, and on page 37 there is a table for converting back from a z-value to its corresponding r-value or  $\rho$ -value. If r or  $\rho$  is - ve, attach a minus sign to the z-value, and vice versa.

So to find a  $\gamma=95\%$  confidence interval for  $\rho$  with the above data, we first find the 95% confidence interval for  $z(\rho)$  as  $\{z(r)-1.9600, \sqrt{n-3}, z(r)+1.9600, \sqrt{n-3}\}$  (the I.9600 being the  $\gamma=95\%$  value in the table of normal percentage points on page 20) where n=8 and z(r)=z(0.8918), which is about 1.4306 (interpolating between z(0.891)=1.4268 and z(0.892)=1.4316 on page 36). This interval works out to (0.554-2.307). These limits for the value of  $z(\rho)$  are then converted to  $\rho$ -values by the table on page 37, giving the confidence interval for  $\rho$  of (0.503-0.980). As a second example, if we wish to test  $H_0$ ,  $\rho=0.8$  against  $H_1$ ,  $\rho>0.8$  at the  $\alpha_1^R=5\%$  significance level, the critical value for z(r) would be  $z(0.8)+1.6449/\sqrt{n-3}$  1.0986 + 1.6449/ $\sqrt{n}=3$  1.0986 + 1.6449/ $\sqrt{n}=3$  2.0). The critical region  $z(r) \ge 1.834$  (the 1.6449 again coming from page 37, and so we are unable to reject  $H_0$ ,  $\rho=0.8$  in favour of  $H_1$ ,  $\rho>0.8$  at this significance level

An alternative and quoker method is to use the charts on pages 38–39. For confidence intervals locate the obtained value of r on the horizontal axis, trace along the vertical to the points of intersection with the two curves labelled with the sample size n, and read off the confidence limits on the vertical axis. For critical values, locate the hypothesised value of p, say  $p_0$ , on the vertical axis, trace along the horizontal to the points of intersection with the two curves, and read off the critical values on the horizontal axis. If these two values are  $r_1$  and  $r_2$ , with  $r_1 < r_2$ , then the one-sided critical regions with significance level  $\alpha_1$  for testing  $H_0$ ,  $p = p_0$  against  $H_1$ ,  $p < p_0$  or  $H_1$ ,  $p > p_0$  are  $r < r_1$  and  $r \ge r_2$  respectively, and the critical region with significance level  $\alpha_2 = 2\alpha_1$  for testing  $H_0$  against  $H_1$ ,  $p \ne p_0$  is comprised of both of these one-sided regions

The reader may check the charts for the results found above using the z-transformation. Accuracy may be rather hmited, especially when  $\epsilon$  and  $\rho$  are close to  $\pm 1$  or  $\pm 1$ , however the z-transformation methods are not completely accurate either, especially for small n. Further maccutaces may occur for sample sizes not included on the charts, in which case the user has to judge distances between the curves.

All of the above work depends on the assumption that (X, Y) has a bivariate normal distribution. Tables for two nonparametric methods, which do not require such an assumption, are given on page 40. These methods do not test specifically for linearity but for the tendency of Y to increase (or decrease) as Y increases.

To calculate Spearman's rank correlation coefficient, first rank the X-values and Y-values separately from 1 to n calculate the difference in ranks for each (X,Y) pair, and sum the squares of these differences to obtain  $D^2$ . Spearman's coefficient  $r_B$  is calculated as  $r_B = 1 - 6D^2/(n^2 - n)$ . With the above data we have

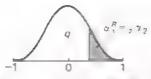
X ranks	1	51	7	2	3	4	54	8
Y ranks	2	5	7	1	3	4	6	8
rank differences	1	5	0	1	D	0	į	0

Thus  $D^2$  is  $2(1)^2 + 2(\frac{1}{2})^2 + 4(0)^2 = 2\frac{1}{2}$ , giving  $r_S = 1 - 6 \times 2\frac{1}{2}/(8^3 - 8) = 0.9702$ . The  $\alpha_1^R = \frac{1}{2}\%$  critical region for testing against the tendency for Y to increase with X is  $r_S \ge 0.8810$ , so there is virtually conclusive proof that this tendency is present. The general forms of the critical regions are the same as for r above

For Kendall's rank correlation coefficient, we compare each (X,Y) pair in turn with every other pair, if the pair with the smaller X-value also has the smaller Y-value, the pair is said to be concordant, but if it has the larger Y-value the pair is discordant if  $N_C$  and  $N_D$  are the total numbers of concordant and discordant pairs, Kendall's coefficient  $\tau$  is calculated as  $\tau = (N_C - N_D)/\frac{1}{2}n(n-1)$ , where in fact  $\frac{1}{2}n(n-1)$  is the total number of comparisons made. Any comparison in which the X-values and/or the Y-values are equal counts  $\frac{1}{2}$  to both  $N_C$  and  $N_D$ . Critical regions are of the same forms as with r and  $r_S$ . In the above example,  $N_C = 26\frac{1}{2}$ ,  $N_D = 1\frac{1}{2}$ , and  $\tau = (26\frac{1}{2} - 1\frac{1}{2})/28$ . 0.8929. This is again clearly significant of the tendency for Y to increase with X, since the  $\alpha_1^R = \frac{1}{2}X$  critical region is  $\tau \ge 0.7857$ .

Unitical regions for large n may be found using the facts that, under the null hypothesis,  $r, r_S$  and  $\tau$  have approximate normal distributions with zero means and standard deviations  $1/\sqrt{n-1}$  for both r and  $r_S$ , and  $\{2(2n+5)/9n(n-1)\}^{1/2}$  for  $\tau$ . For example the reader may check that with n=144 the approximate  $\alpha_2=5\%$  critical regions are  $|r| \ge 0.1639$ ,  $r_S \ge 0.1639$  and  $|\tau| \ge 0.1102$ .

### Critical values for the sample linear correlation coefficient r



q	0.95	0.975	0.99	0 995
$\sigma_1^R$	5%	2 5%	E 1% U	5%
a:	7 9	5%	2	1%
\$1				
- 1		_		
2	-	-	-	-
3	0 9877	0 9969	0 9995	0 9999
4	0 9000	0 9500	0 9800	0.9900
5	0 8054	0.8783	0.9343	0 9587
6	0 7293	0.8114	D B822	0 9172
7	0 6694	0.7545	0 8329	0.8745
8	0 6215	0.7067	0.7887	0.8343
9	0 5822	0 6564	0 7498	0.7977
10	0 5494	0.6319	0.7156	0 7646
31	0.5214	0 6021	0.6851	0 7348
12	0.4973	0.5760	0.6581	0.7079
13	0 4762	0.5529	0 6339	0.6835
14	0 4575	0.5324	06120	0 6614
15	0 4409	0.5140	0 5923	0.6411
16	0.4259	0.4973	0.5742	0 6226
17	0.4124	0 4821	0.5577	0 6055
18	0.4000	0 4683	0.5425	0.5897
19	0.3887	0 4555	0.5285	0.5751
20	0.3783	0.4438	0.6155	0 5614
21	0 3687	0 4 3 2 9	0 5034	0 5487
22	0 3599	0.4227	0.4921	0.5368
23	0.3515	0.4132	0.4815	0.5256
24	0 3438	0 4044	0 4716	0.5151
25	0 3365	D 3961	0 4622	0 5052
20	0 3297	0 3882	0.4534	0.4958
27	0 3233	D 3809	0.4451	0.4869
28	0.3172	0.3739	0.4372	0.4785
29	D 3115	0 3673	0 4297	0.4705
30	0.3061	0.3610	0.4226	0 4629

Q	1.45	0.975	2 99	0.995
$\alpha_t^R$	5%	2	1%	
ů.	0	5%	2	1%
27				
31 7	0.3009	0.3550	0.4158	0.4556
32	0.2960	0,3494	0.4093	0.4487
33	0.2913	0.3440	0.4032	0.4421
34 1	0 2869	0.3388	0.3972	0.415
35 4	0 2826	@ 333B	0.3916	0 4296
36 0	0 2785	D 3291	0.3862	0.4238
37	0.2746	0 3246	0.3810	0.4182
38 3	0.2709	0.3202	0.3760	0.4128
39 1	0.2673	0.3160	0.3712	0.40 6
40 (	0.2638	0.3120	0.3665	0 4026
41 5	0-2605	0.3081	0.3621	0.1 (18
42 1	0.2573	0.3044	0.3578	0 3932
43 (1	0.2542	0.3008	0.3536	0.3887
44 3	0.2512	0.2973	0.3496	0 384 1
45 /	0.2483	D 2940	0.3457	0.3864
46 1	0.2455	0 2907	0.3420	0.3763
47 5	0.2429	0.2876	0.3384	0 7721
46 /	0.7403	0.2845	0.3348	0 3683
49 5	0.2377	0 2816	0.3314	0.364
.60 d	0 2353	0.2787	0.3281	0.3610
TEP S	0 2329	0 2759	0 3249	0.3676
52 1	0.2306	0.2732	0.3218	0 3542
153 II	0.2284	0.2706	0.3188	0.3509
54 5	0.2262	0.2681	0.3158	0.3477
95 d	0.2241	0 2656	0.3129	0.3445
56 1	0.2221	0 2632	0.3102	0.3415
67 3	0.2201	0.2609	0.3074	0.1385
58 0	0.2181	0.2586	0.3048	0.3357
59 7	0.2162	0.2564	0 3022	0.3328
-00 1	0.2144	0.2542	0 2997	0-101

4	0.95	0.975	0.44	0 995
all.	5%	2 "	196 T	Б;
O)	O.	5%	- 2	1%
D				
61	0 2 26	0.2521	0 2972	0 3274
62	0.2108	0.2500	0 2948	D 3248
63	0 2091	0.2480	0 2925	0 3223
54	0.2075	0 2461	0 2902	0 3198
65	0 2058	0.2441	0.2880	0 3173
66	0 2042	0 2423	0.2858	0 3150
67	0.2027	0 2404	0.2832	0.3126
68	0 2017	0.2387	0 2816	0 3104
69	0 1997	0.2369	0 2796	0.3081
70	0 1982	0.2362	0.2776	0 3060
71	0 1968	0.2335	0.2756	0 3038
72	0 1354	0.2319	0.2737	0 30 7
73	0 1940	0.2303	0 2718	0 2997
74	0.4927	0 2287	0 2700	0 2977
75	0 1914	0.2272	0 2682	0 2957
76	0 1901	0.2257	0 2664	0 2938
77	0.1888	0 2242	0 2647	0 2919
78	0 1876	0 2227	0 2630	0.2900
79	0.1864	0.2213	0.2613	D 2882
80	0 1852	0.2199	0.2597	0 2864
87	0 1829	0.2172	0 2565	0 2830
84	0 1807	0.2146	0 2535	, 2796
66	3 1 786	0.2120	0.2505	0.2764
88	0 1765	0.2096	0 2477	0 2732
90	D 1745	0 2072	0 2449	0.2702
92	0 1726	0.2050	0 2422	0.2673
94	0 1707	0.2028	0 2396	0.2645
96	0 1589	0.2006	0.2371	0.2617
98	0 1671	0 1986	0 2347	0 2591
100	0 1654	0 1966	0.2324	0 2565

For description, see page 35.

### The Fisher z-transformation

$$z(r) = \frac{1}{2} \log_{e} \left( \frac{1+r}{1-r} \right) = 1.1513 \log_{10} \left( \frac{1+r}{1-r} \right)$$

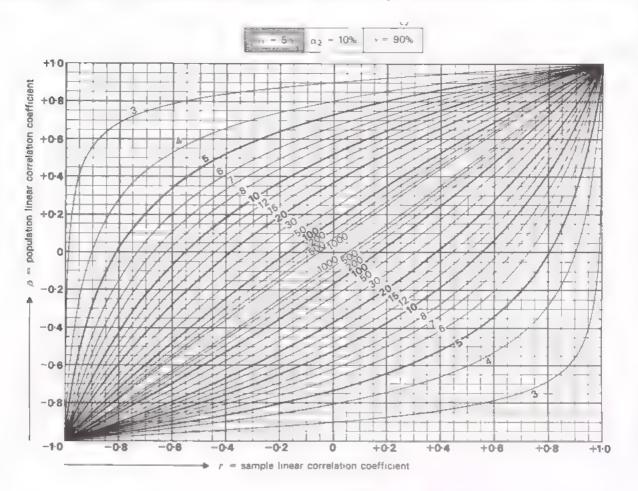
*	0	1	2	3	4	5	6	7		9
0.0	J etalji	9је.	, Ъ	0.0300	0.0400	.5X	16-F-1	,	; B /	51312
01	0 303	0 04	7 206	0.1307	0 1409	15 1	0-1614	1	C-820	0 923
02	0.2027	0.2132	0 2237	0.2342	0 2448	0.2664	0.2661	D . 764	0 2917	0.2486
0.3	0.3095	0 3205	0 37 6	0.3428	0.3541	0 3654	01(3	37 R4	0 4901	P418
0 4	0.4236	0 4356	0.4477	0 4599	0 4722	0 4847	0.4973	0.5101	0 5230	0 5361
0.5	0 5493	0.5627	0.5763	0.5901	0 6042	0.6184	0.6328	0.6475	0 6675	0.6777
0.6	0 6931	0 7089	0 7250	0.7414	0.7582	0.7753	0.7928	0.8107	0 8291	0.8480
6 1	0.8673	0.8872	0 9076	0 9287	0 9505	0 9730	0 9962	1.0203	1.0454	1.0714
0 80	1 0986	1 1014	1 1042	1.1070	1 1098	1 1127	1 1155	1.1184	1 1212	1 1241
0.81	1 270	1 1299	1 1329	1 1 358	1 1 188	1 4 7	1 04	â	150	1 1538
0.82	1 1569	1 1599	1 1630	1 1560	1 1692	1 1723	1 1754	1 1786	1 1817	1 1849
0.63	1 A81	3 914	1.1946	1979	12 11	2044	1.2	2 1	1.2144	1.2178
0.84	1 2212	1 2246	1 2280	1 2315	1 2349	1 2384	1.2419	1 2454	1 2490	1 2526
0 85	1 2562	1 2598	1 2634	1.2671	1 2707	1 2745	1 2 782	1 2819	1 2857	1 2895
Q 86	1.2933	1.2972	1.3011	1 3050	1 3089	1 3129	1 3169	1 3209	1 3249	3290
0.87	1 3331	1 3372	1.3414	1.3456	1 3496	1 3540	1.3583	1 3626	1 3670	1 3714
0 88	1 3758	1 3802	1 3847	1 3892	1 3938	1 3984	1 4030	1 4077	1 4124	1 4127
0 89	1 4219	1 4268	1 4316	1 4365	1 44 15	1 4465	1.4516	1 4566	1 4618	1 4670
0.90	1 4722	1 4775	1 4828	1 4882	1 4937	1 4992	1 5047	1.5103	1.5160	1 5217
0 91	1 5275	1 5334	1 5393	1 5453	1 5513	1.5574	1 5636	1 5698	1 5762	1 5826
0 92	1 5890	1 5956	1 6022	1 6009	1 6157	1 6226	1 6298	1 6366	1 6438	1.65 0
0.93	1 5584	1 6658	1 6734	1 6811	1 6888	1 6967	1.7047	1 7129	1.7211	1 7 2 9 5
0.94	1 7380	1 746	t 7555	1.764+	1 10	1 1828	* 7923	1 80 19	1 8 7 1 7	1 8216
0 95	1 8318	1 8421	1 8527	1 8635	1 8745	1 6857	1 8972	1 9090	1 9210	1 9333
0 96	1 9459	1 9588	1 9721	1 9857	1 9995	2 0139	2 0287	2 0439	2 0595	2 0756
0 97	2 0923	2 1095	2 1273	2 1457	2 1649	2 1847	2 2054	2 2269	2 2494	2 2729
0 98	2 2976	2 3235	2 3507	2 3 7 9 6	2 4101	2 4427	2 4774	2 5147	2 5550	2 5987
0.99	2 6467	2 6996	2 7587	2 8257	2 9031	2 9945	3 1063	3.2504	3.4534	3 8002

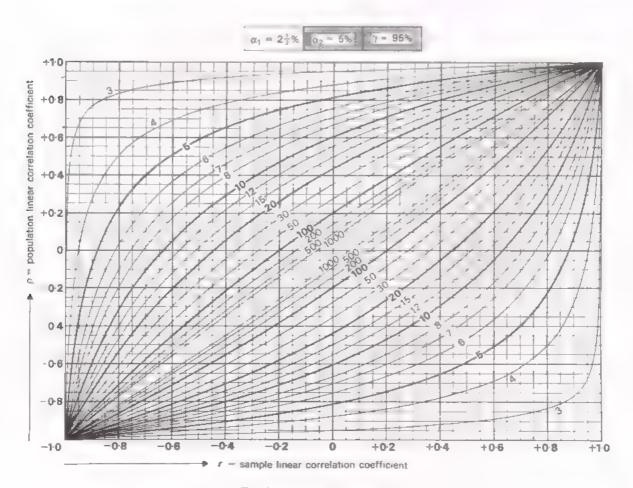
### The inverse of the Fisher z-transformation

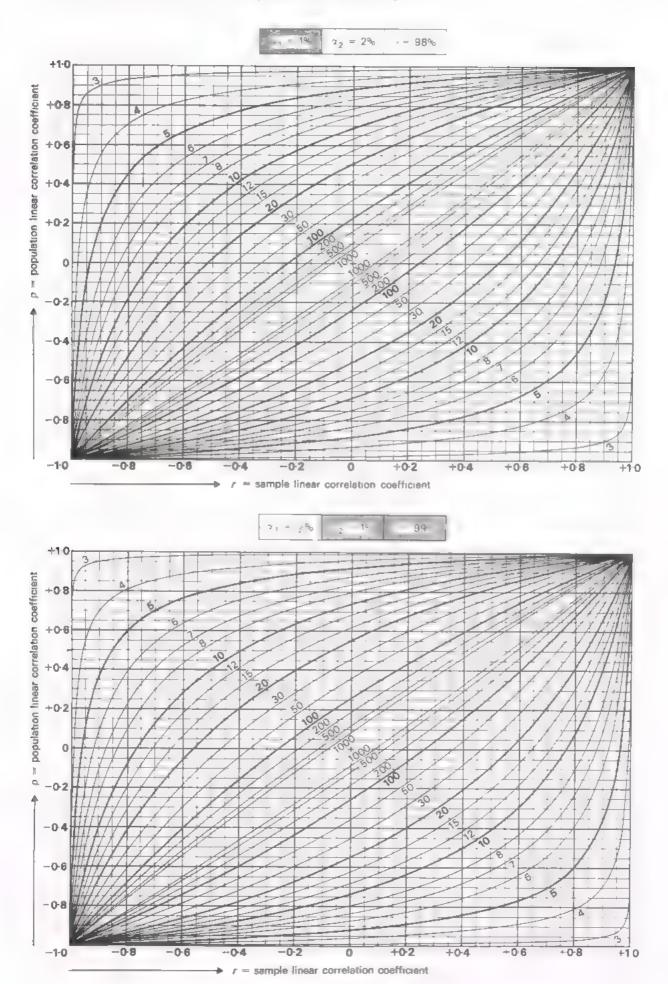
													P	HOPOR	ADD TION/		TS		
2	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	
0.0	0 0000	0100	0200	0300	0400						10	20	30	40	50	60	70	80	9
ı						0500	0599	0699	0798	0898	10	20	30	40	50	60	70	80	1
0 1	0.0997	1096	1194	1293	1391						10	20	30	39	49	59	69	79	-
02	0 1974	20.70	7166	2265	2200	1489	1586	1684	1781	1877	10	19	29	39	48	58	68	78	E
02	0 1974	2070	2165	2260	2355	2449	2543	2636	2729	2821	10	19	28	38	48	57	66	76	- 1
0.3	0.2913	3004	3095	3185	3275	2445	2 943	2030	2123	2621	9	18	28 27	37 36	46 45	56 54	65 63	74	1
						3364	3452	3540	3627	3714	9	17	26	35	44	52	61	70	
0.4	0 3799	3885	3969	4053	4136						8	1.7	25	34	42	50	59	67	
ļ						4219	4301	4382	4462	4542	8	16	24	32	40	48	56	64	
0.5	0.4621	4699	4777	4854	4930						8	15	23	31	38	46	54	61	
						5005	5080	5154	5227	5299	7	15	22	29	36	44	51	58	1
0.6	0 5370	5441	5511	5581	5649						7	14	21	28	35	42	49	56	1
						5717	57B4	5850	5915	5980	7	1.3	20	26	33	39	46	52	
0.7	0 6044	6107	6169	6231	6291						6	12	18	25	31	37	43	49	1
8.0	0 6640	6696	6751	5005	5050	6351	6411	6469	6527	6584	6	12	17	23	29	35	40	46	!
0.0	0 0040	0090	6751	6805	6858	6911	6963	7014	7004	25.14	5	11	16	22	27	33	38	43	-
0.9	0 7183	7211	7259	7306	7352	0311	0.300	7014	7064	7114	5	10	15	19	25 24	30 28	35 33	40 38	
		,		, 000	7 5 72	7398	7443	74B7	7531	7574	4	9	13	17	22	26	31	35	
10	0 7616	7658	7699	7739	7779							-	_			_			_
1	0,010	1440	1000	1130	7770	7818	7857	7895	7932	7969	4	B 7	12	16	20 19	24	28 26	32 30	
11	0 8005	8041	8076	8110	8144	7010	70.37	,023	,002	1303	3	7	10	14	17	21	24	28	
						8178	8210	8243	B275	8306	3	6	10	13	16	19	22	25	-
12	0.8337	B367	8397	B426	8455						3	6	9	12	15	18	20	23	-
						8483	8511	8538	8565	8591	3	5	В	11	13	16	19	21	-
1.3	0.8617	8643	8668	8692	8717						2	5	7	10	12	15	1.7	20	i
	Annes	DATE	Door			8741	8764	B787	8810	8832	2	5	7	9	t t	14	16	18	2
1.4	0 8854	B875	8896	8917	8937	0057	0077	0000	0015	0000	2	4	6	8	10	12	14	16	1
	0.0004	de ee		*		8957	8977	8996	9015	9033	2	4	6	8	9	11	13	15	
15	0.9051	9069	9087	9104	9121	0.00	A				2	3	5	7	9	10	12	14	1
1.6	0.9217	9232	9246	9261	9275	9138	9154	9170	9186	8201	2	3	5	6	8 7	9	11	13	
	D-0211	V C V C	32 40	3201	32/3	9789	9302	9316	9329	9341	1	3	4	5	6	9	10	12	1
17	0.9354	9366	9379	9391	9402		0000	50 0	2020	054	1	2	4	5	6	7	8	10	1
						9414	9425	9436	9447	9458	4	2	3	4	5	6	8	9	1
18	0 9468	9478	9488	9498	9508						1	2	3	4	5	6	7	8	
						9517	9527	9536	9545	9554	1	5	3	4	4	5	6	7	
19	0 9562	9571	9579	9587	9595						1	2	2	3	4	5	6	7	
						9603	9611	9618	9626	9633	1	Ŧ	2	3	4	4	5	6	
20	0 9640	9647	9654	9661	9667						7	1	2	3	3	4	5	5	
						9674	9680	9687	9693	9699	1	1	2	2	3	4	4	5	
21	0 9705	9710	9716	9721	9727	0700	0.700	02.0	02-0	nar é	1	1	2	2	3	3	4	4	
2 2	0 9757	9762	9767	9771	9776	9732	9737	9743	9748	9753	0	1	2	2	2	3	4	4	
	0 5/5/	3,02	8/0/	9771	9//0	9780	9785	9789	9793	9797	0	1	1	2	2	3	3	4	
23	0 9801	9805	9809	9812	9816	3780	3,03	2,02	3/53	0/27	0	1	1	2	2	2	3	3	
				74.6	00.0	9820	9823	9827	9830	9833	0	1	,	1	2	2	2	3	
24	0 9837	9840	9843	9846	9849						0	1	1	1	2	2	2	2	
						9852	9855	9858	9861	9863	0	1	1	1	1	2	2	2	
5	0 9866	9869	9871	9674	9876	9879	9881	9884	9886	9888	0	0	1	1	1	1	2	2	
26	0 9890	9892	9895	9697	9899	9901	9903	9905	9906	9908	0	۵	1	1	1	7	1	2	
2 7	0 9910	9912	9914	9915	9917	9919	9920	9922	9923	9925	0	0	0	1	1	1	1	1	
8 9	0 9926	9926	9929	9931	9932	9933	9935	9936	9937	9938	0	0	0	1	1	1	1	1	
2.9	0 9940	9941	9942	9943	9944	9945	9946	9947	9949	9950	0	0	0	0	1	1	1	1	
	0	1	2	3	4	5	6	7	8	9	-1	2	3	4	5	6	7	В	
														_					_

2	0	1 -	2	3	4		5	0	. 7	8	9
3.	0 995055	0 995949	0 996682	0 997283	0.997775		0 998178	0.998508	0 998778	0 999000	0.999181
4	0 999329	0.999451	0 999550	0 999632	0 999699		0 999753	0 999798	0.999835	0 999865	0 999889
5.	0 999909	0.999926	0 999939	0.999950	0.999959		0 999967	0 999973	0 999978	0 999982	0 999985
6.	0 999988	0 999990	0 999992	0 999993	0.999994		0 999995	0 999996	0 999997	0.999998	0.999998
7.	0 999998	0 999999	0 999999	0 999999	0 999999	1	0 999999	0 999999	1 000000	1 000000	1 0000000

### Charts giving confidence intervals for $\rho$ and critical values for r







For description, see page 35.

### Critical values for Spearman's rank correlation coefficient

$$r_S - 1 = \frac{6D^2}{n^3}$$

α <sup>R</sup>	57%	1	15	
9	1	5%		1%
73				
1				
2				
3				
4	1000			
5	0.9400	0000	9000	
6	0.8186	0 8857	0.9429	0/10/
7	0 1 43	1 357	0 8929	7 728r
8	0.6439	A T S	O B333	J 881;
9	0 6000	0 100	G 833	Q 9333
10	0 5636	0 6485	0 2455	0.7934
11	0 5364	Q = 82	0.1991	0 7546
12	0.5035	0.5874	6193	0 12 13
13	0 4R35	0.5804	0.6484	0 30 33
14	Q 463	G 5385	0 8 2 5 4	06791
15	C 4464	0.57*4	0.6036	1.8436
16	0.4294	0.50.29	0 5824	0.6.53
17	0 4 42	0 4877	0.5862	0 6 76
18	0404	0 47 6	1.5601	0 5006
19	0 19 2	0 4 >96	0.5351	0.6842
20	0 1805	ମ ଏଶ୍ୱନନ	0 52 B	r-5/99
21	032 1	0.4164	0.509	0.5864
22	0 7608	0 4752	13 4975	5418
23	Q 3528	9 4 60	0.4882	0.53-5
24	0 3443	0.4670	04767	0.5269
25	0 7 69	U-50-3	0.4662	. 5 58
26	0.3306	0.390	0.457	. 50GB
27	0.3242	( 3828	0.4487	04115
28	0.815	( 755	0.440	0.4836
29	D 31 B	C 3685	0.4325	0.4.40
30	0.3063	. 3624	0.4251	0.48

E. R.	5%	2 =	1%	4
0-	Q.	91.	2	1%
0				
31	0 3012	1 3560	0.4185	0.4593
32	0.2962	0 3504	0 4 1 ?	0.4523
33	0.2914	0 3449	0.4054	0 4455
34	u 2B71	0.3396	0 3996	0.4390
35	0.5858	0.3947	0 3936	0.4328
36	D 2 *88	0.3300	0.3882	0 4268
37	0.2148	0.3253	0.3829	0.4211
38	72 7	0 3209	03228	0.4155
39	0 2674	0 3168	0.3*29	0.4103
40	0 2640	0 31 28	0.3681	0.4051
41	0.2606	0.3087	0 36 36	0.4002
42	9 25 4	0 3951	0 3594	0 3966
4.3	0.2543	0.3014	n 3650	C-3908
44	0.2513	0.2018	0 3577	0.1864
45	0.2484	r 2945	0.3420	0.1822
46	1 2456	0.2913	0 3433	0.3751
47	1 2423	( 2880	0.3395	0 3 41
48	0 2403	C 2850	0.3461	93702
49	0.2378	0.2820	0.3-26	n 1664
50	2353	0.2791	0 3505	D 3628
5	0 2329	0.2764	3260	0.3542
52	0.2307	0.7 78	22P	, 35F.B
53	C-2*R4	0.2 10	0.2138	0 35.24
54	1 2262	0.2685	0.3168	0.3492
55	0.747	7.7659	6 34	0 346
56	322	0.44.36	D 14	1414
57	3 201	0.26.12	C 30 83	104.00
58	3.2 R*	2589		0 ( [
69	32 (2	( 286 "	0 → 0 3 0	0 434
60	9.2 44	0.2545	0.4065	9 314

aR.	5%	7	1%	u <sub>i</sub> ,
01	10%	5%	1.2	1%
n				
61	0.2126	0 2524	0.2980	0 328
62	0.2 08	0.2503	0.2956	0 326
63	0.2091	0.2483	0.2933	0 323
64	0.2075	0 2463	0.2910	0 120
65	D 205B	0 2444	0.2887	D 318
66	0.2042	0 2425	0.2965	0 316
67	0 20 27	0 2407	0 2844	033
68	0 2072	0.2389	0.2823	03 .
69	0 1997	0 2372	0.2802	0 309
70	0 1982	0 2354	0.2782	0.307
21	0 96B	0.2337	0.2762	0.304
72	0 1954	0 2321	0 2743	0 302
73	0.1946	0 2305	0 2724	0.300
74	0 1927	0.2289	0 2706	0.338
75	0.1914	0 2274	0 2688	0 296
76	901	0.2259	0 2670	0 294
77 :	0 1888	0.2244	0 2857	0 292
7B	0 1876	0.2229	0 2635	0 290
79 1	0 1864	0.22 5	0 2019	0.289
80	n 1852	0.2201	0.2602	0.287
82	0.3829	D 2174	0.7570	0.283
84	0 1807	0 2147	0.539	0.280
86	D > 7B5	D 2122	0.2510	0 277
86	0 765	0.2097	0.2481	0.274
90	0.1245	D 2074	0.2453	D 230
92	0 1 25	0.2051	0 2425	0.268
94	0 1 707	0.20.29	0.2400	0.265
96	0 1689	0.5006	0.2376	0.262
98	( 5 )	0.1987	0 235	0.259
100	0.1864	0 1967	0.2327	0.257

For description, see page 35.

### Critical values for Kendall's rank correlation coefficient

$$\tau = \frac{1}{2} \sum_{n=1}^{\infty} \frac{1}{2}$$

a <sup>ll</sup>	5%	7	1%	
œ	1€	5%	4	1%
n				
1				
2				
3				
4	0000			
5	J 8000	1 0000	1.0000	-
6	0 7333	0.8667	0 8667	1.0000
7	0.6190	D 7143	0 8095	0.9048
8	0.5714	0 6429	0.7143	0.7853
9	0 5000	0 5556	0.6667	r 22
10	0.466	0 4	0 6000	0.6444
11	0.4182	0.4909	0 5636	0 6000
12	D 3939	0.4546	0 5455	0 5758
13	0.3590	0.4359	0.5128	0.5641
14	0.3626	0.4066	0.4725	0.5165
15	0 3333	0 3905	D 4667	0 5048
18	. 3 67	0.3833	0.4333	0 4833
17	0 3088	0.3676	0 4265	0.4706
18	0.2941	0 3464	0.4118	0.4510
19	0 2865	0.3333	0.3918	€ 7.48€
20	0 2737	0.3263	0 3789	0.421
21	D 2667	0.3143	0.3714	0.4099
22	0 2641	0.3074	0.3593	6 3939
23	0 2569	0.2964	0 35 8	0.39.3
24	0 2464	0 2899	0 3406	0 3768
25	0.2400	0 2867	0 3333	0 366
26	0 2369	0 2800	0 3292	0 3600
27	0.2308	0 2707	0.3219	0 3561
<b>Z8</b>	0 2275	0 2646	0 3 22	0.3439
29	0 221 7	0 2611	0.3-03	0 3399
30	0.2184	0 2552	0 3011	0 3333

A.A.	5%		15.	
a		5%		1%
л				
31	. 23	1 24 .	- 294E	. 24
32		7 640	1 290 1	[ -36
33	1.45	C = 424	C 28 9	D 3 44
34	2 3	0.2	0.2.34	0 3119
35	1.Gesq-	0.2736	277	1.3043
36	. 3	0 2 12	0.2130	C-3C 16
37	200	0.2282	4 36 23	- 20 -1
38	202	0.223	5-26-32	- 29 F
39	D 77.	1,200	2+.05	0.29 4
40	436	7 21 79	2564	₹ 284€
61	805	5 21 85	D 25 7	0.2805
42	7	1 7 26	P 49	0.2 53
43	D 61	0.3063	0.2470	0.2735
44	C 34	C 20 2	1243	0.2685
45	0 7 7	0.2040	P 24 4	a 39k
46	0 1691	0.20 4	1.2 486	0.28.69
47	0 1674	G ogg	0.569	0.2599
48	0 1067	0 1368	0.2.53	0.25
49	6 1633	0.1956	0.2296	0.25. 8
50	0 1624	0 1918	0.22 R	U EKIE
51	0 1508	0.1906	0.2,51	[ 248¢
52	0 1584	0 1885	0 2.32	0.2489
53	0.1567	0 1872	0.7206	0.2438
54	0 1558	0 1862	0.2.8	C 25 1
55	0.1542	0 1825	0.2.62	0.239
56	0 619	0 1805	0.2141	0 2 3 64
57	0 *5 16	005	0.2.16	(2343
58	0 * 194	6-1-1	0.2099	0.23
59	0 44 29	0 - 160	0.2986	Γ 2297
50	0 1469	0 1740	0.2068	0.2282

64 0 16 65 0 16 66 0 16 67 0 16 68 1		P	1%
61 G12 C 63 C 65 C 65 C 66 C 67 C 68 C 69	154 0 172		
67 ( 63 ( 146 ( 14	154 0 172		
63 0 16 64 0 16 65 0 16 66 0 16 67 0 16 68 0 17		7 0 2044	0.2262
64 0 16 65 0 16 66 0 16 67 0 16 68 1	144 0 171	9 0 2025	0.2237
65 0 16 66 0 67 0 68 69	129 () 129	15 0 201 2	0 2227
66 ( 67 P 68 69 • 1	919 0168	7 0 994	0.2202
67 P 68 69 11	1 14 E 7	3 6 98	0.2183
68	194 C 65	5 0 963	0.2 68
69	389 0 04	2 0 949	0 2 AB
	10 163	FE 0 932	0.2 33
77	164 F.2	0 0 918	0 2 †4
	354 D F	0 1901	0 2099
71 r :	340 n 15.0	8 0 1887	0.3089
72 P 1	330 0 58	0 1878	0 2074
73	157	5 0 1865	0.2055
74	914 D 55	9 0 1847	0.2040
75 '	1 0 156	3 0 1 B 3 4	0 2029
76 6 2	991 0 53	7 D 1825	0.2014
77 1	285 0 53	0.1811	0.2003
76 7 2	775 0 51	5 0 1795	0 1988
79 0	269 F 50	9 01788	0 1970
80 013	159 0 150	O 0 1772	0 962
82 0 2	244 0 147	В 0 1749	0 1936
84 012	728 0 145	7 0 1727	0 1910
96 C12	212 0 144	2 0 710	0 885
58 01	96 0 42	6 0 1688	0 1865
90 0	86 0 140	6 01665	0 1845
92 0 11	71 0 1 39	0 0 1648	0 1820
94 0.11	\$5 0 37	5 0 631	0.1801
96 01	45 0 136	0 0 1614	0 1785
98 0 11	34 0 134	9 0 1597	0 1 765
100 0 11	19 0 133		

### upper action limit

### Control chart constants and conversion factors for estimating $\sigma$



er	W	A	W	10%	B2	21	d <sub>1</sub>	d <sub>3</sub>	$d_3$	c
2	2282	1 9365	, 6.93	2.8092	6 JO 6	4 24	1 284	2 000G	4 42	0 89, 2
3	0 6686	7 0541	0 179	2 1 766	0.0356	2 9916	1 6926	2 3391	1 9099	0.5908
4	0 4 760	0 7505	0.2888	1 9352	0.0369	25787	2 0588	2 SR03	2 2346	0.4857
5	0 3768	0 5942	0.3653	1 8045	0 586	7 357	2 3259	2 7669	2 4 744	0 4299
6	0 3157	0.4978	0 4206	1 7207	0.2110	2 2112	2 5344	29177	2 6535	0 3946
2	0.2739	0.4319	0 4624	1 6616	0 2556	2118	2 1044	3 D448	18 Bq	0 3698
8	0 24 34	0 3837	0 4952	1 6 73	0 2932	20457	2 8472	3 1541	2 9504	0.35 2
9	0.2200	0 3468	0.5218	1 5826	0 3251	1 9874	5 th 200	3 2444	3 0641	0 3367
10	0 2014	0 3 75	0 5438	1 5545	0 3524	1 9410	3 0 2 7 5	3 3352	3 640	0 3249
11	0 1863	0.2937	0 5624	1 5312	0 3761	1 3024	3 1729	34118	3.251	0.1152
12	0 1736	0 2738	0.5783	16.15	0 1969	1 8097	3 2585	3 4815	3 3.13 3	\$.3069
13	0 1629	0 2569	0.5922	4945	0.4.52	18417	3 3360	3 5452	3 406	0.2998
14	0.1538	0 2424	0.6044	1.4796	0.4 116	1.81.5	3 4068	3 50 39	3 4 728	0 2935
15	0 1458	0.2298	0.6153	1.4666	n 4453	1 795	3 4718	3 6584	3 5343	0.2880
16	0 1387	0 2 87	0.6250	1 4550	0.4596	1.7766	3 5320	3 7091	3 5913	0.2831
12	0 1325	0.2089	0.6338	1 4445	04"17	1 7592	3 5079	3 1565	16443	0.2787
18	0 1269	0.2001	0.6417	1 4351	0.4927	1 7437	3 6401	3 B01	3 6940	0 2747
19	0 1219	0 1922	0.6490	4265	0.4928	1 7295	3 6890	3 8430	3 7405	0.2711
20	0 1173	0 1850	0.6557	4 86	0.6022	1 7165	3 1350	3 8827	3 7844	0.2677

Control charts are designed to aid the regular periodic checking of production and other processes. The situation envisaged is that a quite small sample (the table caters for sample sizes n up to 20) is drawn and examined at regular intervals, and in particular the sample mean  $\bar{X}$  and the sample range R are recorded (the range is the largest value in the sample minus the smallest value). X and R are then plotted on separate control charts to monitor respectively the process average and variability.

The general form of a control chart is illustrated in the diagram. There is a central line representing the expected (i.e. average) value of the quantity  $(\overline{X} \text{ or } R)$  being plotted when the process is behaving normally (is in control). On either side of the central line are warning limits and action limits. These terms are virtually self-explanatory. The levels are such that if an observation falls outside the warning limits the user should be alerted to watch the subsequent behaviour of the process but should also realise that such observations are bound to occur by chance occasionally even when the process is in control. An observation may also fall outside the action limits when the process is in control, but the probability of this is very small and so a more positive alert would normally be signailed. Information can also be obtained by watching for possible trends and other such features on the charts

The central line and warning and action limits may be derived from studying pilot samples taken when the process is presumed or known to be in control, or alternatively may be fixed by a priori considerations If they are derived from pilot samples we shall assume that they are of the same size as those to be taken when the control scheme is in operation and that the mean R and range R are calculated for each such sample. These quantities are then averaged over all the pilot samples to obtain  $\overline{X}$  and  $\overline{R}$ . We may also calculate, instead of R, either the unadjusted or the adjusted sample standard deviations S or x (see below). The charts are then drawn up as follows

X-chart	Central line is $\widehat{X}$ , lower warning limit is $\widehat{\overline{X}} = W\widehat{R}$ , upper warning limit is $\widehat{\overline{X}} + W\widehat{R}$ ; lower action limit is $\widehat{\overline{X}} - A\widehat{R}$ ; upper action limit is $\widehat{\overline{X}} + A\widehat{R}$ .
R chart	Central line is $\widehat{R}_i$ lower warning limit is $w_1\widehat{R}_i$ upper warning limit is $w_2\widehat{R}_i$ lower action limit is $a_1\widehat{R}_i$ upper action limit is $a_2\widehat{R}_i$

As an alternative to using pilot samples, specifications of the mean  $\mu$  and/or the standard deviation  $\sigma$  of the process measurements may be used to define the 'in control' situation. If  $\mu$  is given, use it in place of X in drawing up the X-chart. If  $\sigma$  is given, the expected value of R is equal to  $d_1\sigma$ , so here define  $\bar{R}$  as  $d_1\sigma$  and then proceed as above This application allows an exact interpretation to be made of the warning and action limits, for if the process measurements are normally distributed with mean  $\mu$  and standard deviation of the warning limits thus obtained correspond

to quantiles q of 0.025 and 0.975 and the action limits to quantiles of 0.001 and 0.999. In other words, the limits can be regarded as critical values for testing the null hypothesis that the data are indeed from a normal distribution with mean  $\mu$  and standard deviation  $\sigma$ , the warning limits corresponding to significance levels of  $\alpha_1 = 2\frac{1}{2}\%$ or  $\alpha_2 = 5\%$  and the action limits to levels of  $\alpha_1 = 0.1\%$  or  $\alpha_3 = 0.2\%$ 

If pilot samples are used it may be that the variability of the process has been measured by recording the sample standard deviations rather than ranges. If the unadjusted sample standard deviation  $S = \{\Sigma(X - \bar{X})^2/n\}^{1/2}$  has been calculated for each pilot sample, average the values of S to obtain S, and then define  $R = d_2 S$  and proceed as above. Or, if adjusted sample standard deviations  $s = \{\Sigma (X - \overline{X})^2 /   $(n-1)^{1/2}$  have been calculated, multiply their average  $\bar{s}$  by  $d_3$  to obtain  $R = d_3 \hat{s}$ , and again proceed as above. It should be understood that in general these formulae for R will not give exactly the same value as if R were calculated directly from the pilot samples, but represent the expected value of  $\overline{R}$  given the information available

For convenience we have also included in this table a column of constants c for forming unbiased estimators of the standard deviation o from either the range of a single sample or the average range of more than one sample of the same size. Denoting by  $\bar{R}$  the range or average range,  $\sigma$  is estimated by cR  $\sigma$  may also be estimated from S or  $\tilde{s}$  by  $cd_2\tilde{S}$  or  $cd_3\tilde{s}$  respectively

EXAMPLES: If samples are of size n = 10, and pilot samples have average value of the sample means X=15.00and average range R=700, then the X-chart has central line at 15 00, warning limits at 15 00 ± 0.2014 × 7.00, i.e. 13.59 and 16.41, and action limits at  $15.00 \pm 0.3175 \times$ 7 00, i.e. 12 78 and 17.22, the R-chart has central line at 7.00, warning limits at 0.5438  $\times$  7.00 = 3.81 and 1.5545  $\times$ 7 00 = 10 88, and action limits at 0.3524 x 7 00 = 2 47 and  $1.9410 \times 7.00 = 13.59$ . The standard deviation  $\sigma$  may be estimated from the pilot samples as  $c\bar{R} = 0.3249 \times$ 7.00 - 2.27

Alternatively, if the unadjusted sample standard deviations S had been computed instead of ranges, and the average value S of the S-values were S = 2.00, we would define  $R = d_2 S = 3.3352 \times 2.00 = 6.670$ . The reader may confirm that the X-chart would then have central line 15.00, warning limits 13.66 and 16.34, and action limits 12.88 and 17.12; and the R-chart would have central line 6.670, warning limits 3.63 and 10.37, and action limits 2.35 and 12.95. The standard deviation σ could be estimated as  $cd_2S = 0.3249 \times 6.670 = 2.17$ 

Finally if the 'in control' situation is defined by a mean value  $\mu = 14.0$  and standard deviation  $\sigma = 2.5$ , we define  $\overline{R} = d_1 \sigma = 3.0775 \times 2.5 = 7.694$ , and then obtain an  $\overline{X}$ chart with central line 14.0, warning limits 12.45 and 15.55, and action limits 11.56 and 16.44, and the R-chart would have central line 7.694, warning limits 4 18 and 11 96, and action limits 2.71 and 14.93

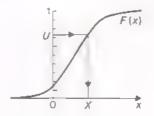
### Random digits

2006   1988   1989   1988   1989   1988   1989																				
\$19.00   \$	02484	88139	31788	35873	63259	99886	20644	41853	41915	02944	82414	59559	41440	22668	37R41	70679	82723	60128	30374	90243
1975   1975	83580	56131	12238	68291	95093	07362	74354	13071	77901											
Decay   Control   Contro	37336	63266																		
APPRING   20785   24119   62724   38717   20886   56506   32000   10007   68272   38886   36504   40475   55506   55507   55686   32500   24707   57070   57070   30190   57070   57070   57070   57070   30190   57070   57	02010	DIOIS	40047	78302	74770	71709	00004	043U4	48801	17115	85281	33517	20576	23195	12081	45048	01285	80874	00702	74771
\$1,000   \$	96417	63336	88491	73259	21086	51932	32304	45021	61697	73953	89168	81340	50382	30286	84550	59488	95424	31734	02673	45586
2009   2009	42293	29755	24119	62125	33717	20284	55606	33308	51007	58272	39426	52113	93433	45546	68180	72212	84593	85572	80863	65594
2009   2009	31378	35714	00941	53042	99174	30596	67769	59343	53193	19203	31228	18442	47214	53414	97924	05540	64402	B6719	57304	53443
	27098	38959	49721	69341	40475	55998	87510													
	86527	73898	66912	76300	52782															
1879   1886   1870	04004		400-4		***															
1988   66460   27901   37388   04890   58947   57957   27967																				
1998   2892   51891   04997   98909   98904   51893   28998   28998   28908   28905   24149   48144   48514   48514   68504   04476   0321   28929   37709   28804   14805   14805   24145   14805   24145   28904   28905   24145   24145							76229		64236	74782	91613		63858	50229	04979	79377	65502	43457	49356	88489
1902   1907   1918					04806	31140	75253	79692	47618	20024	16022	270B1	00058	97199	68594	35853	17062	89925	25742	27742
\$\ \begin{align***   \$\ \text{\$4228} \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	10346	28822	51891	04097	98009	58042	67833	23539	37668	16324	97243	03199	45435	45355	24374	84490	83041	03381	74618	90176
ABSSE   28915   51327   04396   338413   41392   27843   09074   88985   28960   64486   63206   24787   13287   24983   30506   69144   24983   24983   69827   24983   69827   24983   249	20582	49576	91822	63807	99450	18240	70002	75386	26035	21459	74543	48514	68504	04476	80747	64071	03321	29629	37709	73893
ABSSE   28915   51327   04396   338413   41392   27843   09074   88985   28960   64486   63206   24787   13287   24983   30506   69144   24983   24983   69827   24983   69827   24983   249	12023	R2328	54B10	64766	58954	76201	78456	98467	34166	94186	00060	67514	19200	28021	82572	09876	74070	20202	49402	62704
94786 09401 98896 18896 18896 18896 59896 9897 9897 9897 9897 9897 9898 9898																				
\$1,000   \$																				
2008   0311   9937   68176   89100   2237   95420   89974   36036   21781   51986   12077   46250   07925   64333   34783   57776   68352   54531   S0358   22000   43401   40028   69122   07023   58168   69107   27426   19982   79706   59168   41720   41710   4777   86838   36777   7947   2777   2626   68688   77930   65968   41720   4172																				
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62321 72533 23418 06305 41547 40150 55300 23898 34891 85908 47040 67528 12476 16409 74959 1290 23735 78506 66269 74396 1294 2376 39056 42285 87925 71241 48538 16124 12541 81160 67526 76569 11863 56920 36872 84068 23931 03132 98260 40881 36400 20855 61505 43434 77662 50397 04107 48089 33570 43315 01145 01259 41841 14027 91281 73123 73934 25643 73719 12961 91118 51220 32750 85161 17942 09500 82183 70192 61318 76271 50734 88656 55193 92580 17878 87299 96120 66977 74568 21205 25466 97080 43938 06211 31215 83322 27999 50758 76499 08955 97396 68137 36721 50734 88656 55193 92580 17878 87299 96120 66977 74568 21205 25466 97080 43938 06211 31215 83322 27999 50758 76499 08955 97396 68137 36721 50734 88656 55193 92580 17878 87299 96120 66977 74568 21205 25466 97080 43938 06211 31215 83322 40815 50731 92877 46395 86922 92330 33398 78280 33835 32614 81082 84756 01914 32559 27149 39812 24643 49913 43380 88439 91002 10859 25440 26259 40889 91541 78688 17601 76567 11357 01088 52233 21106 73798 90342 07773 42685 04186 61471 47687 20726 03784 41838 17267 04927 26719 30540 22557 33603 75689 04266 61592 18588 59135 95029 46711 01496 49891 22452 81489 62136 88038 78897 37132 44841 85577 07205 03169 19347 17449 86832 46996 84847 16684 15187 33558 2605 83358 15947 51285 01560 88038 79897 37132 44841 85577 07205 03169 19347 17449 86832 46996 84847 16684 15187 33558 2605 83358 15947 51285 01560 9734 12623 20526 27902 28596 69351 73214 67959 48726 68207 29811 11127 81957 79526 66240 35007 68602 32703 16099 46252 18740 00104 87152 34571 74436 85382 63736 47803 65176 20206 25929 51398 80379 75345 50304 60320 31904 78104 00104 87152 34571 74436 85085 45950 9385 40642 01960 26228 18932 04214 61808 9289 24707 22758 18685 63985 1350 95778 69866 72803 98001 74976 88751 93890 93842 97775 89100 00845 06364 31922 8829 02738 39651 88745 68071 11350 33668 51764 44213 16416 93085 9500 96409 98428 99776 77725 89100 00845 06364 31922 8829 02738 39651 88745 68071 11350 33668 51764 44213 16416 93085 9500 96409 98428 99776 77725 89100 00845 06364 31922 8	04771	44497	61709	82465	56798	01632	83576	87547	13795	07104	05742	03616	94098	38561	09721	38603	44622	86735	29208	88356
06318 89 38 46129 47950 73947 87945 81956 06171 30239 77245 49200 67528 12478 16409 74959 12940 23735 78506 86269 74396   23176 39056 42285 87925 71241 48538 16124 13541 81160 95266 76569 11863 56920 36872 84068 23931 03132 98260 40881 36400   20855 61505 43434 77662 50397 04107 48089 33570 43315 01145 01259 41841 14027 91281 73123 73934 25643 73719 12961 81118   51220 32750 85161 17942 09500 82183 70192 61318 76271 83729 96120 69977 74568 21205 25466 97080 43938 06211 31215 83322   27999 50758 76499 08955 97396 68137 35721 50734 88856 56193 92580 17878 87290 87002 49445 09798 53583 18839 24688 27439   02835 40215 61818 64739 13109 61681 00418 26909 90229 36990 258028 20871 78561 81186 64762 90417 68072 39107 48467 74371   40963 38806 82384 00231 83815 30316 40698 38553 30566 62249 93172 84566 89662 28712 91300 53308 14138 07032 38650 22841   50731 92877 46395 86622 92330 33398 78200 33835 32614 81082 84756 01914 32359 27149 39812 24643 49913 43380 88439 19102   10959 25440 26269 40889 91641 78886 17601 76567 11357 01088 52233 21106 73788 90942 07778 42685 04186 61471 47687 20726   03784 41838 17267 04927 26719 30540 22567 33603 75889 04266 61592 18588 59135 95029 46711 01496 49991 22452 81488 62136   86038 78897 37132 44887 85577 07205 03919 19347 17449 86882 46996 84847 15664 15187 33558 25*05 3358 15947 12285 01570   797916 32882 97441 26397 27173 46059 52260 76989 14728 68207 29811 11127 81957 79526 66240 35007 86520 23703 18099 48252 72451 18449 04444 30225 86543 30362 47162 45784 29045 26513 76680 75923 79273 43584 96519 86541 10838 10778 08017 82954 12652 32604 16765 59406 10177 27227 47841 74898 66382 63766 75923 79273 43584 69619 86541 10838 10778 08017 82954 12652 32604 14784 67953 63386 6638 66386 66386 75920 24509 69351 73046 63050 31904 60300 31904 60	75612	51553	02595	24676	49317	00084	58196	40422	30294	90874	89516	10014	13424	06670	91354	02759	27300	80870	13923	94134
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20655 61505 43434 77662 50397	06318	89 38	46129	47950	73947	87945	81956	06171	30239	77245	49200	67528	12476	16409	74959	12940	23735	78506	86269	74396
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10959 25440 26269 40889 91641 78868 17601 76567 11357 01088 52233 21106 73798 90942 07778 42685 04186 61471 47687 20726 03784 41838 17267 04927 26719 30540 22557 33603 75689 04266 61592 18588 59135 95029 46711 01496 49891 22452 81489 62136 80949 08395 58909 64448 04738 07373 00130 08352 75058 58561 77656 67493 82480 03507 34742 82955 31274 17994 46276 01606 86038 76897 37132 44871 85577 07205 03919 19347 17449 86832 46996 84847 15664 15187 33558 26105 83358 15947 51285 01570 97916 32882 97441 26397 27173 46059 52260 76989 14728 68207 29811 11127 81957 79526 56240 35007 86520 23703 16099 46252 72451 18449 04444 30225 86543 30362 47162 45784 29045 26513 76680 75923 79273 43584 96519 86541 10836 10778 08017 82954 12623 20526 27902 28596 69351 73214 67953 43725 71702 07781 99830 83847 18818 94296 60973 57960 91843 86460 93289 36638 13305 23464 16745 99406 10177 27227 47841 74838 65382 63736 47603 65176 20206 25929 51398 80379 75345 50304 60320 31904 78104 00194 87152 34571 74435 35395 18567 65386 93855 40642 01960 26232 18632 04214 61808 92899 24707 22758 18685 56996 13693 59272 95778 69866 72803 98001 74976 28751 52090 22903 79050 55048 73203 95178 30158 52641 46841 20270 39583 50958 47874 68071 11360 33669 51764 44213 16415 93085 95030 96409 98428 99776 77725 89102 00845 06364 31922 88229 02738 39651 88745	40953	38806	82384	00231	83815	30315	40698	38553	30566	62249	93172	84566	89662	26712	91300	5330A	14138	07032	38650	22841
10959 25440 26269 40889 91641 78868 17601 76567 11357 01088 52233 21106 73798 90942 07779 42685 04186 61471 47687 20726 03784 41838 17267 04927 26719 30540 22557 33603 75889 04266 61592 18588 59135 95029 46711 01498 49891 22452 81489 62136 80949 08395 58909 64448 04738 07373 00130 08352 75058 58561 77656 67493 82480 03507 34742 82955 31274 17994 46276 01606 86038 76897 37132 44871 85577 07205 03919 19347 17449 86832 46996 84847 15664 15187 33558 26105 83358 15947 51285 01570 97916 32882 97441 26397 27173 46059 52260 76989 14728 68207 29811 11127 81957 79526 56240 35007 86520 23703 16099 46252 72451 18449 04444 30225 86543 30362 47162 45784 29045 26513 76680 75923 79273 43584 96519 86541 10836 10778 08017 82954 12623 20526 27902 28596 69351 73214 67953 43725 71702 07781 99830 83847 18818 94296 60973 57960 91843 86460 93289 36638 13305 23464 16745 59406 10177 27227 47841 74838 65382 63736 47603 65176 20206 25929 51398 80379 75345 50304 60320 31904 78104 00194 87152 34571 74435 35395 18567 65386 93855 40642 01960 26232 18932 04214 61808 92899 24707 22758 18685 56996 13693 59272 95778 69866 72803 98001 74976 28751 52090 22903 79050 55048 73203 95178 30158 52641 46841 20270 39583 50958 47874 68071 11360 33669 51764 44213 16415 93085 95030 96409 98428 99776 77725 89102 00845 06364 31922 88229 02738 39651 88745	50731	92877	46395	86922	92330	33398	78200	33835	32614	81082	84756	01914	32359	27149	39B12	24643	49913	43380	88439	19102
03784 41838 17267 04927 26719 30540 22567 33603 75689 04266 61592 18588 50135 95029 46711 01498 49891 22452 81489 62136 80949 08395 58909 64448 04738 07373 00130 08352 75058 58561 77656 67493 82480 03607 34742 82055 31274 17994 46276 01606 86038 76897 37132 44871 85577 07205 03919 19347 17449 86832 46996 84847 15684 15187 33558 26105 83358 15947 51285 01570 97916 32882 97441 26397 27173 46059 52260 76989 14728 68207 29811 11127 81957 79526 56240 35007 86620 23703 16099 46252 72451 18449 04444 30225 86543 30362 47162 45784 29045 26513 76680 75923 79273 43584 96519 86541 10836 10778 08017 82954 12623 20526 27902 28596 69351 73214 67953 43725 71702 07781 99830 83847 18818 94296 60973 57960 91843 86460 93269 36536 13305 23464 16745 59406 10177 27227 47841 74838 65382 63736 47603 65176 20206 25929 51398 80379 75345 50304 60320 31904 78104 00194 87152 34571 74435 35395 18567 65386 93855 40642 01960 26232 18632 04214 61808 92899 24707 22758 18688 56996 13693 59272 95778 69866 72803 98001 74976 28751 52090 22903 79050 55048 73203 95178 30158 52641 46841 20270 39583 50958 42926 75661 41312 82548 92060 17676 64499 68650 45971 98490 68982 38487 88558 03466 15752 38590 13687 63909 32355 47874 68071 11360 33669 51764 44213 16415 93085 95030 96409 98428 99776 77725 89102 00845 06364 31922 88229 02738 39651 88745	10959	25440	26269	408B9	91641	78868	17601	76567	11357	01088							04186	61471		20726
80949 08395 58909 08448 04738 07373 00130 08352 75058 58561 77656 67493 82480 03507 34742 82955 31274 17994 46276 01606 86038 78897 37132 44871 85577 07205 03919 19347 17449 86832 46996 84847 15684 15187 33558 26105 83358 15947 51285 01570 97916 32882 97441 26397 27173 46059 52260 76989 14728 68207 29811 11127 81957 79526 56240 35007 86620 23703 16099 46252 72451 18449 04444 30225 86543 30362 47162 45784 29045 28513 76680 75923 79273 43584 96519 86541 10836 10778 08017 82954 12623 20526 27902 28596 69351 73214 67953 43725 71702 07781 99830 83847 18818 94296 60973 57960 91843 86460 93289 35638 13305 23464 16745 59406 10177 27227 47841 74838 65382 63736 47603 65176 20206 25929 51398 80379 75345 50304 60320 31904 78104 00194 87152 34571 74435 35395 18567 65386 93955 40642 01960 26232 19632 04214 61808 92899 24707 22758 18685 56996 13693 59272 95778 69866 72803 98001 74976 28751 52090 22903 79050 56048 73203 95178 30158 52641 46841 20270 39583 50958 42926 75661 41312 82548 92060 17676 64499 68650 45971 98490 68982 38487 88558 03466 15752 38590 13687 63909 32355 47874 68071 11360 33669 51764 44213 16415 93085 95030 96409 98428 99776 77725 89102 00845 06364 31922 88229 02738 39651 88745	03784																			
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13305 23464 16745 59406 10177 27227 47841 74838 65382 63736 47603 65176 20206 25929 51398 80379 75345 50304 60320 31904  78104 00194 87152 34571 74435 35395 18567 65386 93855 40642 01960 26232 18632 04214 61808 92899 24707 22758 18685 56996 13693 69272 95778 69866 72803 98001 74976 28751 52090 22903 79050 55048 73203 95178 30158 52641 46841 20270 39583 50958 42926 75661 41312 82546 92060 17676 54499 68650 45971 98490 68982 38487 88558 03466 15752 38590 13687 63909 32355 47874 68071 11350 33669 51764 44213 16415 93085 95030 96409 98428 99776 77725 89102 00845 06364 31922 88229 02738 39651 88745																86541	10836	10778	08017	82954
78104 00194 87152 34571 74435 35395 18567 65386 93855 40642 01960 26232 18632 04214 61808 92899 24707 22758 18685 56996 13693 69272 85778 69866 72803 98001 74976 28751 52090 22903 79050 55048 73203 95178 30158 52641 46841 20270 38583 50958 42926 75661 41312 82548 92060 17676 64499 68650 45971 98490 68982 38487 88558 03466 15752 38590 13687 63809 32355 47874 68071 11350 33669 51764 44213 16415 93085 85030 96409 98428 99776 77725 89102 00845 06364 31922 88229 02738 39651 88745																57960	91843	86460	93269	35636
13693     69272     95778     69866     72803     98001     74976     28751     52090     22903     79050     56048     73203     95178     30158     52641     46841     20270     39583     50958       42926     75661     41312     82546     92060     17676     64499     68650     45971     98490     68982     38487     88558     03466     15752     38590     13687     63909     32355     47874       68071     11360     33669     51764     44213     16415     93085     95030     96409     98428     99776     77725     89102     00845     06364     31922     88229     02738     39651     88745	13305	23464	16745	59406	10177	27227	47841	74838	65382	63736	47603	65176	20206	25929	51398	80379	75345	50304	60320	31904
13693     69272     95778     69866     72803     98001     74976     28751     52090     22903     79050     56048     73203     95178     30158     52641     46841     20270     39583     50958       42926     75661     41312     82546     92060     17676     64499     68650     45971     98490     68982     38487     88558     03466     15752     38590     13687     63909     32355     47874       68071     11360     33669     51764     44213     16415     93085     95030     96409     98428     99776     77725     89102     00845     06364     31922     88229     02738     39651     88745	78104	00194	87152	34571	74435	35395	18567	65386	93855	40642	01960	26232	19832	04214	61808	92890	24707	22759	18685	5600s
42926 75661 41312 82546 92060 17676 64499 68650 45971 98490 68982 38487 88558 03466 15752 38590 13687 63909 32355 47874 68071 11360 33669 51764 44213 16415 93085 95030 96409 98428 99776 77725 89102 00845 06364 31922 88229 02738 39651 68745																				
68071 11350 33669 51764 44213 16415 93085 95030 96409 98428 99776 77725 89102 00845 06364 31922 88229 02738 39651 68745					1															
19005 11910 51.00 Annes Annes 10101 50000 X1105 40000 3000 32010 32/12 80020 32000 31100 32/23 10433 83022 31898 72444																				
	19002	77070	37.08	00053	40004	1/018	20200	21752	43454	19383	22010	33/12	90370	35023	31100	32231	75933	93022	31898	12444

Fach digit in the table was generated by a process equally likely to give any one of the ten digits 0, 1, 2, ..., 9. The digits have been grouped purely for convenience of reading

Random digits can be used to simulate random samples from any probability distribution. First note that random numbers U from the continuous uniform distribution on  $(0\cdot1)$  can be formed approximately by placing a decimal point in front of groups of, say, five random digits (again for ease of reading), thus: 0.02484, 0.88139, 0.31788, etc. These numbers may in turn be transformed to random numbers X from any continuous distribution with c.d.f. F(x) by solving the equation U = F(X) for X in terms of U — this may be accomplished using a graph of F(x) as

shown in the diagram. Random numbers from discrete distributions may be obtained by a similar graphical process or by finding the smallest X such that  $F(X) \ge U$ .



### Random numbers from normal distributions

0.5117	- 0 6501	0,0240	0.0374	0.4650	0.6573	- 0.8489	1.6237	0.9161	0.4286	2.1530	0.8024	0.6296	- 0 7431	0.2311
0.4219	0 1946	- 0.2223	0.8529	0.3829	1,3436	1.4955	0,5792	-1.1305	-0.3346	1 9110	1.4270	-1 7715	0.6190	1,3728
0.3968	-2.0135	0.3052	1.4541	0.3063	0.0446	-2.1887	0.2511	0.9978	0.4531	-0.8269	-1 1302	-0.2418	0 1 748	-0.2623
0 4687	1.4781	-1 7345	0.7693	-0.9250	0.0144	0.7538	0.0476	- 0 6648	1.0353	- 1.9236	0.0390	1.7233	- 0.3012	1.2579
0.6958	0.9457	- 2.2365	0.2212	- 0.0329	1.3567	-1.0202	-0.6191	-1.5205	-2.4005	0.0528	- D 9080	- 0.6263	0.6274	-0.1816
0 3644	1.5510	-0.4803	-1,0094	0.4757	0.9914	0.5532	0.7414	0.6996	0.4086	-0.7131	0,5659	0.5726	-1,0370	0.6656
0 9069	-0.3967	0.6256	D.7654	0.6252	2 1284	1.2576	0.8842	0.3930	0.2474	- 0.4700	0.5366	- 0.7211	0.4170	0.0039
1 1476	-0.2261	-0.4645	0.3763	- 1.5602	0.8831	1 4995	- 0.5930	0.9010	0.5486	0.8076	0.0739	1.8341	0.6792	- 0.2652
0.6157	1 1829	-1.0711	-0.6905	0.2236	- 0.4170	0.6114	0.0493	1,3242	1.0989	-1.3245	-0.0253	0.3983	1,7539	0.7943
0.0140	0 3773	1 0443	0.3281	0.1657	0.5163	0 0572	1 7496	0 6925	0.9631	2 6 7 4 6	0 1739	0.2046	1 3770	2 5394
0.6567	0.4607	- 0 1899	1.4323	1.6818	-0.9194	- 0.0812	-0.0136	0.5099	0.4718	0.4880	- 1 2776	D 5492	- 0 7707	0.2670
1.2269	2.4441	-2.5492	-0.7248	~ 1.5706	-0.3898	-0.6462	1.5392	0.4541	- 0.2495	- 0,5361	-1.2611	0 1790	0.7144	-0.3908
- 2.0647	-0.1562	-0.2500	1.2900	1.1793	0.4379	-0.5050	-0.8679	- 0.2687	1,0452	0.5523	1.2387	- 1.8821	1.0840	0.8673
0.2633	1.0436	0,3264	0.1131	- 1.9656	0.2444	-0.4575	0.1475	-0.9912	- 0.0698	1.4027	-1.4261	-1.3690	1,1719	0.6424
0 1638	-0,2625	- 0.4261	0.1458	0.1283	-0.0728	1.0004	0.2144	1.7433	0.4577	- 0 7605	-0.8476	- 1 1592	3.0920	0.8802
0 0288	0 0438	0 1742	0.9610	0.3768	0 1367	0.0709	0.7607	1 2500	0.5741	1.6103	0 1116	0.3716	1 3832	0.8992
- 1.8426	-0.3121	-1.0415	0.5305	-0.9029	0 9628	-0.3619	-0.9187	0.2634	- 0.0089	-0.3599	0.8698	1.2590	- 1.2478	-0,8828
-0.7422	-0.5728	0.6748	1.9620	-0.0364	0,3374	0.6351	1.7987	-0.0415	0.9141	0.7215	~ 0.6227	1 1671	- 1.0297	0.5019
- 0.8158	1.6473	-2,0660	-0.5147	0 5564	- 1.0821	-17388	0.0251	-1.3612	-2.2882	0.3054	-1.2463	1,3680	0.1380	1.6723
1.2816	0.4435	0.3760	- 0.6307	0 9982	1,9797	- 0.1486	0.5829	1.7779	0.8335	- 0.4614	0.7387	- 0.9224	1.4158	0 4807
0.3257	1.6609	1.5465	1.8711	0.4291	-0.4098	- 0.9554	0 5928	0.6828	2.8234	0.7119	0.2466	- 0.2270	- 0 9025	0 1486
- 0.5662	0,2938	-1.0305	0.4343	2,1240	1.5033	-0.5762	1.0687	- 0 0615	-1.4243	0.9548	1.2092	-0.1559	0.B749	-01916
-0.7432	0.6906	- 1.9848	-0.2062	1.5273	1.1176	-0.4626	-1.7566	- 0.2784	0.3495	- 0.4353	-25354	- 1.8229	1 2539	0 5565
0.0799	0 8198	1 2491	0 4998	0.0589	0 6848	0 9974	0.8797	0.0676	1 0889	0.5973	3 1585	0.4271	0 6168	2 1738
0.7719	1 2595	0 1923	1 8775	1 2376	0 4795	0 6284	0.0667	0.5308	0 2933	0 7285	1 6920	1 7669	0 5144	0 5109

These random numbers are from the standard normal distribution, i.e. the normal distribution with mean 0 and standard deviation 1. They may be transformed to random numbers from any other normal distribution with mean  $\mu$  and standard deviation  $\sigma$  by multiplying them by  $\sigma$  and

adding  $\mu$ . For example to obtain a sample from the normal distribution with mean  $\mu=10$  and standard deviation  $\sigma=2$  double the numbers and add 10, thus  $2\times(0.5117)+10=11.0234, 2\times(-0.6501)+10=8.6998, 2\times(-0.0240)+10=9.9520, etc$ 

### Random numbers from exponential distributions

0 6193	1 8350	0 2285	1 5106	0 5024	2 3326	4 7123	0 9869	0 7543	0 1759	2 3678	0 1260	1 5913	0 1730	0.5110
0 0354	1 4300	1 6249	0 1402	0 8824	0 9866	0 2289	0.1741	1 3838	0.3772	1 5610	0 1928	0 6389	0 1052	0 468
0.1258	0.2010	0.2728	0.5152	1 2431	0.3924	1 4429	0 5880	0.0941	1 9999	0 2395	2 6969	1 5680	3 7064	D 0879
2 0308	1 0043	0 1779	0 2475	0 2849	0.2800	5 0992	2 2466	2 2083	0.0988	0 0611	2 2454	0 9630	0.8355	4 0204
0 2145	2 5019	1 3019	1 6369	1 3499	0 6203	19 18	0 1670	0 1949	1 3440	0 2005	1 5 1 5 7	1 7353	0 9324	1 3523
1 1118	1 9728	0.6191	0.0149	0 5376	0.0046	0 6252	1 6281	0.2772	0 0556	0.4470	0 5266	0.8817	0.2427	1 1638
0 2432	0.7302	2 4 3 9 6	0.0779	1 0151	0.4888	1 2114	0 3606	0 0234	1 9367	1 2689	2 1829	0.3569	1 4470	0 9422
0 6834	1 2602	0.0440	3 6550	0.1032	1 5326	4 1297	1 2753	0.1516	0 3470	0 9681	0 4149	1 5600	1 7875	0 5968
0.8743	0 5972	0 5226	0.6086	0 4820	0.8126	0.7244	2 8622	1 2995	0 1391	1 0467	0 3153	0 7654	0.0526	0 6286
1 8945	0 0828	0 6279	0 5823	1 7757	0 1087	0 6876	0 5346	0 6817	0 1436	0 6388	0.6211	0 8468	0 9272	0.8470
1 6711	0 2592	2 1458	0 0449	3 1336	0 5581	0 1607	0 4598	0.7907	0 5938	2 7818	1 8210	1 2763	1 2032	0 0126
0 \$536	0 3020	0 7853	1 2 2 9 0	0 4552	0 0068	1 5 7 2 6	0.0027	0 0645	0 2775	3 1438	2 9250	0 8723	4 8510	1 2580
0 9866	0.9132	0 3053	0 3737	0 5469	0.0346	2 8317	0 2933	0 7938	0.2877	0.2119	0.8928	2 0636	0.5153	0.8829
1 3695	0.2366	1 7697	1.0209	0.7348	2 3026	0.0673	↑ 2728	0 5977	\$ 5840	1 0013	0.4362	0 4095	1 7154	0.081
0 5208	0 6984	1.0987	0 1917	0 6229	2 1011	0 0072	1 4618	1 1227	0 6920	0 3934	1 32 36	0 2127	0 1736	1 0093
2 2593	4 3931	1 4765	0 2746	2 681 1	0.0104	0.4500	0 2286	0 1451	0 2324	0 6069	1 2613	1 9487	1 2471	1 3712
1 0490	0 5225	0.2698	0 6562	0.3095	0 7785	0 3197	0 6824	0.3432	0 4526	2 7164	1 0550	0 6933	1 8137	1 7808
0.0518	0 3456	0.1365	0 4320	4 4838	1 1652	0.0927	0.7937	0.0223	1 4675	0.1545	1 4515	0 8765	0 1045	0 2228
0.7941	0.3201	0 0899	1 6611	0 5771	0.2266	0 3686	0 0393	0 8588	0.4303	0 4266	0.3845	0 5723	2 6542	0 6612
0 4676	0 5834	2 3247	0 7372	2 4606	0 3932	0 1851	1 6538	1.7101	1 4550	0.4140	0.0591	0.8581	3 3141	0.4378
0 9766	0.8192	4 1140	0 5508	0 3703	2 3148	0 0545	1 3626	0.3847	2 1840	3 6072	0 1066	0 7252	1 3741	0 8290
1 2443	0 5925	2 2355	0 1753	0.4353	0 7177	3 4943	0.8487	3 9863	2.8398	2 2733	0.4179	0 5265	1 6294	0 491;
0 6793	0.3157	1 6361	0 7469	2 5568	0 2092	0.0555	2 0506	0 1296	1 9426	0 0250	0 9036	1 3022	0.4394	0 6579
0 2690	0 4206	0 9004	2 7633	0.2804	2 7984	2 5987	0 1178	0.5429	1.6306	3.0790	1 1955	0.0738	0 1938	2 0874
0.2610	0 1912	091E 0	1 1692	2 8068	0.2948	0 1969	1 3823	2 1179	0 3821	1.8986	1 3541	0 1657	4 3879	3 3662

These are random numbers from the exponential distribution with mean I. They may be transformed to random numbers from any other exponential distribution with mean  $\mu$  samply by multiplying them by  $\mu$ . Thus a sample from the exponential distribution with mean 10 is 6 193, 18 350, 2.285, ..., etc

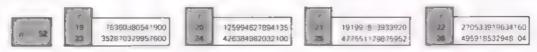
### Binomial coefficients

$\langle n \rangle$	_	/ n ) _	n†	_	$n(n-1)\ldots(n-r+1)$
(1)	_	(n-r)	r!(n-r)!		$\frac{n(n-1)\ldots(n-r+1)}{r(r-1)\ldots 1}$

for n = 1 to 36 and 52 (for playing-card problems)

11	11	10		8	7		5	4	3	2	1	0	1
$\neg$											1	1	1
- 1										1	2	1	2
									1	3	3	1	3
								1	4	6	4	1	4
							1	5	10	10	5	1	5
						1	6	15	20	15	6	7	6
			1		1	7	21	35	35	21	7	3	7
				1	В	28	56	70	56	28	8	1	8
			1	9	36	84	126	126	84	36	9	1	9
		1	10	45	120	210	252	210	120	45	10	1	10
1	1	11	55	165	330	462	462	330	165	55	11	1	11
12	12	66	220	495	792	924	792	495	220	66	12	3	2
78	78	286	715	1287	1716	1716	1287	715	286	78	13	1	3
64	364	1001	2002	3003	3432	3003	2002	1001	364	91	14	3	14
65	1365	3003	5005	64.35	6435	5005	3003	1365	455	105	15	1	15
88	4368	8008	11440	12870	11440	8008	4368	1820	560	120	16	1	6
76	12376	19448	24310	24310	19448	12376	6188	2380	680	136	17	1	7
24	31824	43758	49820	43758	31824	18564	8568	3060	816	153	18	1	8
82	76582	92378	92378	75582	50388	27132	11628	3876	969	171	19	1	9
BC	167960	184756	167960	125970	77520	38760	15504	4845	1140	190	20	1	20
18	352718	352716	293930	203490	116280	54264	20349	5985	1,330	210	21	1	1
32	708432	646846	497420	319770	170544	74613	26334	7315	1540	231	22	1	2
78	1352078	1144066	817190	490314	246157	100947	33649	8855	1271	253	23	1	3
44	2496144	1981256	1307504	735471	346104	134596	42504	10626	2024	276	24	1	4
00	4457400	3268760	2042975	1081575	480700	177100	53130	12650	2300	300	25	1	5
50	7726150	5311735	3124550	1562275	657900	230230	65780	14950	2800	325	26	3	6
36	13037896	8436286	4685826	2220075	888030	296010	80730	17550	2925	351	27	1	7
30	21474180	13123110	6906900	3108105	1184040	376740	98280	20475	3276	378	28	Ť	10
90	34697290	20030010	10015005	4292145	1560780	475020	118755	23751	3654	406	29	1	9
00	54627300	30045015	14307150	5852925	2035800	593775	142506	27405	4060	435	30	1	0
15	84672315	44352185	20160075	7888725	2629575	736281	169911	31465	4495	465	31	1	1 1
30	129024480	84512240	28048800	10518300	3365866	906192	201376	35960	4960	496	32	1	2
20	193536720	92561040	38567100	13884158	4272048	1107568	237336	40920	5456	528	33	1	3
30	286097760	131129140	52451256	18156204	5379618	1344904	278256	46375	5984	561	34	1	4
00	417225900	183579396	70807480	23535820	6724620	1623160	324632	52360	5545	595	35	1	5
16	800805296	254186858	94143280	30280340	8347680	1947792	376992	58905	7140	630	36	1	8
10	60403728840	15820024220	3679075400	752538150	133784560	20358520	2598960	270725	22100	1326	52	1	2

1	12	13	14	16	16	17		31
12	1							Т
1,3	3	3						
14	91	-14	1					ш
15	455	105	15	1				
5	1820	580	120	18	7			Ш
7	6188	2390	680	136	17	1		
П	18564	8568	3080	816	153	18	1	
9	50388	27132	11628	3876	969	171	19	ш
20	125970	77520	38760	15504	4845	1140	190	
1	293930	203490	116280	54264	20349	5985	1330	П
2	646846	497420	319770	170544	74613	26334	7315	ш
3	1352078	1144086	817190	490314	245157	100947	33649	Ш
4	2704158	2496144	1981256	1307504	736471	346104	134596	1
5	5200300	5200300	4457400	3268760	2042975	1081575	480700	1
6	9657.200	10400600	9651700	7726160	5311735	3124550	1562275	
7	17383860	20058300	20058300	17383860	13037895	B4 36285	4686875	
8	30421755	37442160	40116600	37442 60	30421755	21414180	131231 0	н
9	5 895935	67863915	77558760	77558760	67863915	51895935	34597290	ш
٥	B6493225	119759850	145422675	155117520	145422675	119754850	86493225	Ш
4	141120525	206253075	265182525	300540195	300540195	265182525	206253015	ш
2	225792840	347373600	471435600	565722720	601080390	565722720	471435800	. 3
3	354817320	573166440	818809200	1037158320	1166803110	1 66803110	1037158320	ш
đ	548354040	927983750	1391975640	1855967520	2203961430	2333606220	2203961430	
5	834451800	1476337800	2319959400	3247943160	4059928950	4537567650	4637567650	. 3
6	1251677700	2310789600	3796297200	5567902560	7307872110	8597496600	9075135300	
2	206379406870	635013559600	1768956344600	4481381406320	10363194502115	21945588357420	42671977361650	



The binomial coefficient  $\binom{n}{r}$  gives the number of different groups of r objects which may be selected from a collection of n objects: e.g. there are  $\binom{4}{2}$  of different pairs of letters which may be selected from the four letters A, B, C, D, they are (A, B), (A, C), (A, D), (B, C),

(B,D) and (C,D). The order of selection is presumed immaterial, so (B,A) is regarded as the same as (A,B) etc. As a more substantial example, the number of different hands of five cards which may be dealt from a full pack of 52 cards is  $\binom{52}{5} = 2598\,960$ .

### Reciprocals, squares, square roots and their reciprocals, and factorials

n	1/0	a <sup>3</sup>	√n	√10n	1Nn	1/√10n	In
1	1,0000	1	1.0000	3 1623	1.000	.31623	1
2	50000	4	1.4142	4.4721	7071	.22361	2
3	33333	8	1 7321	5.4772	5774	18257	6
4	25000	16	2.0000	6.3246	5000	15811	24
5	.20000	25	2 2361	7.0713	4472	14142	120
6	16687	36	2.4495	7 7460	4082	12910	720
7	14286	49	2.6458	8 3666	3780	11952	5,040
8	12500	64	2.8284	8 9443	3536	11180	40,320
9	11111	81	3.0000	9 4868	.3333	10541	362,880
10	10000	100	3.1623	10.000	.3162	10000	3,628,800
11	.09091	121	3.3166	10 488	.3015	.09535	39 916,800
12	.08333	144	3.4641	10 964	2087	.09129	4 7900 x 10 <sup>8</sup>
13	.07692	169	3.6056	11 402	.2774	.08771	6.2270 × 10°
14	07143	196	3 7417	11.832	.2673	.08452	8.7178 × 1010
15	.06667	225	3.8730	12 247	.2582	.08165	1 3077 x 10 <sup>12</sup>
16	06250	256	4 0000	12.649	2500	.07906	2.0923 × 10 <sup>13</sup>
17	.05882	289	4 1231	13.038	2425	07870	3.5569 × 10 <sup>14</sup>
18	05558	324	4.2426	13 416	2357	07454	6.4024 × 10 <sup>15</sup>
18	05263	361	4.3589	13 784	2294	07255	1.2165 x 1017
20	.05000	400	4.4721	14 142	2236	.07071	2.4329 x 10 <sup>18</sup>
21	.04762	441	4.5826	14.491	2182	.06901	5,1091 x 10 <sup>19</sup>
22	04546	484	4.6904	14.832	2132	.06742	1,1240 x 10 <sup>21</sup>
23	.04348	529	4 7958	15 166	2085	06594	2.5862 x 10 <sup>22</sup>
24	04167	576	4 8990	15 492	2041	06455	8.2046 x 10 <sup>13</sup>
25	.04000	625	5 0000	15.813	2000	.06325	1.5511 × 10 <sup>35</sup>
26	.03846	676	5.0990	16 125	1961	.06202	4.0329 x 10 <sup>26</sup>
27	.03704	729	5 1962	16 432	1925	.06086	1.0889 x 10 <sup>20</sup>
28	03571	784	5.2915	16 733	1890	.05976	3.0489 x 10 <sup>37</sup>
29 30	.03448	841 900	5.3852	17.029	1857	.05872	8.8418 × 10 <sup>30</sup> 2 6525 × 10 <sup>37</sup>
31	03226	961	5 5078	17 607	1798	05680	8 2228 × 10 <sup>33</sup>
32	.03125	1024	5.6569	17.889	1768	.05590	2.6313 x 10 <sup>35</sup>
33	03030	1089	5 7446	18 166	1741	05505	8.6833 x 10 <sup>34</sup>
34	.02941	1156	5.8310	18.439	1715	.05423	2.9523 x 10 <sup>30</sup>
35	02857	1225	5,9161	18 708	1690	.05345	1.0333 × 10 <sup>40</sup>
38	02778	1296	6.0000	18 974	1687	05270	$3.7199 \times 10^{41}$
37	02703	1369	6.0828	19 235	1644	.05199	1.3764 x 10 <sup>43</sup>
38	02632	1444	6 1644	19 494	1622	05130	5.2302 x 10 <sup>44</sup>
39	.02564	1521	8.2450	19 748	1601	05064	2,0398 x 10 <sup>44</sup>
40	.02500	1600	6.3246	20 000	1581	.05000	8.1592 × 104*
41	02439	1681	6 4031	20 248	1562	04939	3.3453 x 10 <sup>49</sup>
42	02381	1784	6.4807	20 494	1543	04880	1.4060 x 10 <sup>51</sup>
43	.02326	1849	6 5574	20 736	1525	04822	5.0415 x 10 <sup>53</sup>
44	02273	1936	6 6332	20 976	1508	04767	2.8583 x 10 <sup>94</sup>
45	02222	2025	6 7082	21.213	1491	04714	1.1982 x 10 <sup>36</sup>
46	02174	2116	6 7823	21 448	1474	.04663	5.5026 x 10 <sup>17</sup>
47	02174	2209	6.8557	21 679	1459	.04613	2.5862 × 10 <sup>35</sup>
48	02083	2304	6 9282	21 909	1443	.04564	1,2414 × 10 <sup>61</sup>
49	.02041	2401	7.0000	22 136	1429	04518	6.0628 × 10 <sup>62</sup>
50	02000	2500	7.0711	22.361	1414	04472	3 0414 × 10 <sup>94</sup>
100	UE LAND	5000	1.0711	1 00.33	1-11-4	21110	30717 10

n	1/a	n <sup>3</sup>	√n	√10n	1/√n	1/√10π	ni
51	.01961	2601	7,1414	22 583	,1400	.04428	1.5511 × 10 <sup>66</sup>
52	.01923	2704	7.2111	22.804	,1387	.04385	8.0658 × 10 <sup>67</sup>
53	.01887	2809	7.2801	23.022	,1374	.04344	4.2749 × 10 <sup>69</sup>
54	.01852	2916	7.3485	23.238	.1381	.04303	2.3084 x 10 <sup>71</sup>
55	.01818	3025	7.4162	23.452	.1348	.04284	1,2698 x 10 <sup>73</sup>
56	.01786	3136	7,4833	23.664	.1338	.04226	7.1100 x 10 <sup>74</sup>
57	.01754	3249	7.5498	23.875	,1325	.04189	4.0527 x 10 <sup>76</sup>
58	.01724	3364	7,6158	24,083	,1313	,04152	2.3506 x 10 <sup>76</sup>
59	.01695	3481	7.6811	24 290	.1302	.04117	1,3868 x 10 <sup>80</sup>
60	.01667	3800	7.7480	24.496	.1,291	.04082	8,3210 x 10 <sup>11</sup>
61	,01639	3721	7.8102	24.698	.1280	,04049	5,0758 x 10 <sup>13</sup>
62	.01613	3844	7,8740	24.900	.1270	.04018	3 1470 × 10 <sup>85</sup>
63	.01587	3969	7.9373	25,100	.1260	.03984	1.9826 x 10 <sup>87</sup>
64	.01563	4096	0.0000	25.298	.1260	.03963	1,2689 x 10 <sup>50</sup>
65	01538	4226	8.0623	25.495	1240	.03922	8 2477 x 10 <sup>90</sup>
98	.01516	4356	B.1240	25.690	.1231	.03892	5.4434 x 10 <sup>91</sup>
67	.01493	4489	8.1854	25.884	.1222	.03863	3.6471 x 10 <sup>94</sup>
60	,01471	4624	8.2482	26.077	.1213	.03835	2.4800 x 10 <sup>96</sup>
88	.01449	4761	5.3066	26.268	.1204	.03807	1.7112 x 10 <sup>94</sup>
70	.01429	4900	8,3666	26.458	,1105	.03780	1.1979 x 10 <sup>100</sup>
. 71	.01408	5041	8 4261	26.646	.1187	.03753	9.5048 × 10 <sup>61</sup>
72	.01389	5184	8.4853	26.833	.1179	.03727	6.1234 x 10 <sup>163</sup>
75	.01370	5329	8.5440	27.019	.1170	.03701	4,4701 x 10 <sup>101</sup>
74	.01351	5478	8.6023	27.203	.1162	.03678	3.3079 x 10 <sup>107</sup>
75	.01333	5625	8.6603	27.388	1155	.03651	2.4809 x 10 <sup>100</sup>
76	.01316	5776	8 7178	27 568	1147	,03627	1.8856 x 10 <sup>111</sup>
77	.01299	5829	8,7750	27.749	.1140	.03804	1.4518 x 10 <sup>111</sup>
78	.01282	8084	9.8318	27.028	.1132	.03581	1.1324 x 10 <sup>111</sup>
77	.01285	6241	8.8882	28.107	.1125	.03658	8.9462 x 10 <sup>116</sup>
80	01250	8400	8 9443	28 284	1118	03536	7 1589 × 10 <sup>116</sup>
81	01235	6561	9 0000	28.460	1111	.03514	6 7971 × 10 <sup>120</sup>
82	.01220	8724	9.0554	28.636	.1104	,03492	4,7536 x 10 <sup>173</sup>
83.	Ø1205	6889	9.1104	28.810	,1098	.03471	3.9466 × 10 <sup>124</sup>
184	.01190	7056	9.1652	28.983	.1001	.03460	3.3142 × 10 <sup>126</sup>
85	.01178	7225	9,2196	29.155	,1085	,03430	2,8171 × 10 <sup>138</sup>
86	.01163	7396	9 2736	29 326	1078	.03410	2 4227 x 10 <sup>130</sup>
37	.01148	7589	9.3274	29.496	.1072	.03390	2.1078 × 10 <sup>131</sup>
100	.01136	7744	9.3808	29.665	.1066	.03371	1.8548 x 10 <sup>134</sup>
38	.01124	7921	9.4340	20.833	.1000	.03352	1.8508 x 10 <sup>136</sup>
90	01111	8100	9.4868	30 000	1054	03333	1 4857 × 10 <sup>134</sup>
91	.01099	8281	9 5394	30 166	1048	03315	1 3520 × 10 <sup>140</sup>
92	.01087	8464	9,5917	30.332	.1043	.03297	1,2438 x 10 <sup>143</sup>
93 .	.01076	8649	9.6437	30,498	.1037	.03279	1.1568 x 10 <sup>144</sup>
94	.01084	8836	9.6954	30.650	.1031	.03262	1.0874 x 10 <sup>146</sup>
96	.01053	9025	9.7468	30.822	.1026	.03244	1.0330 x 10 <sup>148</sup>
96	.01042	9216	9.7980	30.984	.1021	.03227	9.9168 x 10 <sup>149</sup>
97	.01031	9409	9,8489	31,145	.1015	,03211	9,5193 x 10 <sup>193</sup>
98	.01020	9804	9.8995	31.305	.1010	.03194	9.4269 x 10 <sup>153</sup>
90	.01010	9801	9.9499	31,464	.1005	.03176	9.3326 x 10 <sup>136</sup>
100	01000	10000	10.000	31.623	1000	.03162	9 3326 x 10 <sup>157</sup>

### Useful constants

я	3 14159 26536
√n	1 77245 38509
	2 7 1828 18285
log <sub>e</sub> 10	2.30258 50930
$\sqrt{2}$	1 41421 35624

1/x	0.31830 98862
1/√≡	0.56418 95835
1/e	0.36787 94412
logios	0.43429 44819
1/√2	0.70710 67812

g <sup>2</sup>	9,86960 44011
√2π	2.50662 82746
V6	1.64872 12707
log,#	1 14472 38858
√3	1 73205 08076

11/12	0 10132 11836
1/√2π	0.39894 22804
1/√€	0.60653 06597
log <sub>10</sub> #	0.49714 98727
1/√3	0.57735 02692

# The negative exponential function: e-x

4	-	_	-	_	_	-	7		ŭ.	-	_			_		_						-				_	m			1	_			_	-				
H	ė.	20	all to	26	3 8	55	67	5 5	8 5	7 7	43	6	4 2	3 5	92	2 :	, 9		9	4	eT.	2 9		70	20		ė,	0 6		-	4	pr .			1 1/4	~	P4 C	1	b
H		38	2 2	19	1 6	28	45	25 5	4	42	1 27	3 3	m 9	196	23	17	2 2	- 2	Ξ	ς.	_	= 0	· ad	x	***	-	9 ,	, ,	T	₹	m	-				-	2 0	. 00	
l	0-	99	62	8	8 2	2 5	69	96		2 2	. 9	8 :	2 3	2 2	92			-		- :	G		2		٥	2		- 4	v	-	I <sub>e</sub> U	_		1	. 2	m	_	Pre	
ľ		25	8 2	9 5	D 15	5	=	9 :	, Y	2 -	90	22	33			Ø 4			_	e .	=		20	2	2	-			P3	~	A4.	~ /	- ~	2	-	_		10	
1				2				8 2			24			0 10		-		-	C	Ø		2 4		0	T	~	0 0	U lev	-	N	~	2 1	'4 P4	-		_		40	
H		Ľ		2 5							2				-	c 0		20	^	10 1	٠.		4	lg!	m	п	m /	1 ~	6	~	N	F						-	
l		6	D ^	25 25	r (1	PV	_	0 0	. ~	9	7	0 3	+	-0	- 6	20	1	9 90					PA.		_	-			- P	-	_	_		1	-		_	-	
I.	20			7 7			7	m ·								0 0			197	-	-		. ^-	N	Pq	,			-							0	00	П	
١,	-			40 0							· en			ra	П		, ,		Ph	٥.								4-		0	0	0 0			0	0	0 0	-	
t	+	-	72	0	e:		_		-		- 10	* "			.71				0		+			2			7.						0		i			Н	i
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0 1 2 3	2007 8669	2003	7964 2960	7324 2332 7340 734	7412 7419	7490 7497	7566 7574	7642 7649	7716 7723	2789 7796	7860 7868	7938	8069 8075	8129 8136 8142 814	8202 8209	8267 8274	8331 8338	8305 8401	8457 8463	8525	SATA BASAS	8008 8704	8756 8762	8814 8820	8975 8877 8875 888 8927 8927 8938	8982 8987	9036 9042	9606 0606	2138 9143 9149 915 2191 0106 0201 020	9248 9253	9289 9304	9350 9355	9400 9405	GARA SARGA DISZA DED	05.47 GKR2	9596 9600	9643 9647	9689 9694	9736 9741 974	9782 9786	9827 9832	5808 5807 5807 8808	9961 9962

### Glossary of symbols

		Main page			
4	Southern Connection William . W. 1	references			
A	factor for action limits on $\overline{X}$ -chart	41	S	the sign test statistic	28-29, 35
$a_1$	lower action limit on R-chart is a <sub>1</sub> R	41	2	unadjusted sample standard deviation:	
$a_2$	upper action limit on R-chart is a 2 R	41		$S = \{\Sigma (X - \bar{X})^2 / n\}^{1/2}$	
C	$= a/E\{R\} = 1/d_1$ ; conversion factor for	r .	Š	average value of S in pilot samples	41
	estimating o from sample range	41	2	adjusted sample standard deviation,	
c.d.f.	cumulative distribution function:			satisfying $E\{s^2\} = \sigma^2$ (but not $E\{s\} = \sigma$ )	,
	Prob $(X \leq x)$			with single sample, $s = \{\sum (X - \bar{X})^2 / (n - \bar{X})^2 \}$	1)}1/2
D	Kolmogorov-Smirnov two-sample test		ž.	average value of s in pilot samples	41
	statistic	28, 35	12, 17.	s adjusted sample variances	1.7
$D^{\bullet}$	$= n_A n_B D$	28, 31	T		28-29, 35
$D^2$	sum of squares of rank differences	35, 40	r	'Student' & statistic, test or distribution	20
$D_n$	test statistic for Kolmogorov-Smirnov		U	random variable having uniform	243
- 71	goodness-of-fit test or test for normalit		0	distribution on (0:1)	40
$D^{*}$ , $D$	one-sided versions of D <sub>n</sub>	26-27	U	the Mann-Whitney test statistic	42
d	$= E\{R\}/\sigma$ ; conversion factor from $\sigma$ to				28, 30, 35
d <sub>2</sub>	$= E\{R\}/E\{S\}$ ; conversion factor from	71	$U_A$	$=R_A-1n_A(n_A+1)$	28
0.5	S to R	41	$U_B$	$= R_B - \frac{1}{2} n_B (n_B + 1)$	28
4.	= $E\{R\}/E\{s\}$ ; conversion factor from	41	14/	factor for warning limits on X-chart	41
d <sub>3</sub>	i to R	41	WI	lower warning limit on R-chart is $w_1 \overline{R}$	41
$E\{ \}$		41	14'2	upper warning limit on R-chart is w2R	41
	expected, i.e. long-term mean, value of		X	random variable	
e e	= 2.718 28; base of natural logarithms	18, 46	X	value of X	
F	(Snedecor) F statistic, test or distribution	on 22-25	$X, X_1$	$, \vec{X}_2, \vec{Y}$ sample means	
$F_0(x)$	c.d.f. of (null) hypothesised probability	7	$\overline{X}$	average of sample means in pilot sample	8 41
	distribution	26	(X, Y)	matched-pair or bivariate (two-variable)	
$F_n(x)$	sample (empirical) c.d.f.; proportion of			quantity	28, 35
	sample values which are < x	26	Y	random variable	,
1	sample fraction; number of occurrences	8	9	value of Y	
	divided by sample size	10~13	Z	random variable having standard normal	
$f_1$	lower critical value for f, or confidence			distribution	18-20
	limit using F distribution	10-13, 22	7	value of Z	16-20
$f_2$	upper critical value for f, or confidence			, z(p) values obtained using Fisher's	10-20
	limit using F distribution	10-13, 22	41 4477	2-transformation	26 22
H	Kruskal-Wallis test statistic	28, 32-35		2-MERSIOT HIRLION	35-37
$H_0$	null hypothesis (usually of status quo	20, 52 55	O:	sometimes used in place of a2 if	
	or no difference)			one-sided test non-existent	28
$H_1$	alternative hypothesis (what a test is		$\alpha_1$	significance level for one-sided test	20
211	designed to detect)		of	significance level for left-hand tail	-
k		41.00	mg.	one-sided test	20
k	number of regression variables	22	$\alpha_1^R$	significance level for right-hand tail	20
	number of samples	28, 32-35	wil.	one-sided test	20
ln	logarithm to base e (natural logarithm),				20
log <sub>e</sub>	such that if $\log_e x = y$ then $e^y = x$	45, 47	03	significance level for two-sided test	20
logio	logarithm to base 10 (common		γ	confidence level for confidence intervals	
	logarithm), such that if $\log_{10}x = y$		$\mu, \mu_1, \mu_2$		ly
	then $10^y = x$	45, 48		distributions; $\mu = E\{X\}$	
M	Friedman's test statistic	28, 34-35	$\nu_{\varepsilon}\nu_{1}$ , $\nu_{2}$		
max {}	maximum (largest) value of	26		F distributions)	20-25
N	total number of observations	28, 32-33	- II	mathematical constant, = 3,141 59	18, 45
$N_C$	number of concordant pairs, i.e.		ρ	population linear correlation coefficient	35-39
	$(X_1, Y_1), (X_2, Y_2)$ with		Po	(null) hypothesised value of p	35
	$(X_1 - X_2)(Y_1 - Y_2) + ve$	35, 40	Σ	summation, e.g.	
$N_D$	number of discordant pairs, i.e.			$\Sigma X = \Sigma X_1 = X_1 + X_2 + X_3 + \dots$	
_	$(X_1, Y_1), (X_2, Y_2)$ with		$\sigma, \sigma_{I}, \epsilon$	D <sub>2</sub> population standard deviations;	
	$(X_1 - X_2)(Y_1 - Y_2) - ye$	35, 40		standard deviations of probability	
	, nA, nB, ni sample sizes	30, 40		distributions; $o = (E\{(X - \mu)^2\})^{1/2}$	
10.11.03	common sample size of equal-size sampl	50 34	02	population variance, variance of probabil	itv
n)	bromiel coefficient and be of excite	es 28, 34		distribution; $\sigma^2 = E\{(X - \mu)^2\}$	21
()	binomial coefficient; number of possible		7	the Kendall rank correlation coefficient	35, 40
	groups of r objects out of n	4, 44	Ф	c.d.f. of the standard normal	22, 40
p	binomial parameter, probability of even				8-20, 27
	happening at any trial of experiment	4			
	(null) hypothesised value of p	10~11	φ	ordinate of the standard normal curve	18-19
			$\chi^2$	chi-squared statistic, test or distribution	21
Q	quantile; the number x such that		<	is less than	
	$\operatorname{Prob}\left(X\leqslant x\right)=q$	20	<	is less than or equal to	
R	multiple correlation coefficient	22	>	is greater than	
R	sample range:		>	is greater than or equal to	
	maximum value - minimum value	41	#	is not equal to	
Ŕ	average range in pilot samples	41	+ ve	positive (> 0)	
	rank sums of samples A and B	28	- ve	negative (< 0)	
P	Sample linear correlation coefficient	35-39	11		- 18
$F_1, F_2$	lower and upper critical values for			modulus, absolute value, ignore minus sig	
	the Spearman rank correlation coefficien	35	[ ]	integer part; $[x]$ is the largest integer $\leq x$	
FB	Spearman (aux constation coefficie)	nt 35, 40	-	factorial, e.g. $4! = 4 \times 3 \times 2 \times 1 = 24$	44-45
				integral	

These tables have been carefully prepared for the many users of statistical analysis at an introductory level. The enthusiastic reception accorded to the author's *Statistics Tables* (1978) by specialist statisticians highlighted the need for a briefer set of tables to be tailored to the requirements of students who have to use statistical analysis but with no greater commitment to it than is represented by a basic and often brief introductory course.

Both the coverage and the presentation of this set of tables have been determined with great care. In contrast with competing sets at this level, the content should match closely the requirements of users, who need have little mathematical background. The book is a positive teaching and learning aid, not just a stark and impenetrable reference item. Most of the tables are accompanied by fully explanatory introductory text and by some examples of use. Each table has been designed and laid out carefully for maximum clarity and ease of use, features which the large page size should also reinforce. There are many new or improved tables, some being much more extensive than in competing books. In view of the increasing recognition of nonparametric tests for their convenience, ease of use and wide application, the tables covering these tests should prove especially valuable.

The tables should serve the needs of all users of elementary techniques of statistical analysis, from engineers and technicians to geographers and social scientists. All students taking first courses in statistical analysis will find them an invaluable aid.

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ROUTLEDGE

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